國立交通大學

電子工程系　　　電子研究所碩士班

碩士論文

喝啾式多層堆疊量子點雷射之特性
暨其適用於光學同調斷層掃描系統
之可行性分析研究

Characterization of

chirped-multilayer quantum dot laser and

feasibility study of its application on

Optical Coherence Tomography

研 究 生：黃俊仁

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摘　　　要

　　本篇論文主要是計對自行設計之啁啾式多層堆疊量子點寬頻雷射的同調性暨其是否適用於生醫領域上在近年來蓬勃發展的光學同調斷層掃描術(OCT)來做探討。為了定量寬頻光源的同調長度，我們架設了一套光纖式、並以程式自動控制的促動器來調整光程差的 Mach-Zehnder 式干涉儀，並搭配一張高速數位器卡整合成一套同調長度量測系統。為了驗證該量測系統的準確性，我們也用理論來數學模擬了頻譜形式較為簡單的雷射，並與之和實驗結果相比較。

　　為了提供 OCT 系統更高解析度的光源，我們嘗試設計了一種多層堆疊結構的量子點雷射(chirped- multilayer quantum dot laser diode, CMQD LD)，期望利用其基態與激發態同時雷射的特性得到高輸出功率的寬頻光源。我們藉有系統的量測來觀察該雷射的表現，包括其同調性，並發現當其操作於高電流時，於高解析度 0.1 nm 的量測條件下，單一量子態的發光頻譜寬度可達到 29 nm，且當中不存在任何 3dB 凹陷，而該頻譜中心位在 1270 nm，我們預估其同調長度可落在 50 μm 以內。由於縱向模態的存在，我們提出量測干涉圖將是用來評斷一個"寬頻"雷射是否合適於 OCT 系統應用的一個較直接且實際的方式。另外，於干涉圖中光程差為零的主峰，其半高寬可視為用來檢視雷射寬頻程度的重要依據。最後，我們也將提供 CMQD LD 在未來可以更適合做為 OCT 光源的設計思維。

Characterization of chirped-multilayer quantum dot laser and
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Optical Coherence Tomography

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Abstract

This thesis will focus on discussing the coherence of chirped multilayer quantum dot (CMQD) laser and feasibility study of its application on optical coherence tomography (OCT). To acquire the coherence information of CMQD, we have set up a fiber-based and delay-tunable Mach-Zehnder interferometer. The accuracy of measurement has been confirmed by mathematical simulation on commercial lasers.

To achieve an OCT light source with higher axial resolution, we have specially designed a chirped multilayer (N=10) quantum dot laser. The measurement of laser characteristics of CMQD was demonstrated, including interferograms. An extremely broad spectrum of 29 nm without any 3dB dip was achieved. It centered at 1270 nm and was expected to have a coherence length less than 50 μm. Due to the longitudinal modes, we conclude that measuring interferogram is a more direct and more practical way to decide if a "broad spectrum" laser is suitable or not for OCT application. Furthermore, the FWHM of the main peak in an interferogram could be viewed as an indicator for judging the broadness of the spectrum for a broadband laser. Finally, suggestions will be provided in order to improve the performance of CMQD.

致　　謝

碩班生涯兩年，說長不長，說短不短，轉晃眼就這樣過去，回首過往，我想這會是人生中最精華的一段。

有幸進到這個同時充滿活力與溫馨的實驗室，為我的研究生涯增添不少色彩。感謝 MBE 實驗室裡的總舵手---李建平老師，嚴謹的研究氣氛、完善的實驗設備、學術討論中給予的關鍵性指引以及令人振奮的鼓舞，無疑地是我個人在研究之路上動力來源，將是我未來努力朝向的目標。謝謝林聖迪老師，清晰的思路與時常地不吝叮嚀總提醒了自己可以改進、努力的地方，透徹的理解力與隨時保持對未知事物的積極求知慾，是我理想中的學習模範。感謝我的指導老師---林國瑞老師，針對專業領域地廣泛訓練與實驗上不吝地給予實質上協助，因此培養了自主學習和從錯誤中成長的學習態度，體驗到學習的真諦，會是我一生受用無窮的寶貴資源。更謝謝大學時期的專題老師電物系徐琅老師，當初對許多軟體的訓練讓我獲益良多。最後也鄭重感謝台大光電所蔡孟燦學長、電物所羅志偉老師，無私地教導並提供經驗上的珍貴資訊，是我在研究過程初期重要的引導者。

在碩士生涯初期得到不少應具備的實用基礎背景知識，感謝實驗室中的大學長羅明城、凌鴻緒與林大鈞，曾一同參與的馬拉松比賽會是我難忘的回憶，不論是玩樂或是做研究，認真面對生命中每件事物一直是我想要從中學習的。謝謝同是電物出身的潘建宏與蘇聖凱學長，曾在長晶、光路調整與研究方向上給予建議，伴我走過了不少學習中的瓶頸。感謝巫朝陽和林建宏學長，除了在程式及光學系統設計上慷慨給予幫助，閒暇一起丟球的時光帶給我不少充電的機會。謝謝同是電物的同屆夥伴 queena，同樣的背景與一路走來的相互扶持，感受到大學以來的感情延續。感謝林博、賴大師、品維、韋智、小傅，幾個實驗室同伴時常彼此分享並互相打氣，一起走過了不少低潮和艱難的時光。最重要的，感謝旭傑學長、小豪、JackSu、歪哥、皓皓、小微、小史，除了實驗上實質地給予協助、討論、分享，每天課後一

同用餐與定期出遊培養出共患難的感情，同時釋放了許多壓力，是我能夠一路走到此重要的推手，我想我會永遠珍惜並保持這段得來不易的情誼。

　　走出實驗室，仍然是在自己過去熟悉的交大，同樣留在新竹的電物同伴也扮演了我碩士過程中重要的地位。謝謝大頭、達叔在自己低潮時總是給我支持和鼓勵，不失為我的心靈導師。感謝古新安、小給和同寢六年的室友彥緯，在自己焦頭爛額的非常時期仍願意播時間陪我討論到凌晨並給予許多關鍵性的建議。謝謝小猴和牛奶願意幫我把連自己都看不下去的爛英文做了校稿的動作。感謝 yes、tsao、堯堯、大給，陪伴我走過許多不在實驗室的課餘時光，讓我都能以全新的面貌來面對看似艱困的每一天。

　　經過了許久的努力，不斷地克服接踵而至的挑戰，最後要感謝的，是默默在背後支持我的家人，爸、媽與兩個弟弟，比起給予的實質幫助，不論何時何地給我在精神上的支持，心照不宣的體會和諒解，使我在為自己奮鬥的同時能夠無後顧之憂，於此將這份畢業的喜悅獻給我的家人，謝謝。

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Chapter 1

Introduction

1.1 Optical Coherence Tomography (OCT)

Optical coherence tomography (OCT) is an emerging optical imaging and diagnostic technology in biomedical optics and medicine. OCT uses low-coherence interferometry to perform high resolution, cross-sectional and non-invasive imaging of the en-face internal microstructure in materials or biological tissues in a way that is analogous to ultrasonic pulse-echo imaging [1]. Tissue pathology can be imaged *in vivo* and in real time with resolutions of 1~15 μm, about one to two orders of magnitude finer than conventional ultrasound. The unique features of OCT make it a powerful imaging tool, which promises to enable many fundamental researches in many areas, especially in clinical applications.

OCT performs cross-sectional imaging by measuring the single axial magnitude and echo time delay of backscattered light (axial scan or A-scan) and then scanning the incident optical beam transversely, as shown in Fig. 1.1. The generated two-dimensional data set represents the optical backscattering in a cross-sectional plane through the sample. Images, or B-scans, can be displayed in false color or gray scale to visualize tissue morphology. Three-dimensional data sets can be generated by acquiring sequential cross-sectional images by scanning the incident optical beam in a raster pattern (C-scan). Three-dimensional OCT (3D-OCT) data contain comprehensive volumetric structural information and can be manipulated similar to magnetic resonance imaging (MRI) or computed tomography (CT).

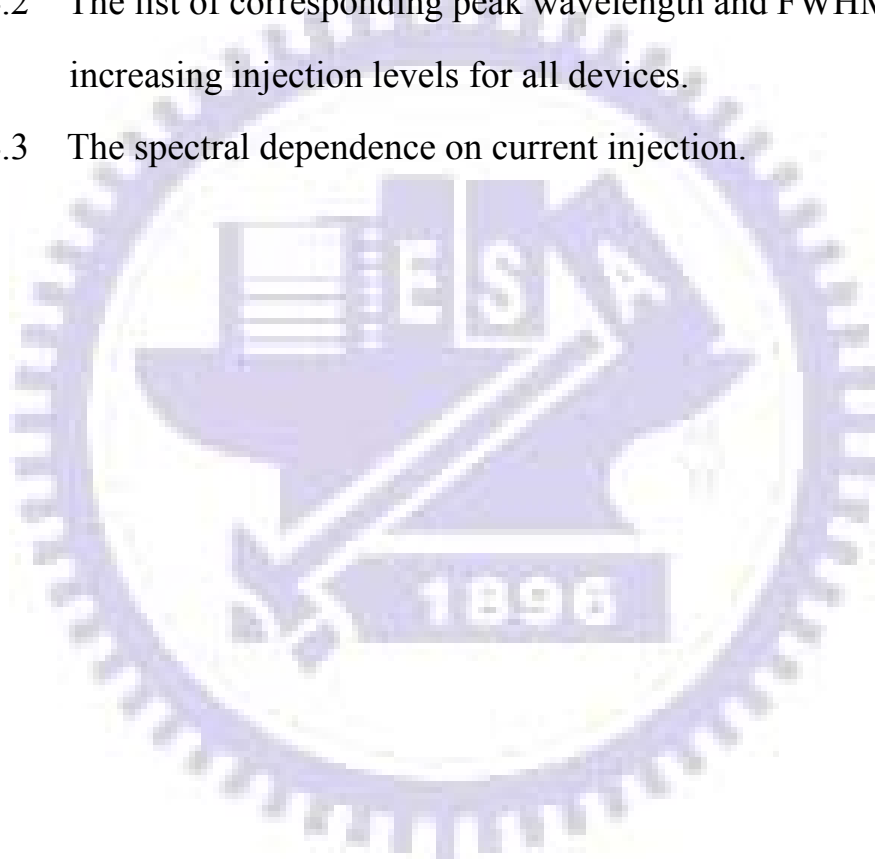| A scan	B scan	C scan
Axial (Z) scanning	Axial (Z) scanning	Axial (X) scanning
	Transverse (X) scanning	XY scanning
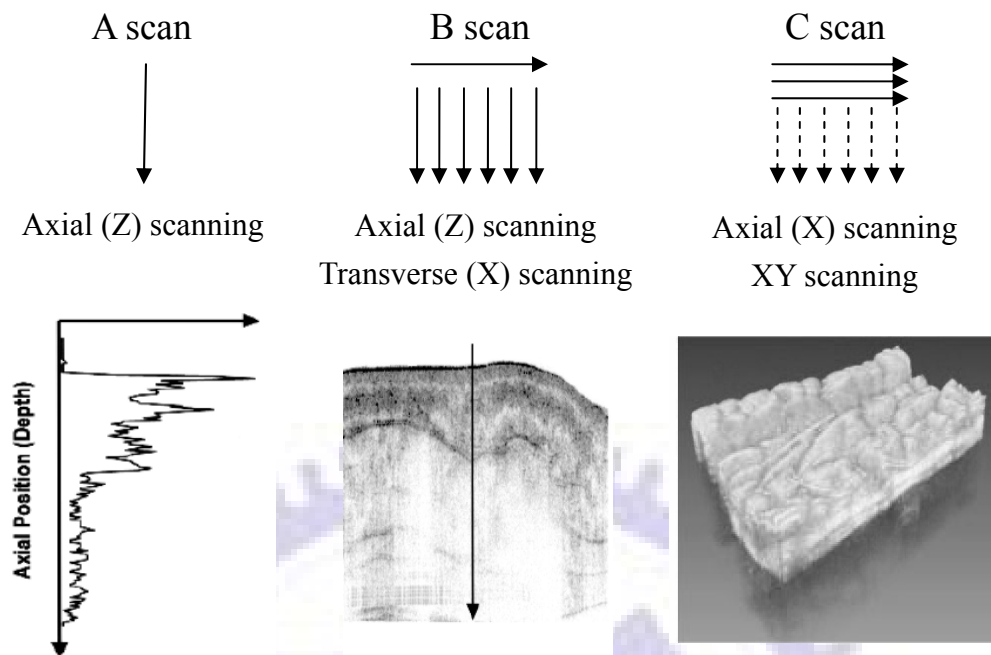
Fig. 1.1 A-scans measure the magnitude and echo time delay of backreflection or backscattering light. B-scans perform multiple axial scanning at different transverse position. By raster scanning a series of B-scan, C-scan or three-dimensional data set can be generated.

Without invasion and the need to remove and process the specimens, OCT has advantage in particular clinical situation [2]. For example, applications include tissues such as the eye, coronary arteries or nerve, where biopsy is harmful or impossible. By means of coupling with catheter, endoscope or other needle delivery devices, OCT gradually performs to have impact on many clinical areas ranging from gastrointestinal tracts to other internal medicine.

To understand what role that OCT plays in the biomedical imaging method, it's helpful to compare it with other conventional imaging technology. OCT imaging is analogous to ultrasound imaging except that it uses light instead of sound. Both the resolution and the penetration depth of ultrasound imaging depend on the frequency of sound wave

(3~40MHz) it uses [3]. High frequency ultrasound has been developed to achieve as high resolution as 15 μm with frequencies of ~100MHz. However, significant attenuation of the sound wave may occur with propagation and the imaging depths will be limited to only a few millimeters in such high frequencies. Microscopy and confocal microscopy are examples of high-resolution imaging modality. Resolution approaching 1 μm can be performed in an *en face* plane which is determined by the diffraction limit of light. However, imaging depth in biological tissue is limited to only a few hundred micrometers because optical signal and imaging contrast is strongly degraded by optical scattering.

OCT fills the gap between ultrasound and confocal microscopy, as shown in Fig. 1.2. The axial resolution in OCT depends on the bandwidth of the light source. Current OCT technologies have typically axial
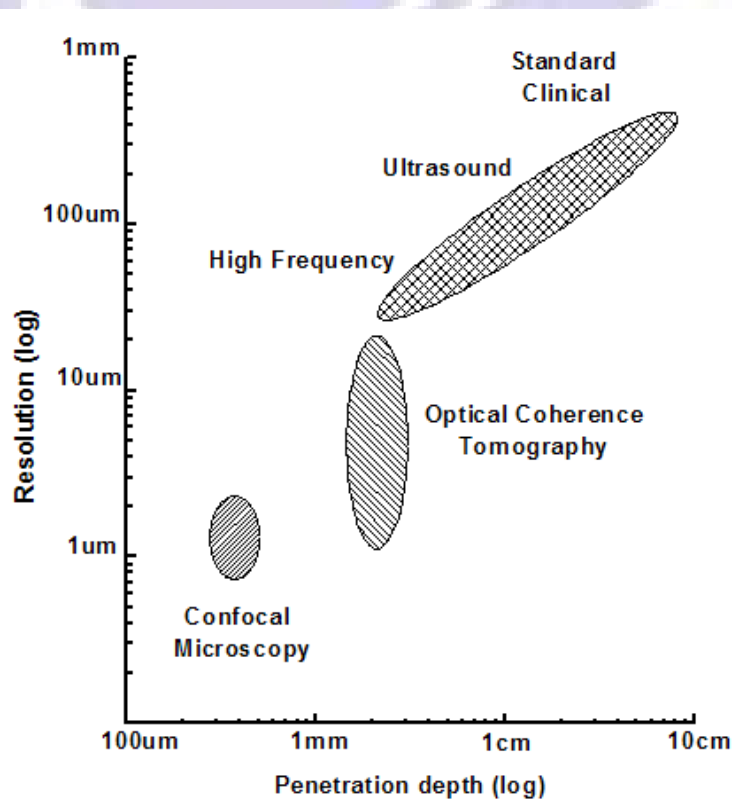
Fig. 1.2 OCT technology has typically axial resolution ranging from 1~15um and imaging depth about 2mm, which fills the gap between ultrasound and confocal microscopy.

resolutions ranging from 1 to 15 μm, approximately 10~100 times finer than standard ultrasound imaging. Recently, OCT has become a clinical standard in ophthalmology, because no other method can achieve non-invasive imaging with such high resolutions [4]. The major drawback of OCT is that light is strongly scattered by most biological tissues, and attenuation from scattering limits the image penetration depths to ~2 mm.

1.1.1 Time-Domain OCT (TD-OCT)

A general time-domain OCT (TD-OCT) system schematic is illustrated in Fig. 1.3. An incident broadband (low-coherence) and continuous wave (CW) light source is directed into a 2×2 fiber coupler implementing a Michelson interferometer. The coupler is assumed to split the incident light power equally into the reference and sample arms. Light existing the reference fiber is incident on a mirror which repetitively scans in length and provides a reference delay, and then it reflects back into the same fiber. Similarly, the light from the sample fiber is incident
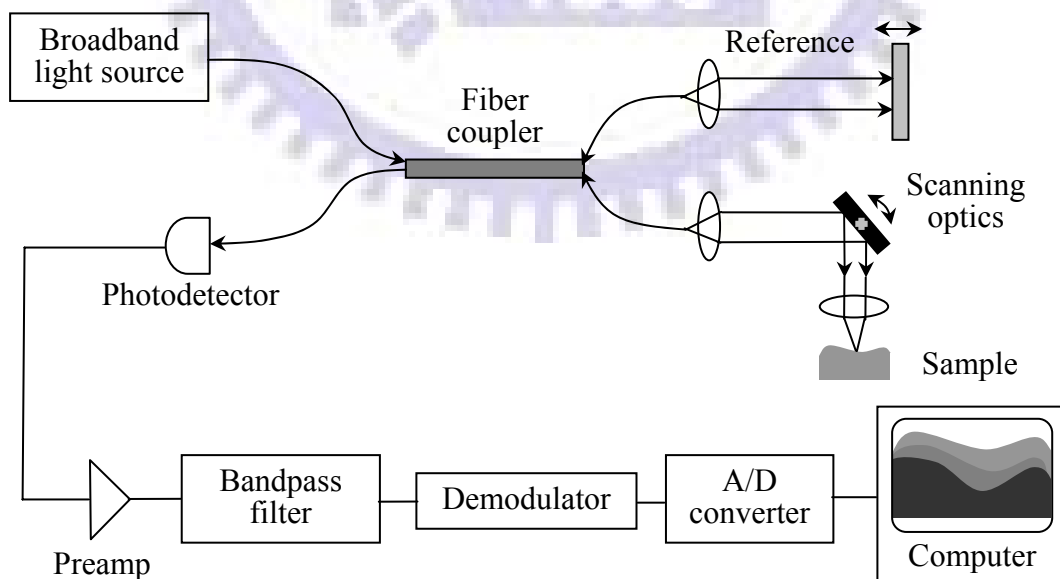
Fig. 1.3 A general time-domain OCT (TD-OCT) system schematic.

upon the investigated sample through a computer-controlled scanning mechanism designed to focus the beam onto the sample and to scan the focused spot in one or two transverse direction. The light backscattered or reflected from the sample is redirected back through the same optical scanning system into the sample arm fiber, where it is mixed with the returning reference arm light in the fiber coupler, and the combined light interfere on the surface of a single-channel photodetector. After processing the electronic signals received from the photodetector, the depth resolved reflectivity profile (or A-scan) at the focal spot of the sample beam at a specified transverse position can be generated. Demodulator plays an important role and is used to depict the envelope of the interference fringe pattern.

1.1.2   Axial and Transverse Resolution of OCT

To achieve higher quality of OCT imaging, image resolution has been a major research topic since OCT had been developed. Unlike standard microscopy, OCT has mutually independent axial and transverse resolution. OCT can achieve finer axial resolution independent of the spot size and the beam focusing. As in low-coherence interferometry, the axial resolution is determined by the width of the field autocorrelation function, which is inversely proportional to the bandwidth of the light source. Take a Gaussian-shape spectrum for example, the axial resolution or half coherence length (Δz) is related to the full-width-at-half-maximum (FWHM) of the power spectrum ($\Delta\lambda$) of the source by:

$$\Delta z = \frac{2\ln 2}{\pi}\frac{\lambda^2}{\Delta\lambda},$$

where λ is the center wavelength [5~6]. Since axial resolution is

inversely proportional to the bandwidth of the light source, ultra-broadband light sources are required for implementation of ultra-high resolution OCT (UHR-OCT).

The transverse resolution of OCT imaging is the same as that in the conventional optical microscopy and is determined by the diffraction limited spot size of the focused beam. The minimum spot size limited by diffraction is inversely proportional to the numerical aperture (NA) of the focusing optics. For a Gaussian beam, the transverse resolution or the minimum beam spot size is given by:

$$\Delta x = 2w_0 = \frac{2\lambda}{\pi\theta} \approx \frac{4\lambda}{\pi}\frac{f}{d} \approx \frac{2\lambda}{\pi \cdot NA},$$

where w_0 is the beam waist, θ is the convergence half-angle, d is the spot size of the beam on the objective lens and f is the focal length [7]. It means finer transverse resolution can be obtained by using larger NA which corresponds to a smaller spot size. However, the transverse resolution is also related to the depth of field or the confocal parameter b, which is two times the Rayleigh range:

$$b = 2z_R = \frac{2\pi(w_0)^2}{\lambda} = \frac{\pi(\Delta x)^2}{2\lambda},$$

Fig. 1.4 shows the relationship between the minimum spot size and the depth of field. Thus, similar to conventional microscopy, improving transverse resolution involves a trade-off in decreasing the depth of field at the same time. Typically, focusing optics with low NA is commonly employed in OCT because they have a relatively large Rayleigh range and thus provide longer depth of focus. In this way the axial resolution will be dominated by the coherence length of the light source, which is shorter than confocal parameter.
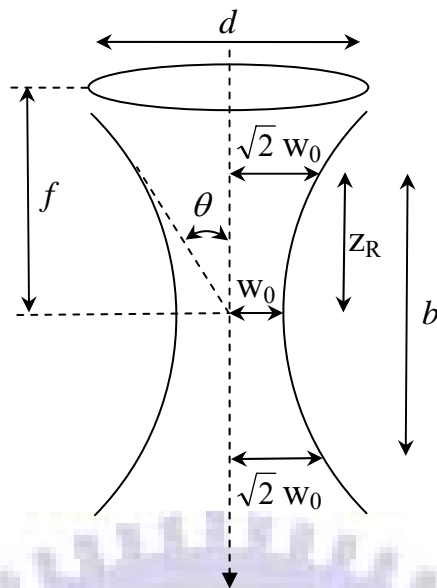
Fig. 1.4 The relationship between minimum spot size and depth of field.

1.1.3   Other types of OCT

To achieve real-time imaging, imaging speed becomes an important parameter in OCT. Recently, two types of Fourier domain detection have been developed to increase the imaging speed dramatically. These techniques are known as Fourier/spectral domain detection (SD-OCT) [8~11] and swept source/Fourier domain detection (SS-OCT) [12~14]. Unlike TD-OCT, SD-OCT performs high-resolution detection by measuring the interference spectrum with a low-coherence light source and a spectrometer. SS-OCT utilizes an interferometer with a narrow-bandwidth, frequency-swept light source and detectors to measure the interference signal as a function of time. The main reason that Fourier domain detection has a powerful sensitivity advantage over the time domain detection is that it essentially measures all the backscattered light simultaneously [14~16]. On the other hand, only the transverse scanning has to be performed. The depth information is provided by an inverse Fourier transform of the spectrum of the interference between the

backscattered light from fixed reference and sample. Such a sensitivity enhancement in Fourier-domain OCT corresponds to a boom in image speed.

For more information and details about OCT, see the reference [17].

1.2 Broadband emitters for OCT

In order to meet the requirement of broad spectrum, superluminescent diodes (SLDs) and femtosecond laser are two kinds of major low-coherence light sources in OCT.

1.2.1 Superluminescent Diodes (SLDs)

Briefly, SLD is the light output from laser structure below threshold. Operating at amplified spontaneous emission (ASE) and suppressing stimulated emission, SLD achieves wider spectrum than laser does by tilting the ridge structure. Compared to its competitive light sources, SLDs are now considered the most attractive light emitters due to their small size, easy use, and much lower price.

In the past, SLD could not become an ideal light source for OCT application because it was unable to meet all the demands simultaneously, including high optical power, broad spectrum, and negligible parasitic spectrum modulation. Early medical OCT application employed commercially available GaAs-based SLD, which operated at near 800nm with bandwidths of ~30 nm to achieve axial resolutions of ~10 μm in tissue. Besides, there have been advances in multiplexed SLD. Bandwidths broader than 150 nm but with limited power, which corresponds to axial resolutions as fine as 3-5 μm, can be achieved [18]. However, for scattering tissues, light sources with longer wavelengths are

essential to get enough penetration depth. At the same time, increasing of spectral wavelength results in increasing of coherence length which is proportional to square of wavelength. Therefore, SLD with centered wavelength at 1300 nm must be at least 2.5 times broader than 800nm counterpart to achieve the same resolution. Although much broader spectrum in multiple quantum well (MQW) and quantum dot (QD) SLDs at 1300~1550 nm have been demonstrated, spectral width of the most powerful (10~20 mW from SM fiber) commercial SLDs at 1300 nm is currently around 60~70 nm [19~20].

1.2.2 Femtosecond Lasers

Femtosecond lasers are the other powerful light sources for applications of ultra-high resolution OCT because they can generate extremely broad bandwidth spectrum at near infrared (IR) region. The Kerr lens modelocked (KLM) $Ti:Al_2O_3$ is the most commonly used technique in femtosecond optics and ultra-short pulse application. Through the development of double-chirped mirror technology (DCM) [21], high-performance $Ti:Al_2O_3$ laser has been implemented recently. Using state-of-the-art $Ti:Al_2O_3$ lasers, axial resolution of ~1 μm can be demonstrated [22]. Fig. 1.5 shows a comparison of the spectrum, autocorrelation function and its demodulated envelope (coherence length) of a typical SLD and a $Ti:Al_2O_3$ laser. A pioneering study of UHR-OCT in the retina reported by Drexler *et al*. shows axial resolution of ~3 μm by using a femtosecond laser light source [23]. In combination with nonlinearity, air-silica microstructure fibers or tapered fibers, $Ti:Al_2O_3$ laser can generate broadband continuum and achieve axial resolution of ~1 μm in the different spectral region ranging from visible to near IR [24~26]. Despite of their outstanding performance in bandwidth,
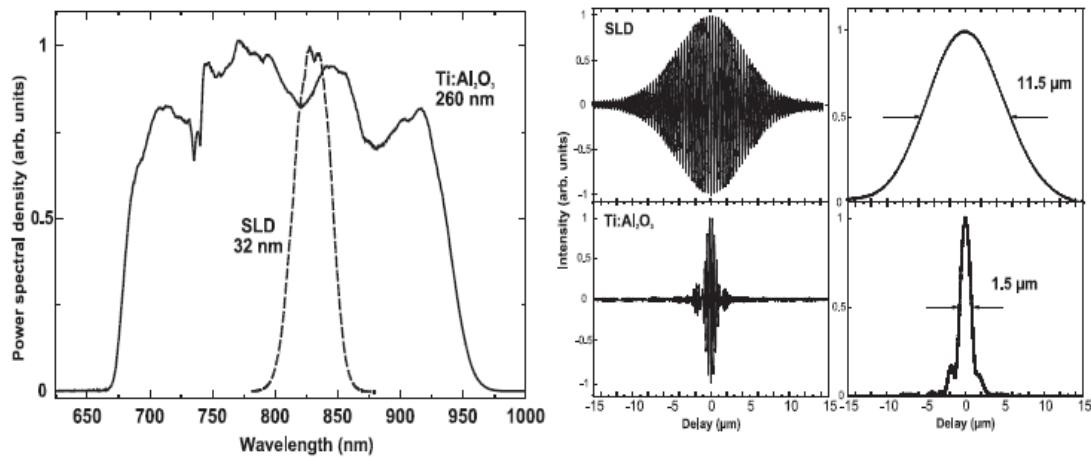
Fig.1.5 Optical bandwidth, interference signal and point spread function using a typical SLD and a femtosecond Ti:Al$_2$O$_3$ laser. For ultra-high resolution OCT, a broadband femtosecond laser with spectrum bandwidth ~260 nm can achieve a free space axial resolution of 1.5 μm.

femtosecond lasers are criticized due to its relatively high cost and complex. Recently, new Ti:Al$_2$O$_3$ lasers operate with much lower pump power and therefore greatly reducing cost has been developed [27].

1.3 Overview of Semiconductor Quantum Dot Lasers

Self-assembled quantum confined nanostructures, in the form of quantum dots, have been paid lots of attention due to its near delta-function of density of states (DOS) [28]. Ultralow threshold current density J_{th} [29], better temperature stability T_0 [30], high modulation bandwidth [31], low chirp [32], and small linewidth enhancement factor have been demonstrated [33]. Limited by the number of quantum dot (QD), the gain in QD saturates rapidly at a certain level, g_{st}, with increasing current density [34], which is the main difference of QD laser behavior from quantum well (QW) system. After the gain saturation at ground state (GS), carriers start accumulating at excited states (ES) and then achieve its threshold condition. For a specific laser device, GS

and/or ES lasing will be determined by its cavity length, density of QD, driving current, and other structural factors.

Broad-spectrum, high-power and highly efficient semiconductor light sources are strongly desirable for sensing and low-coherence imaging applications such as OCT. With higher power than SLD and more compactness than femtosecond laser, broadband semiconductor laser is more competitive if real supercontinuum broad bandwidth can be performed. Nevertheless, because of active material growth technology and fundamental physics, a conventional QW laser generally produces a narrow spectrum with a spectral width of the subnanometer order for a single-frequency laser to a few nanometers for multi-longitudinal mode lasers. Recently, simultaneous two-state lasing from the GS and ES has been observed from QD lasers with well-separated wavelength emissions [35]. Except for incomplete gain clamping at threshold stated as before, this behavior is also attributed to the retarded carrier relaxation process in QDs, which is also known as the phonon-bottleneck [36]. On the other hand, to achieve real broad laser spectrum of tens of nanometer scale from the QD laser, high dispersion in QD size and small energy spacing between quantized energy states that lead to the broadened optical gain characteristics play important roles as well. In fact, optical line broadening of the emission spectrum of a transition depends on both homogeneous and inhomogeneous broadening mechanisms. Besides the contribution of large dot size fluctuation towards inhomogeneous broadening phenomenon, mechanisms such as acoustic and optical phonon-carrier interaction, lifetime broadening, and carrier-carrier interaction greatly affect the homogeneous linewidth in semiconductors [37]. Lately, NL Nanosemiconductor demonstrated the extended lasing spectral width with uniform intensity distribution (only a 3dB modulation) of about 75 nm [38~39]. A broad lasing spectrum of 40 nm was also

demonstrated by H. S. Djie *et al* [40].

In this study, specially designed chirped-multilayered QD (CMQD) lasers with three kinds of different wavelength InAs-InGaAs QD stacks were grown. Besides, we have set up a fiber-based, delay-tunable Mach-Zehnder interferometer to measure the interferograms or autocorrelation function which can be used to quantitatively determine the coherence length of a light source. Except for achieving low threshold current density and high saturated modal gain, we demonstrate broad spectrum of 29 nm in this structure and expect that it could be improved to satisfy all the demands for a suitable OCT light source someday.
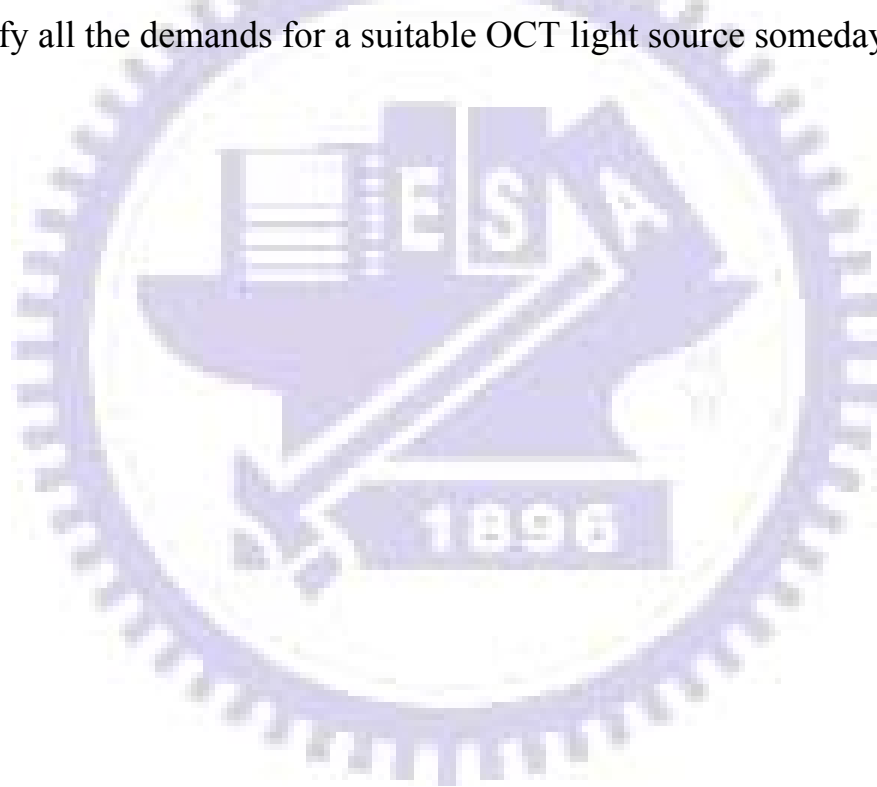
Chapter 2
Theoretical Fundamentals

2.1 Coherence Theory

In optics, the original sense of the word coherence was attributed to the ability of radiation to produce interference phenomena. Nowadays, the term of coherence is defined more specifically by the correlation properties between quantities of an optical field. Common interference is the simplest phenomenon showing correlations between light waves. It is convenient to divide coherence effects into two classifications, temporal and spatial. The former relates directly to the finite bandwidth of the light source, the latter to its finite extent in space. Experimentally, Michelson introduced a technique for measuring the temporal coherence by Michelson interferometer. Spatial coherence is illustrated by the double-slit experiment of Young. When it comes to coherence length, what we mainly consider here is temporal coherence.

2.1.1 Temporal Coherence

First of all, we consider the path of rays in a Michelson interferometer which is shown in Fig. 2.1. The incident light is divided into two beams by a beam splitter. One beam is reflected back onto itself by a fixed mirror, the other one is also reflected back by a mirror which can be shifted along the beam. Both reflected beams are divided again into two by the beam splitter, whereby one beam from each mirror propagates to a photodetector (PD). The idea of this arrangement is to superimpose a light wave with a time-shifted copy of itself.
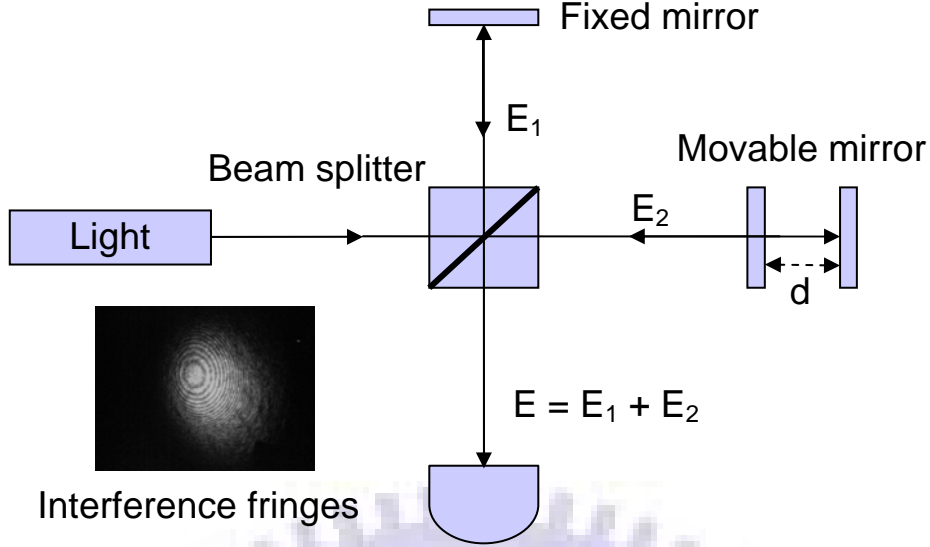
Fig.2.1 The Michelson interferometer.

Let E_1 be the light wave that reaches the screen via the fixed mirror and E_2 be the one that reaches the PD via the movable mirror. Then we have at a point on the PD, when the incoming wave has been split evenly at the beam splitter,

$$E_2(t) = E_1(t+\tau), \text{ or } E_1(t) = E_2(t-\tau). \tag{2.1}$$

The wave E_2 thus has to start earlier to reach the screen at time t due to the additional path of length $2d$. The quantity τ depends on the mirror displacement d according to

$$\tau = \frac{2d}{c}. \tag{2.2}$$

On the PD, the interference of both waves given by the superposition of the wave amplitudes:

$$E(t) = E_1(t) + E_2(t) = E_1(t) + E_1(t+\tau). \tag{2.3}$$

This superposition is not directly visible. A photodetector with a finite integration time detects the superposed light beams and provides the integrated/averaged intensity:

$$\begin{aligned} I &= \langle EE^* \rangle = \langle (E_1 + E_2)(E_1 + E_2)^* \rangle \\ &= \langle E_1 E_1^* \rangle + \langle E_2 E_2^* \rangle + \langle E_2 E_1^* \rangle + \langle E_1 E_2^* \rangle \end{aligned}$$

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$$= I_1 + I_2 + 2\,\mathrm{Re}\{\langle E_1^* E_2 \rangle\}$$
$$= 2I_1 + 2\,\mathrm{Re}\{\langle E_1^* E_2 \rangle\}\,. \tag{2.4}$$

The total intensity on the PD is given by the sum of the intensity I_1 of the first wave and I_2 of the second wave and an additional term, the interference term. The meaningful information is contained in the expression $\langle E_1^* E_2 \rangle$. With Eq. (2.1) this gives rise to the definition:

$$\Gamma(\tau) = \langle E_1^*(t)E_1(t+\tau)\rangle$$
$$= \lim_{T_m \to \infty} \frac{1}{T_m} \int_{-\frac{T_m}{2}}^{+\frac{T_m}{2}} E_1^*(t)E_1(t+\tau)dt\,. \tag{2.5}$$

$\Gamma(\tau)$ is known as the complex self coherence function. It is the autocorrelation function of the complex light wave $E_1(t)$. We then get

$$\mathrm{I}(\tau) = I_1 + I_2 + 2\,\mathrm{Re}\{\Gamma(\tau)\} = 2I_1 + 2\,\mathrm{Re}\{\Gamma(\tau)\}\,. \tag{2.6}$$

The complex self coherence function $\Gamma(\tau)$ can be normalized:

$$\gamma(\tau) = \frac{\Gamma(\tau)}{\Gamma(0)}\,. \tag{2.7}$$

The magnitude $\gamma(\tau)$ is called the complex degree of self coherence. Because $\Gamma(0) = I_1$ is always real and is the largest value that occurs when we take the modulus of the autocorrelation function $\Gamma(\tau)$, we have

$$|\gamma(\tau)| \le 1\,. \tag{2.8}$$

Then the intensity $\mathrm{I}(\tau)$ can be written by

$$\mathrm{I}(\tau) = 2I_1 + 2I_1\,\mathrm{Re}\{\gamma(\tau)\}$$
$$= 2I_1(1 + \mathrm{Re}\{\gamma(\tau)\})\,. \tag{2.9}$$

Actually, $\Gamma(\tau)$ and $\gamma(\tau)$ are not directly obtainable. It is, however, easy to determine the contrast K between interference fringes. This quantity has been used by *Michelson* who called it visibility and defined

it via the maximum and minimum intensity $I_{\max}$ and $I_{\min}$ as

$$K = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}. \qquad (2.10)$$

Obviously, the maximum and the minimum intensity of the interference fringes do not occur at the same time shift of the light waves; that is, K is a function of τ. Let τ_1 and τ_2, $\tau_2 > \tau_1$, be the time shifts belonging to adjacent interference fringes of $I_{\max}(\tau_1)$ and $I_{\min}(\tau_2)$. Then the contrast $K(\tau)$ is defined on the interval $[\tau_1, \tau_2)$ by

$$K(\tau) = \frac{I_{\max}(\tau_1) - I_{\min}(\tau_2)}{I_{\max}(\tau_1) + I_{\min}(\tau_2)}. \qquad (2.11)$$

$\tau_2 - \tau_1$ corresponds to half a mean wavelength, which is small compared to the duration of the wave train to be investigated. Only in this case does the definition make sense. According to Eq. (2.6), the maximum intensity is attained at maximum $\mathrm{Re}\{\Gamma(\tau)\}$, occurring at τ_1, and the minimum intensity at minimum $\mathrm{Re}\{\Gamma(\tau)\}$, occurring at τ_2. It follows, for τ taken from this interval, that

$$\mathrm{Re}\{\Gamma(\tau_1)\} = |\Gamma(\tau)| \quad \text{and} \quad \mathrm{Re}\{\Gamma(\tau_2)\} = -|\Gamma(\tau)|. \qquad (2.12)$$

This leads to the intensities

$$I_{\max}(\tau_1) = 2I_1 + 2\,\mathrm{Re}\{\Gamma(\tau_1)\} = 2I_1 + 2|\Gamma(\tau)|, \qquad (2.13)$$
$$I_{\min}(\tau_2) = 2I_1 + 2\,\mathrm{Re}\{\Gamma(\tau_2)\} = 2I_1 - 2|\Gamma(\tau)|, \qquad (2.14)$$

and to the contrast function

$$K(\tau) = \frac{2I_1 + 2|\Gamma(\tau)| - 2I_1 + 2|\Gamma(\tau)|}{2I_1 + 2|\Gamma(\tau)| + 2I_1 - 2|\Gamma(\tau)|}$$

$$= \frac{4|\Gamma(\tau)|}{4I_1} = \frac{|\Gamma(\tau)|}{I_1} = \frac{|\Gamma(\tau)|}{\Gamma(0)}$$

$$= |\gamma(\tau)|. \qquad (2.15)$$

The visibility then is identical to the modulus of the complex degree of

coherence. This is valid for two waves of equal intensity, otherwise some prefactors will arise. Fig.2.2 shows the self coherence function $\Gamma(\tau)$ in the complex plane (*up*) and contrast function $K(\tau)$ (*down*) for different light sources. Light in the large range in between the two limiting cases, completely coherent and completely incoherent, is called partially coherent. The following cases are distinguished ($\tau \neq 0, |\gamma(0)| = 1$) :

$$|\gamma(\tau)| \equiv 1 \quad completely \ coherent,$$
$$0 \leq |\gamma(\tau)| \leq 1 \quad partially \ coherent,$$
$$|\gamma(\tau)| \equiv 0 \quad completely \ incoherent,$$

All real light sources are partially coherent. Most part of natural and artificial light sources have a monotonously decreasing contrast function; for instance, the light from a mercury lamp. To characterize the decay of the contrast function, the coherence time τ_c is introduced. It is defined as the time delay when the contrast function has dropped to $1/2$ or possibly $1/e$ of its maximum value. In other words, it specifies the duration of time that a source maintains its phase. Equivalently to the coherence time, the coherence length

$$l_c = c\tau_c, \tag{2.16}$$

Completely coherent   Completely incoherent   Partially incoherent
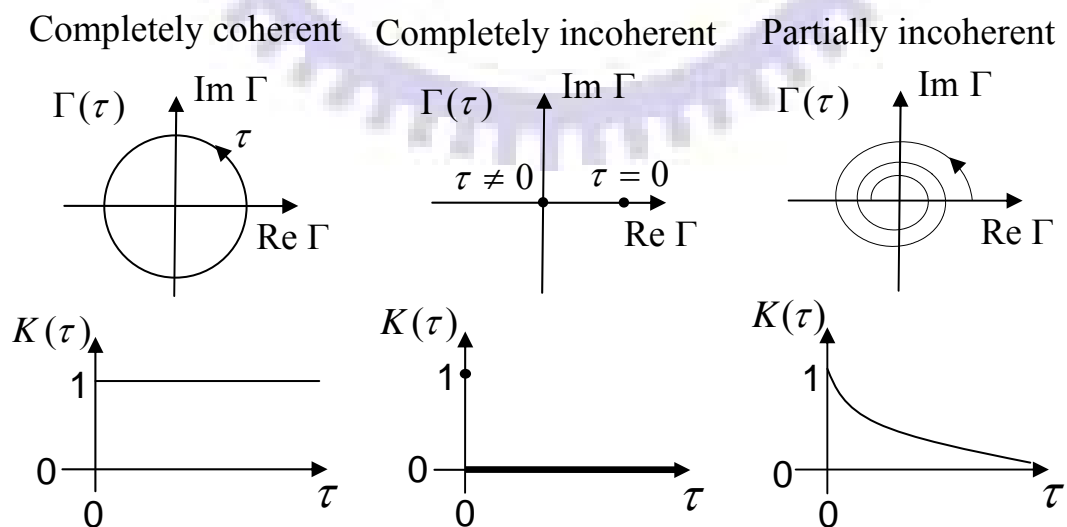
Fig.2.2 Graph of the self coherence function $\Gamma(\tau)$, and the contrast function $K(\tau)$ for light from completely coherent, completely incoherent, and partially coherent light, respectively.

is used for characterizing the interference properties of light. Typical values of the coherence length are some micrometers for incandescent light and some kilometers for single-mode laser light.

In a word, to determine the coherence length of some light source experimentally, all we have to do is to measure the interferogram or autocorrelation with enough path difference by a delay-tunable interferometer. After extracting the AC component and then detecting its envelope, we can define the FWHM of this profile as the coherence time. Coherence length will be obtained after multiplying coherence time by the light speed, c.

2.1.2 Wiener-Khinchin Theorem

When it comes to coherence of a light source, its spectral bandwidth plays an important role. A connection between the autocorrelation of a function and its Fourier transform is established by the Wiener-Khinchin theorem. It states that the autocorrelation and the power spectrum of a function are Fourier transforms of one another. In the time domain, if $f(t)$ is a radiated electric field, $|f(t)|^2$ is proportional to the radiant flux or power, and the total emitted energy is proportional to $\int_0^\infty |f(t)|^2 dt$. In the frequency domain, $F(\omega)$ is the Fourier transform of $f(t)$, which is called the field spectrum. $|F(\omega)|^2 = F^*(\omega)F(\omega)$ must be a measure of the radiated energy per unit frequency interval, which is sometimes called the power spectrum. In other words, $|F(\omega)|^2$ is just what we measure from the optical spectrum analyzer (OSA).

According to the definition, the autocorrelation of $f(t)$ is denoted by

$$\Gamma(\tau) = \int_{-\infty}^{+\infty} f^*(t)f(t+\tau)dt \tag{2.17}$$

Let $F(\omega)$ be the Fourier transform of $f(t)$, denoted by $FT\{f(t)\}$.

$$FT\{f(t)\} = F(\omega) = \int_{-\infty}^{+\infty} f(t)e^{-i\omega t} dt \tag{2.18}$$

The autocorrelation can be rewrite to

$$\int_{-\infty}^{+\infty} f^*(t)f(t+\tau)dt = \int_{-\infty}^{+\infty} [\frac{1}{2\pi} \int_{-\infty}^{+\infty} F^*(\omega)e^{-i\omega t} d\omega] \times f(t+\tau)dt \tag{2.19}$$

Changing the order of integration, we obtain

$$\frac{1}{2\pi} \int_{-\infty}^{+\infty} F^*(\omega)[\int_{-\infty}^{+\infty} f(t+\tau)e^{-i\omega t} dt]d\omega = \frac{1}{2\pi} \int_{-\infty}^{+\infty} F^*(\omega) \times FT\{f(t+\tau)\}d\omega$$

In the last integral, notice that

$$f(t+\tau) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} F(\omega)e^{+i\omega(t+\tau)} d\omega] = IFT\{F(\omega)e^{+i\omega\tau}\}$$

IFT means inverse Fourier transform. Then, Eq. (2.19) becomes

$$\int_{-\infty}^{+\infty} f^*(t)f(t+\tau)dt = \frac{1}{2\pi} \int_{-\infty}^{+\infty} F^*(\omega)F(\omega)e^{+i\omega\tau} d\omega \tag{2.20}$$

and both sides are functions of the parameter τ. If we take the transform of both sides, Eq. (2.20) then becomes

$$FT\{\Gamma(\tau)\} = |F(\omega)|^2 \tag{2.21}$$

This is a form of the Wiener-Khinchin theorem. It allows for determination of the spectrum by way of the autocorrelation of the generation function. By the way, Wiener-Khinchin theorem is the main idea in Fourier-Transform Spectroscopy (FTS). The variable part of the interference function, on Fourier transformation, yields the spectrum. It is now used widely in the infrared region because of the improved signal-to-noise (S/N) ratio, high throughput, and high resolution possible with it.

2.2 Semiconductor Quantum Dots

In this chapter, I will discuss about the density of state (DOS) in semiconductor, the formation of quantum dots and the carrier transition between excited states and ground state in quantum dots.

2.2.1 Ideal Quantum Systems

In semiconductor, an interaction between electrons of neighboring atoms is sufficiently strong. This interaction splits an atomic energy level to as many sublevels as the number of atoms contained in the system. These sublevels are grouped in bands. The width of a band is controlled by the strength of interaction of electronic shells, that is, interatomic spacing. In semiconducting crystals, where the interatomic spacing is set by the lattice constant in the range of few angstroms, the width of the order of several electron volts is typical for the valence (the last occupied) and conduction (the first empty) bands. The energy gap, which exists between these two allowed bands, contains no electronic states and is known as the forbidden band. Its width ranges from several electron volts (insulators) to zero (metals).

The number of allowed states within a given band is roughly equal to the number of atoms inside the crystal. It is as many as few 10^{22} electrons per cubic centimeter. However, these states are not distributed uniformly within the band. To characterize this distribution, a DOS is introduced. DOS is a function of energy $\rho(E)$ and it is a measure of allowed electronic states within unit energy interval per unit volume of crystal:

$$\rho(E) = (1/V)(dN/dE) . \tag{2.22}$$

DOS has dimensionality of energy^{-1} volume^{-1} and shows how many states are available within unit energy interval around some energy E in a crystal of unit volume. Eq. (2.23)~(2.30) are the corresponding dispersion relation and DOS for four kinds of ideal quantum systems:

Bulk:

$$E(\vec{k}) = E(k_x, k_y, k_z) = \frac{\eta^2}{2m^*}(k_x^2 + k_y^2 + k_z^2) + E_0 \tag{2.23}$$

$$\rho^{3D}(E) = \frac{(2m^*/\eta^2)^{3/2}}{2\pi^2}(E - E_0)^{1/2} \tag{2.24}$$

Quantum Well (QW):

$$E(\vec{k}) = E_n(k_x, k_y) = \frac{\eta^2}{2m^*}[k_x^2 + k_y^2 + (\frac{n\pi}{L_z})^2] + E_0 \tag{2.25}$$

$$\rho^{2D}(E) = \frac{m^*}{\pi\eta^2 L_z}\sum_n \Theta(E - E_n) \tag{2.26}$$

Quantum Wire (QWire):

$$E(\vec{k}) = E_{m,n}(k_x) = \frac{\eta^2}{2m^*}[k_x^2 + (\frac{m\pi}{L_y})^2 + (\frac{n\pi}{L_z})^2] + E_0 \tag{2.27}$$

$$\rho^{1D}(E) = \frac{n_{QWire}\sqrt{2m^*}}{\pi\eta}\sum_n\sum_m (E - E_{n,m})^{-1/2} \tag{2.28}$$

Quantum Dot (QD):

$$E(\vec{k}) = E_{l,m,n} = \frac{\eta^2}{2m^*}[(\frac{l\pi}{L_x})^2 + (\frac{m\pi}{L_y})^2 + (\frac{n\pi}{L_z})^2] + E_0 \tag{2.29}$$

$$\rho^{0D}(E) = 2n_{QD}\sum_n\sum_m\sum_l \delta(E - E_{n,m,l}) \tag{2.30}$$

where E_0 is the energy of the band edge of the corresponding band; $\Theta(E - E_n)$ is step-function which returns zero if $E < E_n$ or unity otherwise; $\delta(E - E_{n,m,l})$ is the delta-function; and n_{Qwire} (cm^{-1}) and n_{QD}

(cm^{-2}) are the surface density of quantum wires and QDs, respectively. Fig. 2.3 illustrates the schematic view and DOS of various ideal quantum nanostructures.
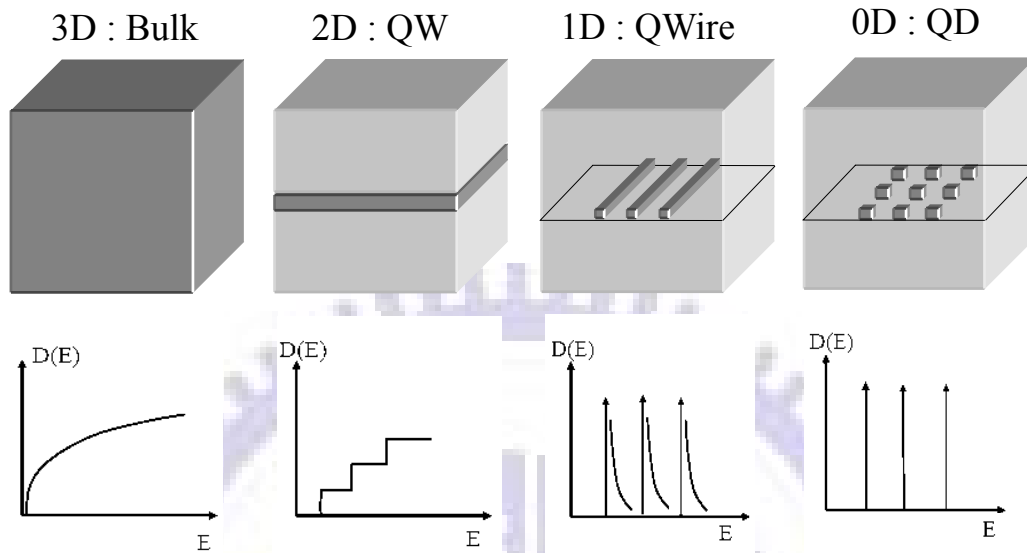
Fig. 2.3 Schematic view and DOS for various quantum nanostructures.

2.2.2 Structural Characteristics of Quantum Dots

To realize quantum dot structure, various techniques based on self-organization have been intensively investigated recently instead of conventional lithography-based or regrowth technology. The self-organized quantum dots have high crystal quality, and they are small enough to exhibit quantum confined effects. Among several techniques, the Stranski-Krastanow (S-K) growth in highly strained heteroepitaxial systems is most studied by using molecular beam epitaxy (MBE) or metalorganic chemical vapor deposition (MOCVD). Cluster formation occurred during epitaxial growth of a semiconductor material on top of another one that has a lattice constant several percent smaller, for instance, InAs on GaAs substrate. For the first few atomic layers, the atoms arrange themselves in a planar layer called the wetting layer. As the

epitaxial overgrowth proceeds, the atoms tend to bunch up and form clusters (quantum dots). It is energetic favorable, because the lattice can elastically relax the compressive strain and thus reduce strain energy within the islands.

The size of the islands can be adjusted within a certain range by changing the amount of deposited dot material. The change in size corresponds to an energy shift of the emitted light, which is due to the altered carrier confinement and strain in the dots. On the other hand, to obtain the information about structural and morphological characteristics of QDs, atomic force microscopy (AFM), scanning tunneling microscopy (STM), transmission electron microscopy (TEM), and photoluminescence (PL) spectroscopy are the most well-known and widely adopted methods. In fact, except for its shape and size, the energetic property of QDs also depends on the thickness and the highness of potential barrier of the capping layer.

2.2.3 Carrier transition in Quantum Dots

To achieve population inversion, fast intraband relaxation time is required. In quantum well systems, the typical intraband relaxation lifetime is about 0.1~1 picoseconds (ps). However, due to the lack of phonons needed to satisfy the energy conservation rule, the carrier relaxation into the discrete ground state is significantly slowed down in QDs (the so-called phonon bottleneck). Retarded carrier relaxation, with a lifetime ranging from several tens to hundreds of picoseconds, has been observed in many experiments using time-resolved PL. Even though Auger-like process and carrier-carrier scattering have been suggested for possible fast relaxation channels with a lifetime of 10 ps or less, the bottleneck effect still affects QD laser performance to some extent, such

as the degradation of threshold current and the external quantum efficiency.

2.3   Quantum Dot Lasers

Laser is an acronym meaning "light amplification by stimulated emission of radiation". A semiconductor, owing to a possibility of direct injection of electrons to the active region, gives an opportunity to make compact and efficient laser device. Basically, laser consists of the light-amplifying region where inverse population takes place and the positive optical feedback.

2.3.1 Basic Principles of Diode Lasers

In semiconductor, photon emission due to electron return from the conduction band to the valence band can be considered as radiative recombination of electron-hole pair. However, electron can also lose its energy non-radiatively. For any light-emitting device, too non-radiative recombination results in additional consumption of excited electrons and has to be minimized. Actually, there are two possible mechanisms when photon emission occurs. One is spontaneous emission with arbitrary phase, arbitrary direction and at an unpredictable instant of time. Otherwise, photon emission can be triggered by another photon, the so-called stimulated emission, and holds all the properties of the initial one.

Under condition of thermal equilibrium, light emission is balanced by the light absorption. The following equation connects the electron, n, and hole, p, concentrations:

$$np = n_i^2 \tag{2.32}$$

Here n_i is intrinsic concentration governed by temperature. To overcome this loss of photons, larger population of the upper level than that of the ground level is required. This situation, the so-called population inversion, is obviously non-equilibrium and can be reached by some external influence, such as illumination or current injection.

$$np > n_i^2 \tag{2.33}$$

To describe concentrations of electron and hole, their non-equilibrium Fermi levels, F_C and F_V are introduced. A condition of inverse population means that electron population probability of the conduction band state $f_C(E_C)$ having energy E_C is higher than that of the valence band state with E_V energy:

$$f_C(E_C) > f_V(E_V) \tag{2.34}$$

where population probability of carriers in semiconductor follows Fermi-Dirac distribution:

$$f_C(E_C) = \frac{1}{1 + \exp((E_C - F_C)/k_B T)} \tag{2.35}$$

Taking into account these expressions, the condition of inverse population comes to the following inequality:

$$F_C - F_V > E_C - E_V = E_g \tag{2.36}$$

It means that energy separation of electron and hole Fermi levels has to be larger than the band gap of a semiconductor, E_g. At this moment, so-called *transparency* takes place. Material becomes transparent for light of the given energy $\eta\omega = E_C - E_V$. The corresponding density of injection current is known as the transparency current density.

2.3.2 Optical Gain and Laser Threshold

When light propagates through a medium, its intensity, Φ, will be attenuated due to light absorption, which is characterized by absorption coefficient α. Mechanisms which contribute to optical loss have various origins. They usually are divided into the output (mirror) loss, α_m, caused by light output from the cavity and the internal loss, α_i, which combines the effect of all the other mechanisms. However, if population inversion takes place in the medium, the absorption coefficient changes sign to negative due to stimulated emission dominates the light absorption. To emphasize these two different cases of light absorption or light amplification, optical gain coefficient, G, is introduced. Now we consider the output loss inside a Fabry-Perrot cavity as shown in Fig. 2.4.

Let us assume that light propagating from the left to the right facet has intensity Φ_0 at its initial position at the left facet. Over the length L it becomes to $\Phi_0 \exp[(G - \alpha_i)L]$. After partial reflection at right facet having reflectivity R_1, a beam of intensity $R_1\Phi_0 \exp[(G - \alpha_i)L]$ starts from right to left. In the similar manner, the intensity of the light becomes equal to $R_1 R_2 \Phi_0 \exp[2(G - \alpha_i)L]$ at its initial position after a round trip, where R_2 is the left-facet reflectivity. In steady state (at threshold), this
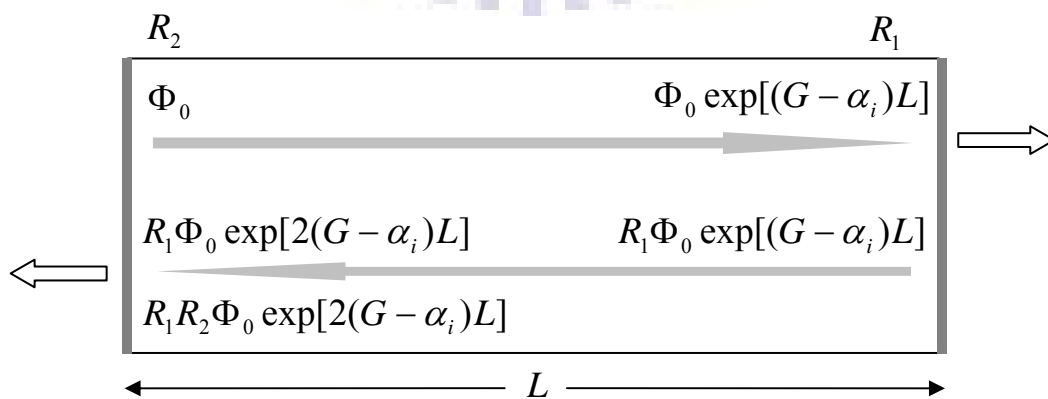

Fig. 2.4 Light propagation and its intensity in a round-trip cycle inside the Fabry-Perrot cavity.

round trip results in no change of the light intensity.

$$\Phi_0 = R_1 R_2 \Phi_0 \exp[2(G_{th} - \alpha_i)L] \tag{2.37}$$

$$G_{th} = \alpha_i + \frac{1}{2L}\ln(\frac{1}{R_1 R_2}) = \alpha_i + \alpha_m \tag{2.38}$$

G_{th} is the threshold gain. At this moment, the injected current density is called the threshold current density J_{th}. The optical confinement factor Γ should be introduced when we consider the interaction between charge carriers and the light. It is defined as the ratio of the integrated light intensity with the region of inversion population to the total optical intensity throughout the laser structure. Different transverse optical modes will have different overlap with the active region. Therefore, the optical gain in Eq. (2.38) corresponds to a certain mode and is known as the modal gain as opposed to the material gain. Specifically, the modal gain is a product of the Γ - factor of the given q_{th} mode and the material gain, g_{mat}:

$$G^q = \Gamma^q g_{mat} \tag{2.39}$$

2.3.3 Characteristics of Quantum Dot Lasers

For an individual self-organized QD, its electronic structure is very similar to the ideal case. There is a set of atomic-like quantum levels composed of several excited states and ground state. However, in contrast to the ideal array of identical QDs, self-organized islands differ greatly from each other in their size , shape, and other parameters affecting the energy of the quantum level. Namely, the quantum energy of real QD arrays is statistically determined rather than the zero-dimensional DOS of the individual QD. The DOS is maximum at the energy that corresponds

to the most probable QD size. In fact, the DOS of the array is characterized by a set of subbands that originates from inhomogeneously broadened quantum level of the GS and ES of individual QDs. Typically, the energy separation between ground state (GS) and excited state (ES) in QD is about 40~70 meV.

Compared to QW laser, the saturated gain, G_{sat}, of QD laser is much lower and proportional to the DOS at the maximum:

$$G_{sat} \propto \rho_{QD}^{max} \propto g_i \cdot n_{QD} / \Delta \tag{2.40}$$

where g_i is the level degeneracy (g=1 for the GS and ES is usually characterized by g_i >1), n_{QD} is surface density of QD and Δ is the energy width of the DOS. Real QD array will decrease G_{sat} due to inhomogeneous broadening. On the other hand, the saturated gain can be increased by means of several QD planes or denser QD arrays in each plane. However, the transparency current density which is also proportional to the total surface density of the QD array will be traded off. In a word, the competition between the transparency current density and the gain saturation determines the threshold current density at the given cavity loss.

In addition to the GS level, it was observed that one or more ES levels can be thermally populated to give an additional contribution to the threshold current density [41]. With higher degeneracy, these ES levels have higher saturated gain. Thus, the transition of the lasing emissions from the GS to the ES can be observed with increasing total loss. The situation is illustrated in Fig. 2.5, where the gain-current dependence is schematically shown for ideal as well as self-organized QD arrays. By the way, it has been shown that the experimental dependence of the optical modal gain on the threshold current density can be well fitted by the following empirical equation [42]:

$$G = G_{sat}[1 - \exp(-\gamma \frac{J - J_{tr}}{J_{tr}})] \tag{2.41}$$

where G_{sat} and J_{tr} are usual meaning of saturated gain and transparency current density, γ is an additional dimensionless gain parameter which can be treated as a non-ideality factor.
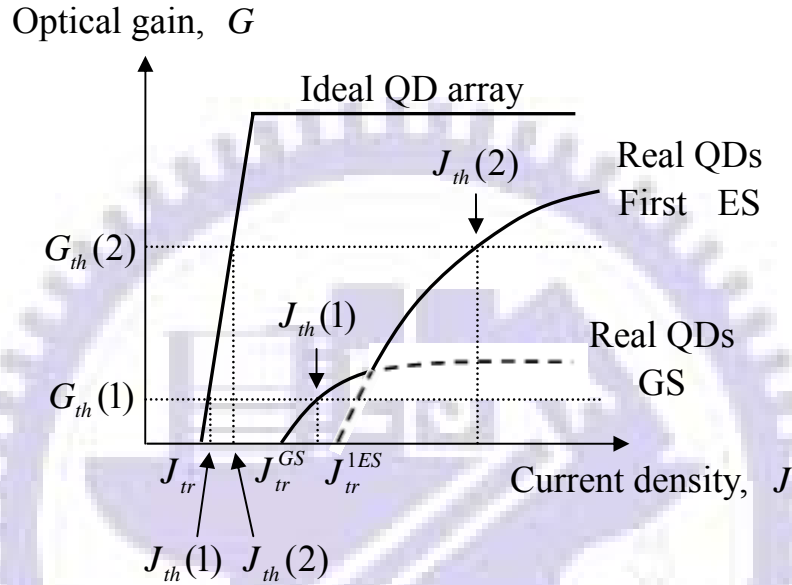

Fig. 2.5 Schematic dependence of the optical gain on the current density for the ideal and real (self-organized) QDs.

Chapter 3
Experimental Techniques

3.1 Coherence Length Measurement

Compared with measuring the spectrum of some light sources, the measurement of coherence length provides a more direct way to judge whether an emitter is suitable or not for OCT application. To achieve the goal, we have set up a fiber-based, delay-tunable Mach-Zehnder interferometer.

3.1.1 Experimental Setup

The automatic, delay-tunable interferometer is re-equipped from the commercial, manually path-tunable MZI-VAR 1300, which is used as the frequency clock in SS-OCT originally and is produced by Thorlabs. Fig. 3.1 shows the scheme of the whole system. Roughly speaking, the system is composed of three components, fiber-based Mach-Zehnder interferometer (MZI), computer-controlled translation stage and signal digitizer. They function as doing interference, providing path difference
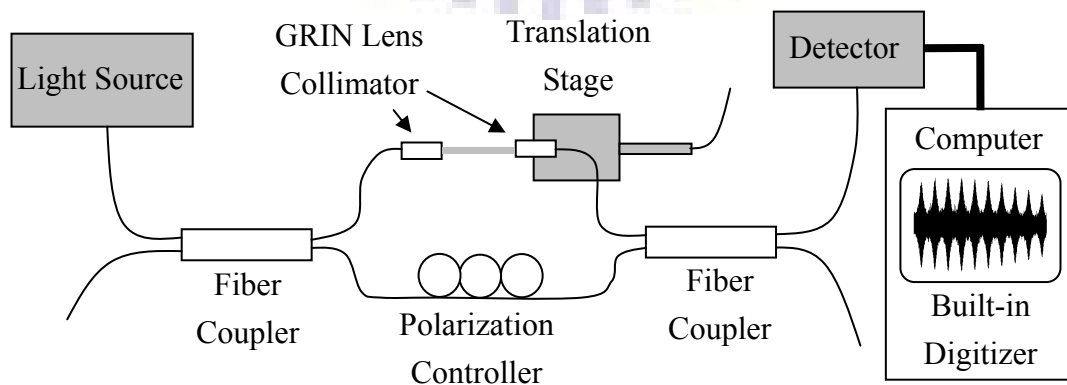

Fig.3.1 The scheme of the coherence length measurement system.

and demonstrating signal processing, respectively. Compared to free-space Michelson interferometer, the advantage of the fiber-based MZI is that it doesn't require aligning the light beams except for the face-to-face collimators.

In short, the MZI is constructed by two 50/50 couplers. A translation stage driven by a computer-controlled actuator is used to change the optical delay in one arm of the MZI. Fig. 3.2 shows the photo of the MZI. The polarization controller in the other arm of MZI can be used to optimize the polarization status in the fiber and maximize the interference fringe contrast in the detector output. One of the two output ports of the second 50/50 coupler is connected to a photodetector (PD). Then the interference signal from the PD will be sampled by a high-speed digitizer and the data can be saved.

The actuator, Z825, with a maximum traveling range of 25mm and a minimum resolution of 29 nm, is produced by Thorlabs. In other words, only light sources with coherence length shorter than 25 mm can be defined by this system. The high-speed digitizer, NI 5122, with a maximum sampling rate of 100M points per second, is a product of National Instrument. Narrow-shape interferogram can be obtained by means of setting appropriate traveling velocity and enough sampling rate.
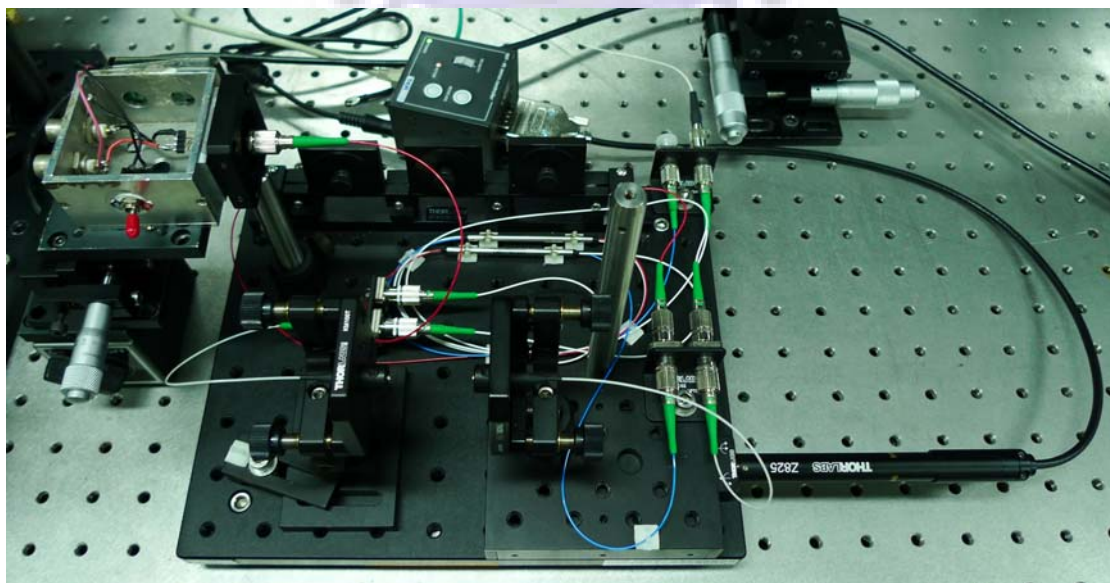
Fig. 3.2 Photo of the fiber-based, computer-controlled MZI.

Labview software is used to controlled the actuator and digitizer simultaneously and output the digital interferogram data. Fig. 3.3 shows the interface of the control panel.

Fig. 3.3 The interface of the Labview control panel.

Followings are some crucial issues that have to be concerned in this system. First, to define the coherence length correctly, the traveling range of the actuator must pass through the point of zero path difference. It can be proved by the characteristic of perfect symmetry of the

interferogram. Second, the face-to-face collimators must be aligned as good as possible to achieve nearly equal receiving power during translation. Finally, due to the sensitivity of interference, the whole system including all the fibers must rem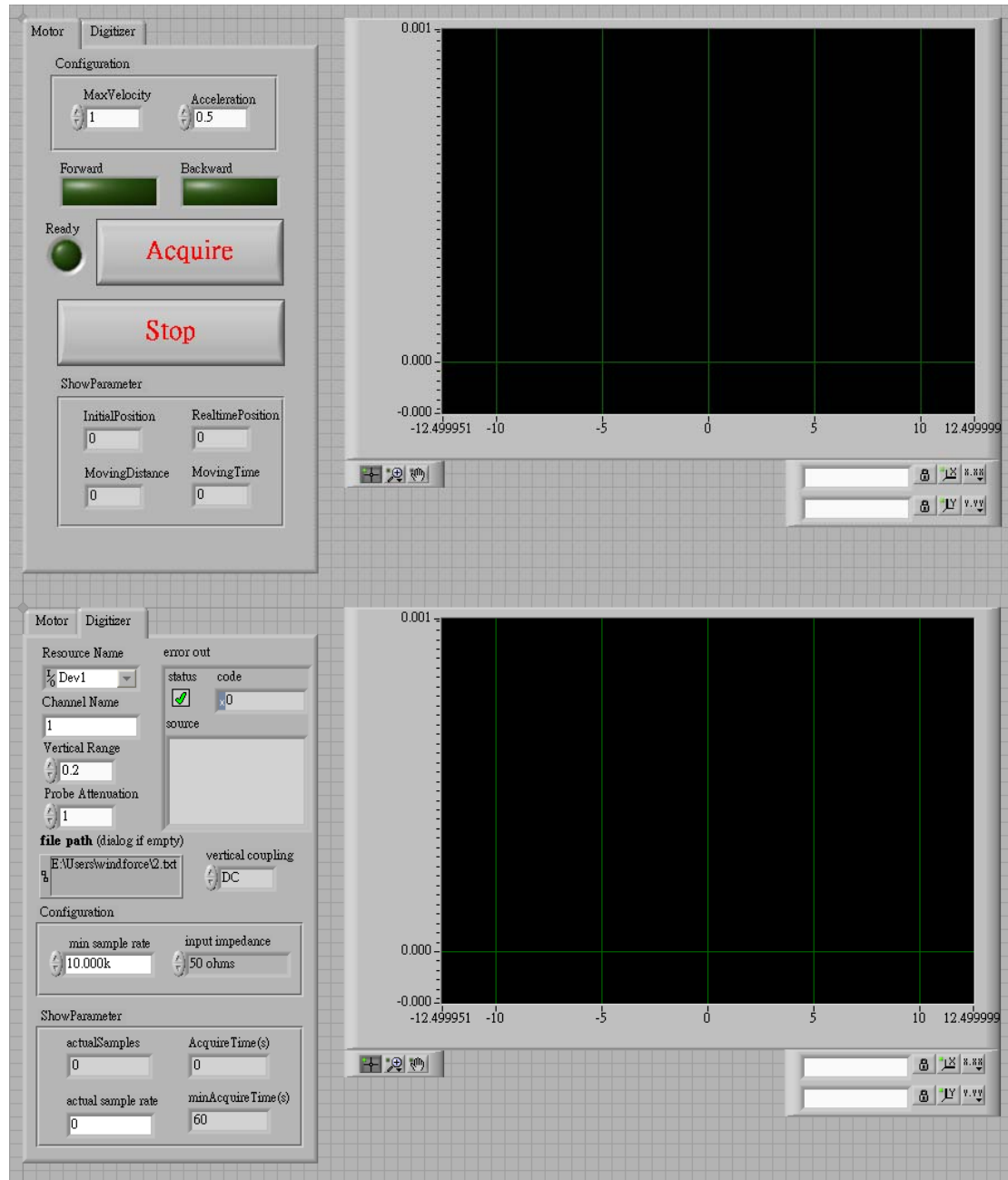ain stationary during the measurement. Any fluctuation will change the polarization state of the fiber output and further make an impact on the interferogram.

3.1.2 The Accuracy of Measurement

The Wiener-Khinchin theorem provides us a method to verify whether our measurement is accuracy enough or not. The interferogram and the power spectrum form a Fourier Transform pair. We measure the power spectra and interferograms of three commercial lasers. They are 1310 nm MQW-FP LD (multiple quantum well - Fabry-Perot laser diode), 1310 nm MQW-DFB (distributed feedback) LD and 1550 nm MQW-DFB LD and then will be abbreviated by LD#1, LD#2 and LD#3, respectively. The measurement of optical spectrum will be discussed later.

In this regard, an issue must be concerned before performing Inverse Discrete Fourier Transform (IDFT) on linear-scaled power spectrum we measured. According to sampling theorem, an analog signal that has been sampled can be perfectly reconstructed without aliasing from the samples only if the sampling rate exceeds two times of the highest frequency in the original signal. On the other hand, the sampling interval in the time domain is the reciprocal of the sampling range in the frequency domain; the sampling range in the time domain determines the reciprocal of the sampling interval in the frequency domain, and vice versa. In conclusion, to make sure the reconstructed data is without aliasing and is correct, some conditions when measuring the power spectrum must be considered,

such as enough sampling rate and sampling range. By the way, a more efficient algorithm, IFFT (Inverse Fast Fourier Transform), is used to compute the IDFT. More details about these concepts can be referred to textbooks of digital signal processing (DSP) [43].

Fig. 3.4~3.6 show the comparison of (a) the power spectrum in linear scale, (b) IFFT of power spectrum, (c) IFFT of power spectrum in the measurable area (d) envelope detection on IFFT of power spectrum, (e) the experimental interferogram and (f) its detail for the three different light sources. The FWHM of the main peak in the three power spectra (Fig. 3.4~3.6 (a)) are 0.022 nm, 0.012 nm and 0.050 nm, corresponding to theoretical coherence length (Fig. 3.4~3.6 (d)) as long as 64.30 mm, 124.69 mm and 26.82 mm, respectively. As expected, the narrower a spectrum of some light source is, the longer its coherence length will be. Obviously, due to the limitation of our optical spectrum analyzer (OSA), the power spectrum of LD#2 (Fig. 3.5 (a)) may not accurate enough and should be narrower in reality. In other words, its coherence length should be longer than the value above. Besides, the periodic behavior of the carrier wave in the interferogram will be the other evidence to confirm if what we measured is reasonable. The oscillation period of an interferogram directly depends on the central wavelength of a light source. It also can be observed from Fig. 3.4~3.6 (f). Though these coherence lengths longer than 25mm can not be defined experimentally with our interferometer, the accuracy of the measurement can be confirmed by the similarity between theory (Fig. 3.4~3.6 (c)) and our experiment (Fig. 3.4~3.6 (e)).

The interferograms we measured here are all obtained when these lasers are under continuous-wave (cw) mode operation. For most broadband lasers, including our CMQD LDs, relatively high current injection is necessary. However, severe thermal effect induced by highly

cw pumping will cause great damage to our devices which are unpackaged and without facet coating. Some differences between interferograms measured at cw and pulsed mode will be discussed later.

Fig. 3.4 (a)The power spectrum in linear scale, (b)IFFT of power spectrum, (c) IFFT of power spectrum in the measurable area (d)envelope detection on IFFT of power spectrum, (e)the experimental interferogram and (f)its detail for LD#1.

Fig. 3.5 (a)The power spectrum in linear scale, (b)IFFT of power spectrum, (c) IFFT of power spectrum in the measurable area (d)envelope detection on IFFT of power spectrum, (e)the experimental interferogram and (f)its detail for LD#2.
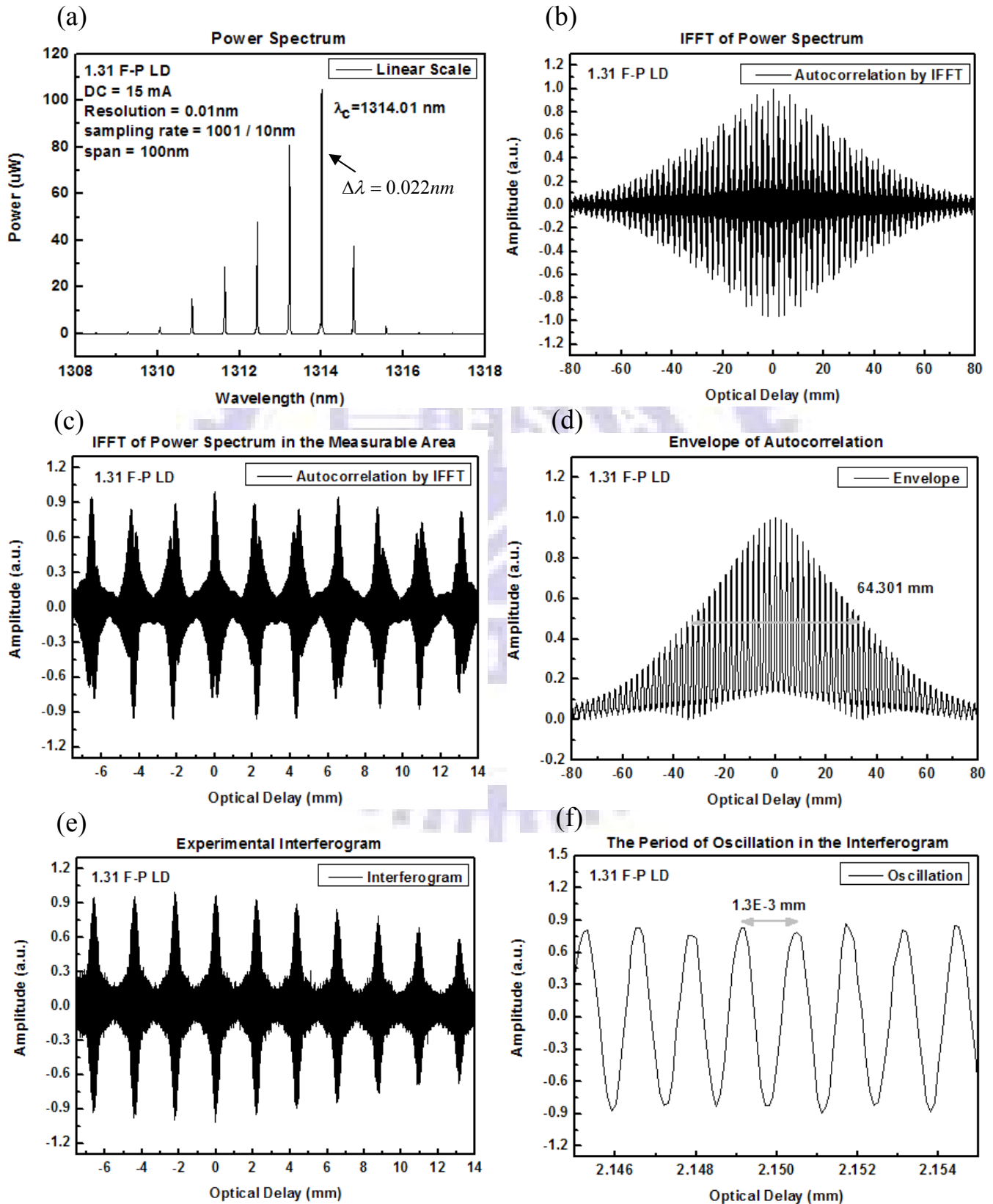
Fig. 3.6 (a)The power spectrum in linear scale, (b)IFFT of power spectrum, (c) IFFT of power spectrum in the measurable area (d)envelope detection on IFFT of power spectrum, (e)the experimental interferogram and (f)its detail for LD#3.
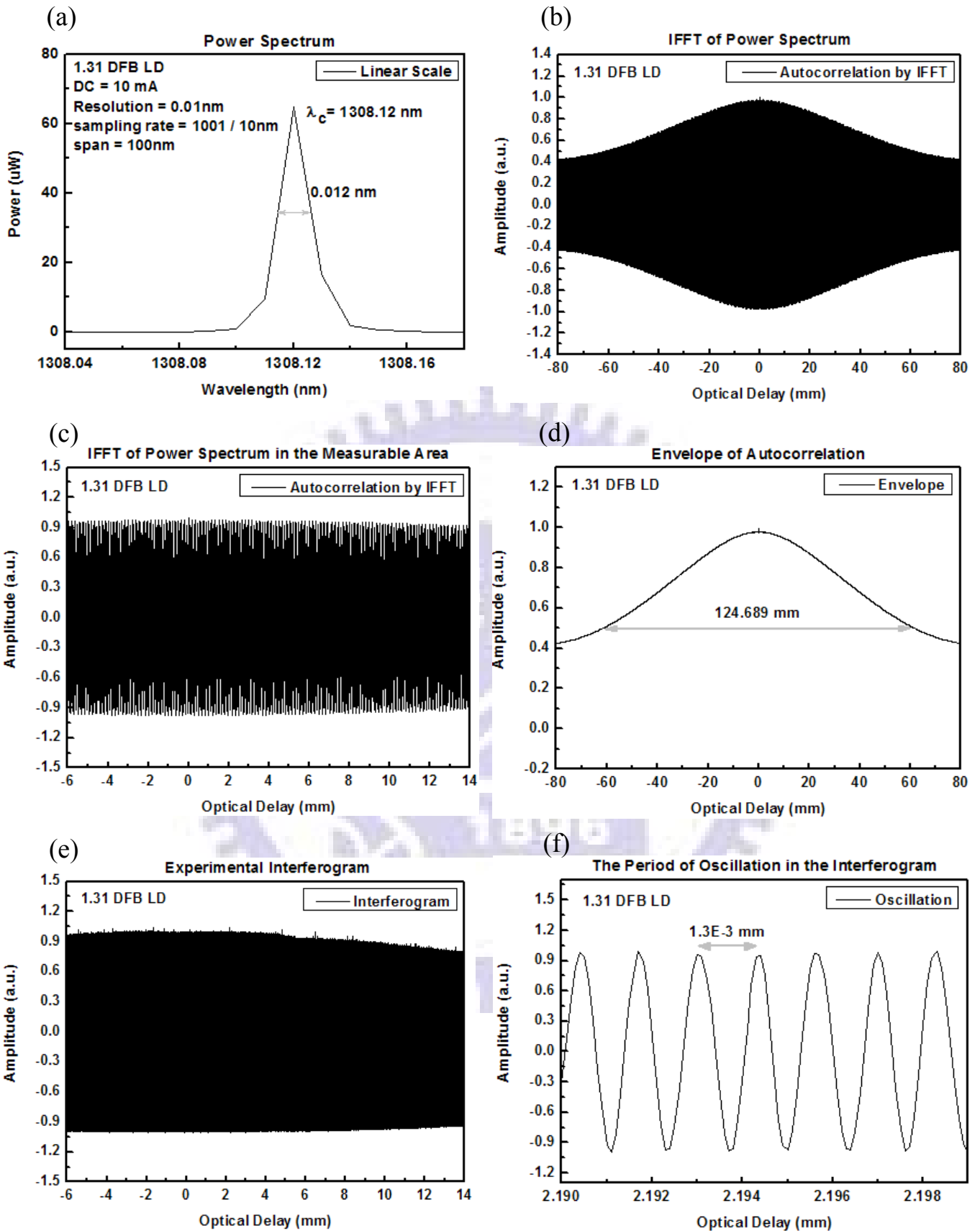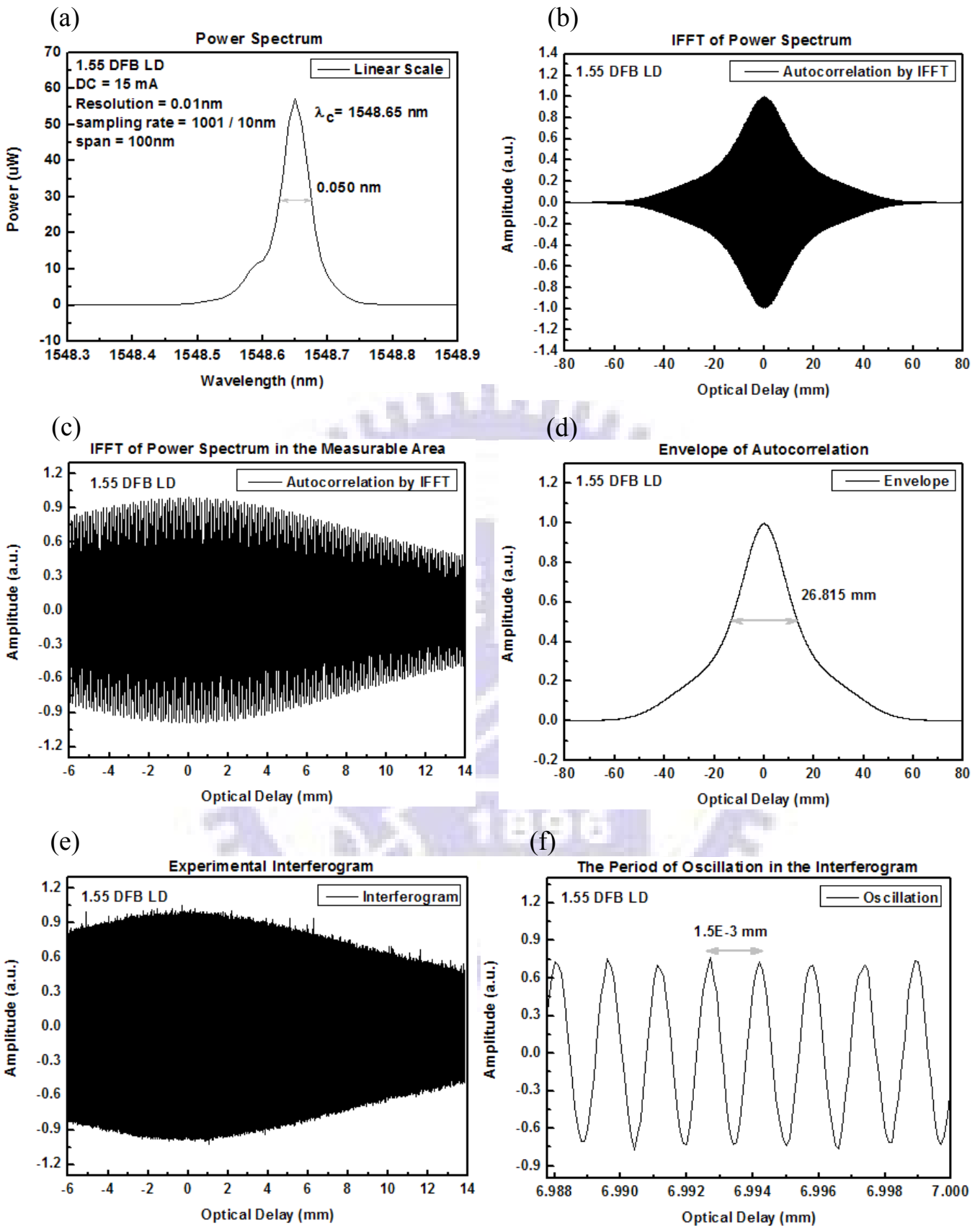
3.2 Characteristics of Laser Diode

3.2.1 Light - Current - Voltage (L-I-V) Characteristic

L-I-V characteristic is the most fundamental characteristic of a LD. The threshold current (I_{th}), slope efficiency (η), turn-on voltage (V_0) and series resistance (R_s) of a LD can be immediately determined from a measured L-I-V curve. More parameters, such as internal loss (α_i), model gain (G),...etc, can be obtained by analyzing these basic parameters from devices of different cavity length. Fig. 3.7 shows the schematic diagram for the measurement of L-I-V characteristics.

In our L-I-V measurement, laser device is put on a copper stage which is equiped with a TE-cooler to stabilize the temperature of our device. Keithley 2520 pulsed laser diode test system is used for current injection and photocurrent detection. The light output is detected by a Ge detector and eventually will be calibrated mathematically by a well calibrated power meter. In the meanwhile, electrical information will be feedbacked to Keithley when current injection begins. With GPIB-interfaced connection, the whole measurement can be controlled by the computer.
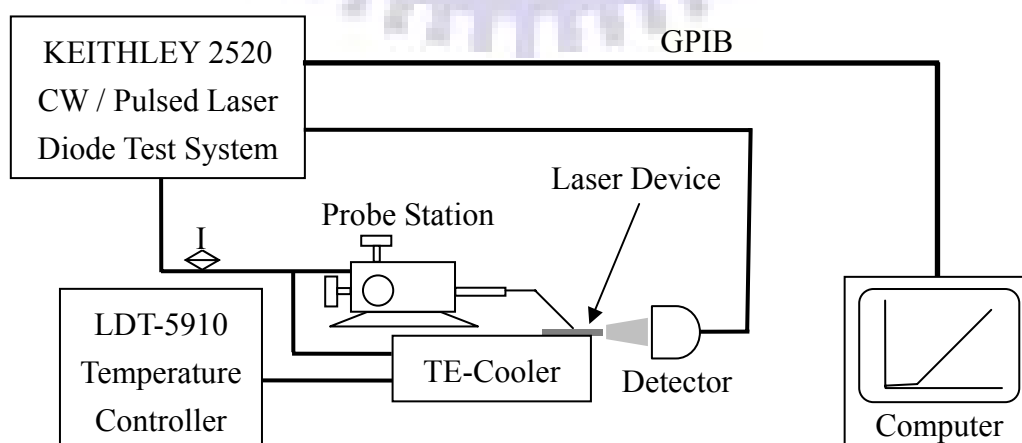
Fig. 3.7 The schematic diagram for the measurement of L-I-V characteristic.

3.2.2 Lasing Spectrum

The same probe system and temperature controller are used. Laser emission is coupled into a single-mode (SM) fiber and then transfered to ANDO AQ-6315E, the optical spectrum analyzer (OSA) with a minimum resolution of 0.05nm. To overcome insufficient coupling efficiency, a lens module composed of an aspheric lens and a well-coated collimator is used. All spectums we measured from our CMQD laser are with resolution of 0.1 nm. Fig. 3.8 illustrate the setup for the measurement of lasing spectrum. With GPIB interface between OSA and computer, measurements can be achieved by program.
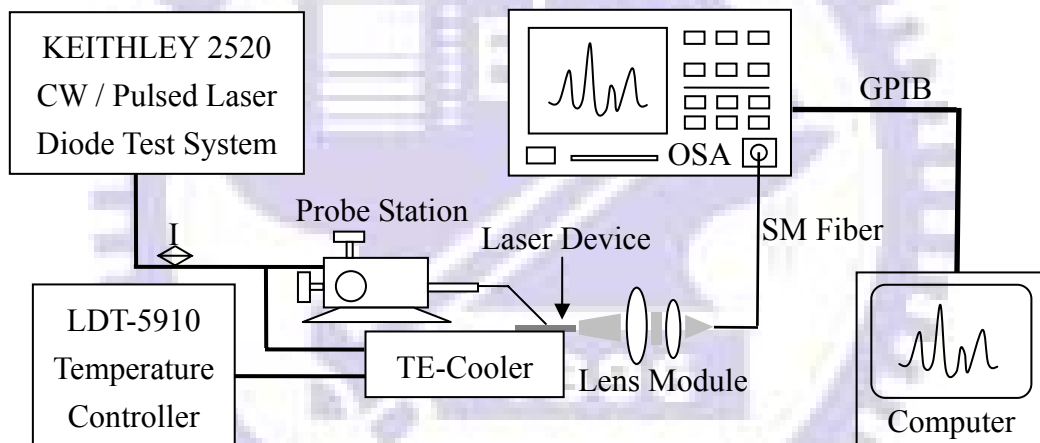
Fig. 3.8 The setup for the measurement of lasing spectrum.

3.2.3 Far-Field Pattern

Nowadays, Semiconductor lasers play an more and more important role in the field of fiber-optic communication. To improve the coupling efficiency into the single-mode fiber of some light source, a circle shape and narrow beam divergence of the far-field pattern (FFP) is demanded. Fig. 3.9 shows the experimental setup used to perform the FFP measurement. The same probe system and temperature controller are used.
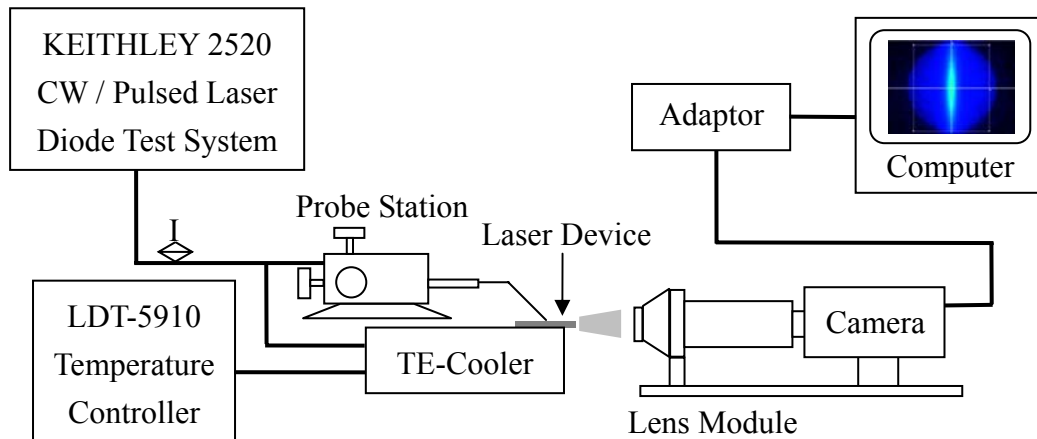
Fig. 3.9 The setup for the measurement of FFP.

The emitting ligth is focused on the Hamamatsu IR CCD camera (C5840) through the Hamamatsu FFP lens module (A3267-12). Combined with a frame grabber card built in the computer, the signal received by camera can be visulized and analyzed by computer. To prevent the gain saturation of CCD, some attenuators will be used in the high-power measurement case. After appropriate calibration for corresponding wavelength of the light source, the cross-sectional (vertical and lateral) beam divergence angle can be determined conveniently.

Chapter 4
Chirped-Multilayer Quantum Dot Lasers

4.1 Introduction

Due to the inhomogeneity in shapes, sizes and composition, self-assembled QDs is subjected to lower saturated optical gain. Stacking multiple QD layers of the same growth condition (uniform-stacked) has been proposed to increase the optical gain for well-performed QD laser in the 1.3 µm region [44]. In other hand, the intrinsic characteristic of broad gain spectrum in QDs, if properly engineered, are promising for low coherence application such as OCT.

Operating at amplified spontaneous emission (ASE) and suppressing stimulated emission, SLD has been one of the candidates for low-coherence application. However, its lower output power may limit the performance on real-time imaging of OCT. Furthermore, the tilted ridge waveguide (RW) configuration for low mirror reflectivity complicates the fiber coupling and increase the package cost. Recently, it was announced that QD lasers, in normal RW configuration, can be managed to lase with a wide emission spectrum [38~40].

In this work, we propose the control of the emission wavelength in the chirped structure by changing the matrix surrounding of the QDs. Specifically, when the InAs QDs are covered by an InGaAs strain-reducing layer (SRL), a red-shift of the emission wavelength is observed, depending on the composition and thickness of the SRL [20]. The areal density is not significantly affected by the capping, so that the available gain and the wavelength are effectively decoupled. In contrast to other approaches, this technique is reproducible and easy to implement,

since it relies on well-controlled growth parameters.

We have demonstrated 10-layer QD laser with three chirped-wavelength QD-stacks, which we called chirped-multilayer quantum dot laser diode, CMQD LD, once and for all. Some basic parameters of the CMQD LD will be measured and discussed. Empirical gain-current analysis is also performed. The measurement of interferograms will be demonstrated by our delay-tunable Mach-Zehnder interferometer to exhibit how broad a spectrum is in a more different way.

4.2   Device Growth and Fabrication

The CMQD laser structure was based on a typical p-i-n configuration grown on a silicon-doped, (100)-oriented n^+-GaAs by the molecular beam epitaxy. Multilayer QD active region with undoped graded-index separate-confinement heterostructure (GRINSCH) of 0.5μm was sandwiched between Si-doped and C-doped $Al_{0.35}Ga_{0.65}As$ cladding layer of 1.5 μm, and followed by heavily C-doped GaAs contact layer of 0.4 μm. The emission wavelength of InAs QDs are tuning by the subsequent $In_{0.15}Ga_{0.85}As$ capping layer of different thickness. Multilayer QDs are spaced by GaAs and centered in the active region also by GaAs. The spacing thickness of 33 nm is chosen so that strain is not accumulated in the multilayer deposition. The wafer growth is credited to the Innolume GmbH in Germany.

To chirp the emission wavelengths of QD active region, three wavelengths designated as QD_L, QD_M and QD_S (stand for longer-, medium- and shorter-wavelength QD stacks, respectively) were engineered in the laser structure, which corresponding to the InAs QDs of 2.6 ML capped by InGaAs of 4 nm, 3 nm and 2.5 nm, respectively. The

stacking numbers for QD_L, QD_M and QD_S were 3, 4 and 3 layers, respectively. The stacking sequence of different capping thickness was interlaced. Fig. 4.1 shows the schematic diagram of chirped-multilayer QD structure.

Ridge waveguide of 3μm width was formed by high-density-plasma dry etching. The etching depth was *in situ* monitored to stop just above GRINSCH waveguide. Thin oxide was then deposited by plasma-enhanced chemical-vapor deposition. The contact window opening over the narrow ridge was done by double-channel self-aligned process. After p-metallization by Ti/Pt/Au deposition, the substrate was thin down to around 100 μm, and n-type metal of AuGe/Ni/Au was deposited afterwards. As-cleaved and uncoated laser bars with cavity lengths from 0.5 mm to 5 mm were fabricated then evaluated by standard light-current-voltage (*L-I-V*) and spectrum measurement. Both pulsed and continuous-wave driving conditions are performed under varied heatsink temperature.
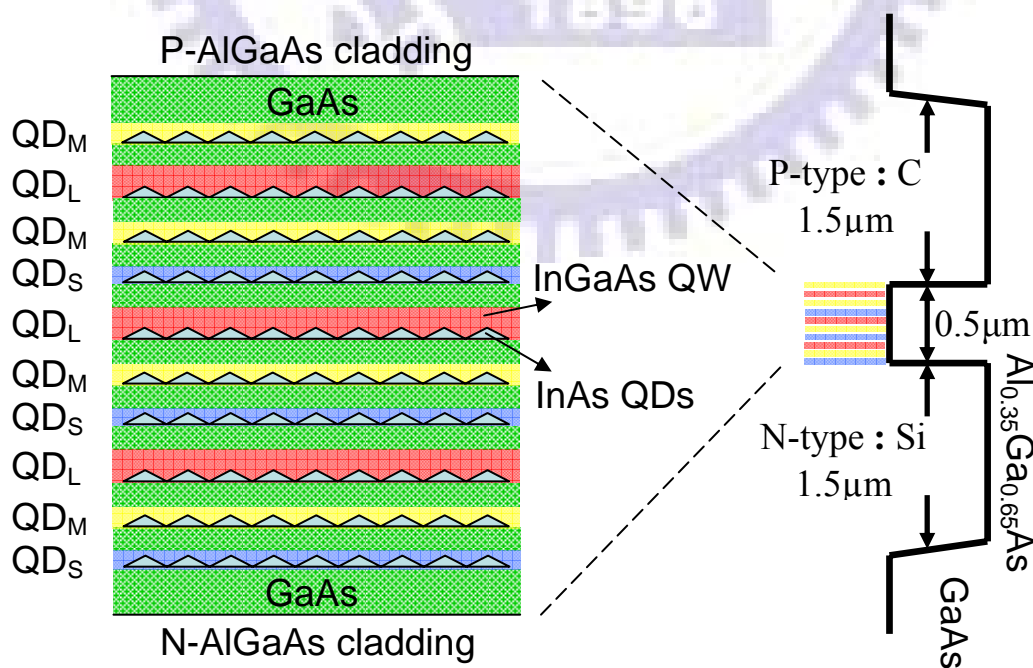

Fig. 4.1 The schematic diagram of the chirped multilayer QD structure.

4.3   Results and Discussion

The areal density of InAs QDs without InGaAs capping was grown separately and characterized by AFM to be around $5*10^{10}$ cm^{-2}. Fig. 4.2 shows the AFM image of epitaxial surface immediately following the QD deposition. According to the room-temperature (RT) photoluminescence (PL), the dependence of QD emission wavelength on the thickness of capping InGaAs layer can be determined. Fig. 4.3 illustrates the dependence of GS and ES peaks at RT PL on the thickness of In$_{0.15}$Ga$_{0.85}$As capping layer. The peak wavelength of GS for QD$_L$, QD$_M$ and QD$_S$ in our case is about 1262 nm, 1230 nm and 1215 nm, respectively. The peak wavelength of first ES for QD$_L$, QD$_M$ and QD$_S$ is also estimated to be around 1183 nm, 1155 nm and 1145 nm, respectively. Since the available gain and wavelength are decoupled in the chirped structure [20], stacking CMQD in which each QD layer is capped with different thickness of InGaAs SRL could effectively increase available
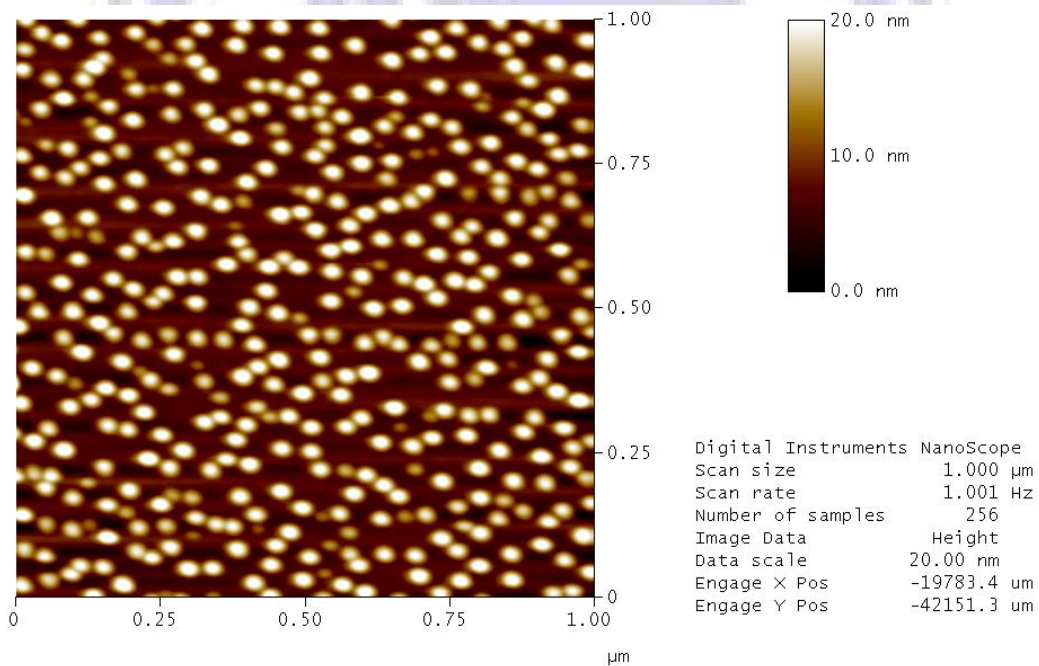

Fig. 4.2 The AFM image of epitaxial surface immediately following the QD deposition.
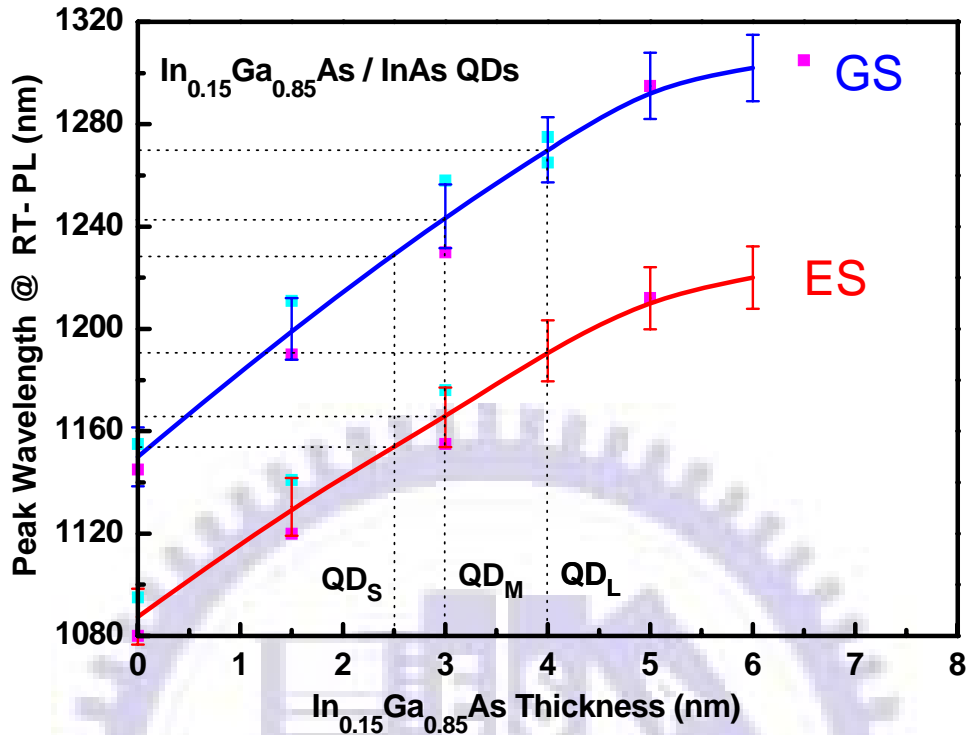
gain and spectral width.

Fig. 4.3 The dependence of GS and ES peaks at RT PL on the thickness of $In_{0.15}Ga_{0.85}As$ capping layer.

4.3.1 Laser Characteristics

Fig. 4.4 shows the RT pulsed L-I-V characteristics of CMQD LD with a narrow RW of 3 μm and different cavity lengths. Fig. 4.5 shows the lasing spectra around threshold relevant to different cavity lengths. Longer lasing wavelength around 1265 nm was achieved for cavity length above 0.75 mm. Only the 0.5 mm cavity length was found lasing at 1173nm. Compared it to the results of RT PL, it was expected that these two wavelength emissions was contributed by the GS and ES of QD_L. For the cavity length of 5 mm, the threshold current is 34 mA, which corresponds to a threshold current density (J_{th}) of 226.7 A/cm^2. By fitting the relationship of inverse external slope efficiency $1/\eta_{ex}$ versus cavity length L to the equation $1/\eta_{ex} = 1/\eta_i[1 - \alpha_i L/\ln(R)]$ with R (reflectivity
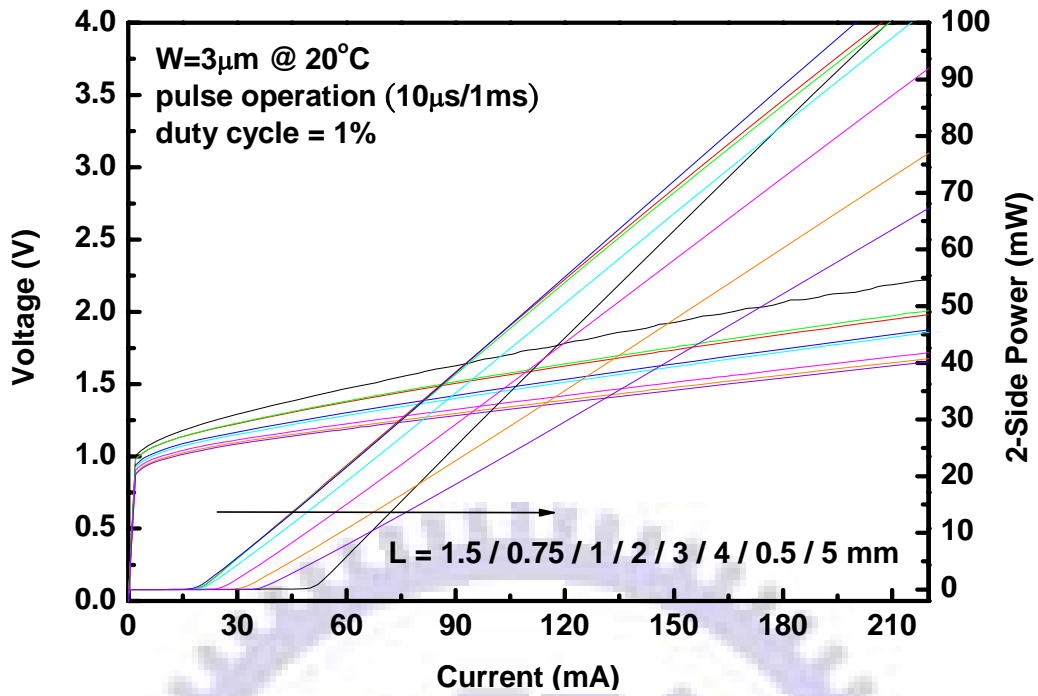
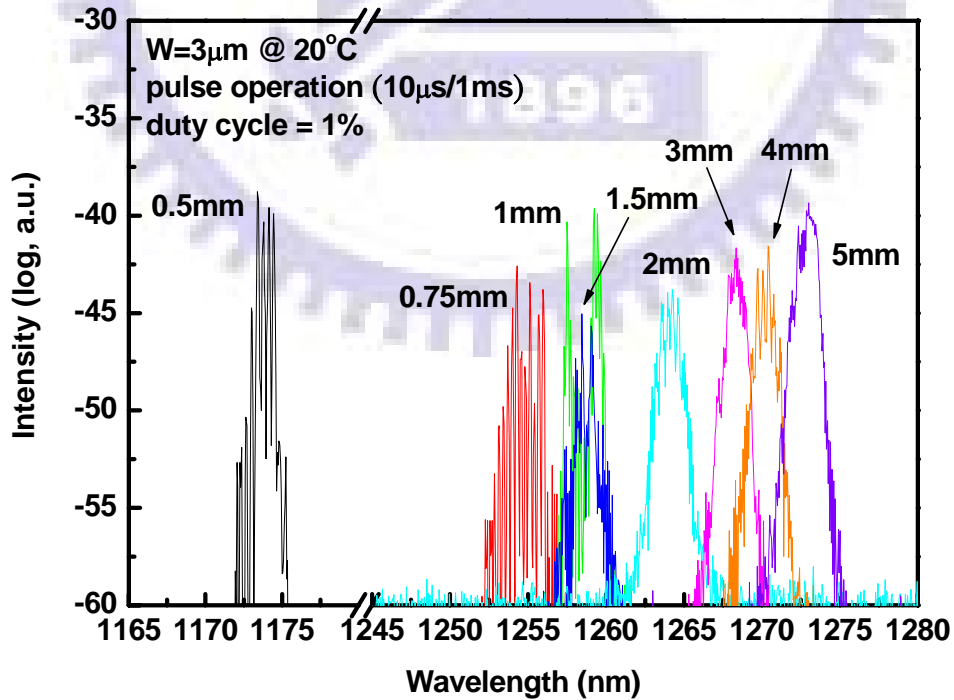Fig. 4.4 The RT L-I-V characteristics of our CMQD LD for different cavity lengths.

Fig. 4.5 The RT lasing spectra of CMQD LD operated around threshold for different cavity lengths.

at facet) = 0.32, a η_i of 88.3% and an α_i of 3.0 cm^{-1} are obtained, as shown in Fig. 4.6.
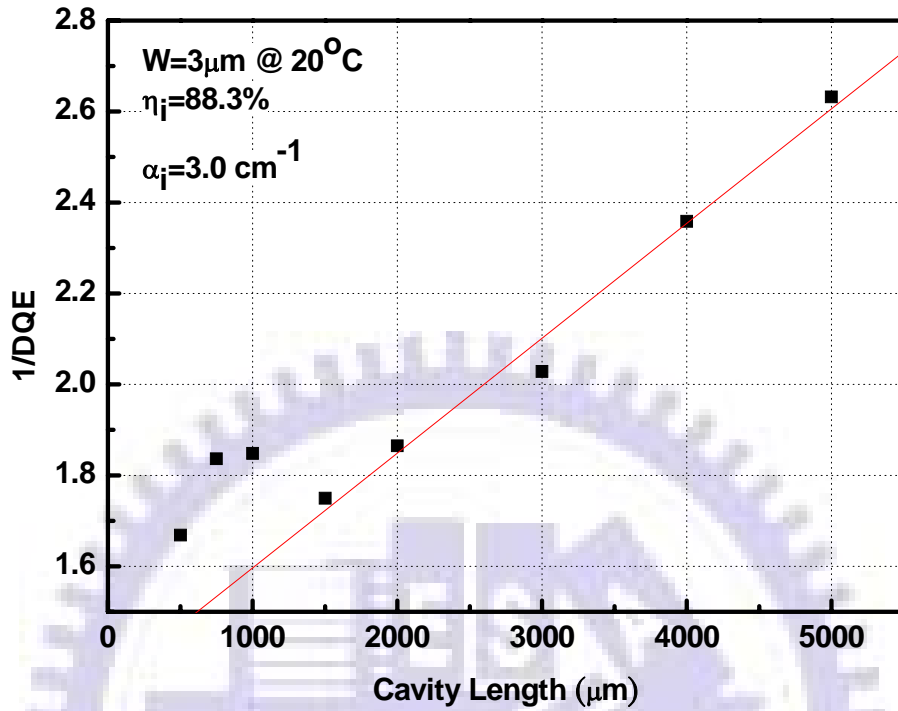
Fig. 4.6 Inverse of external differential efficiency plotted as a function of cavity length of CMQD LD.

4.3.2 Gain-Current Analysis

The dependence of the modal gain, G, on current density, J is one of the main characteristics of the active region in a QD laser. Due to the non-ideality such as inhomogeneous broadening of the self-assembled QD, its gain-current characteristic demonstrates higher transparency current density, lower saturated gain, and less abrupt increase of the gain on increasing the current density. After determining the current dependence of threshold modal gain, we fitted the gain curve based on the empirical equation proposed by Zhukov *et al*. [42], i.e. Eq. (2.41). The experimental data points and fitting curves are shown in Fig. 4.7. The lasing wavelengths at each threshold condition were also shown here.

Gain-Current Analysis

$$G=G^{sat}[1-exp(-\gamma(J-J_{tr})/J_{tr})]$$

GS:
$G^{sat}=20.9$ cm^{-1}
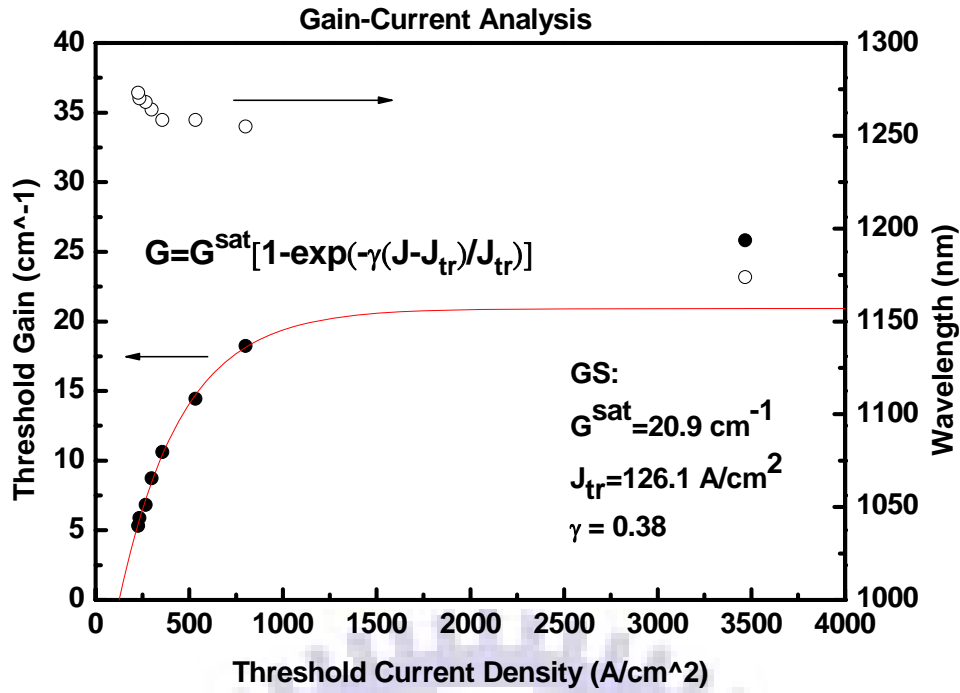$J_{tr}=126.1$ A/cm^2
$\gamma = 0.38$

Fig. 4.7 Modal gain and lasing wavelength as functions of current densities for CMQD LD.

Since the lasing wavelength significantly switched to higher energy at cavity length of 0.5mm, the others could be viewed as coming from the GS. If the GS saturated gain of 20.9 cm^{-1} is from 3*QD$_L$, the GS saturated gain per QD is about 7 cm^{-1}. Compared to the typical value of 4 ~ 6 cm^{-1}, this value is unreasonably high. Furthermore, the fitting transparency current density is 126.1 A/ cm^2 and the non-ideality parameter γ is equal to 0.38. Due to the trade-off between saturated gain and transparency current density discussed before, the relatively higher GS saturated gain and higher transparency current density manifest the fact that the total dot density is high in our CMQD structure. On the other hand, the relatively low γ-factor and the less abrupt increase of optical gain with increasing the current density could be attributed to the simultaneous population of the higher-energy states. The contribution of the higher-energy state such as the GS of QD$_M$ can not be ignored. In other words, instead of coming from single quantized state, the lasing peak results from the total effect of simultaneous multi-states pumping. It is reasonable that this behavior occurs in our specially designed CMQD structure.

4.3.3 Far-Field Pattern

To obtain a high power coupling, not only the high output power but also narrow beam divergence is required. To reveal the superior performance on power issue than that of SLD, the divergence angle of a broadband laser is also an important parameter in the fiber-based OCT application. Fig. 4.8 shows the measured far-field patterns with increasing current density of our CMQD LD with cavity length of 2mm.

Since the divergence angle does not significantly depends on the cavity length of a device, only the 2mm one is measured. This result shows that both the lateral and vertical divergence angle almost remain the same when current density increases to $10*I_{th}$. The vertical far-field angle $(\theta_{\perp})$ is $52.0°$ and the lateral far-field angle $(\theta_{//})$ is $7.8°$. The aspect ratio, defined as $\theta_{\perp}/\theta_{//}$, is 6.8. Without appropriate engineering of cladding layer structure, the FFP performance of CMQD LD is not good enough when compared to well-engineered QW laser which the optical coupling efficiency higher than 60% can be obtained. Only coupling efficiency of 10%~20% can be achieved in our case when measuring the interferograms. All parameters are listed in Table 4.1.

Table 4.1 All parameters of FFP for the 3μm-wide ridge and 2mm-long CMQD LD with increasing current density.

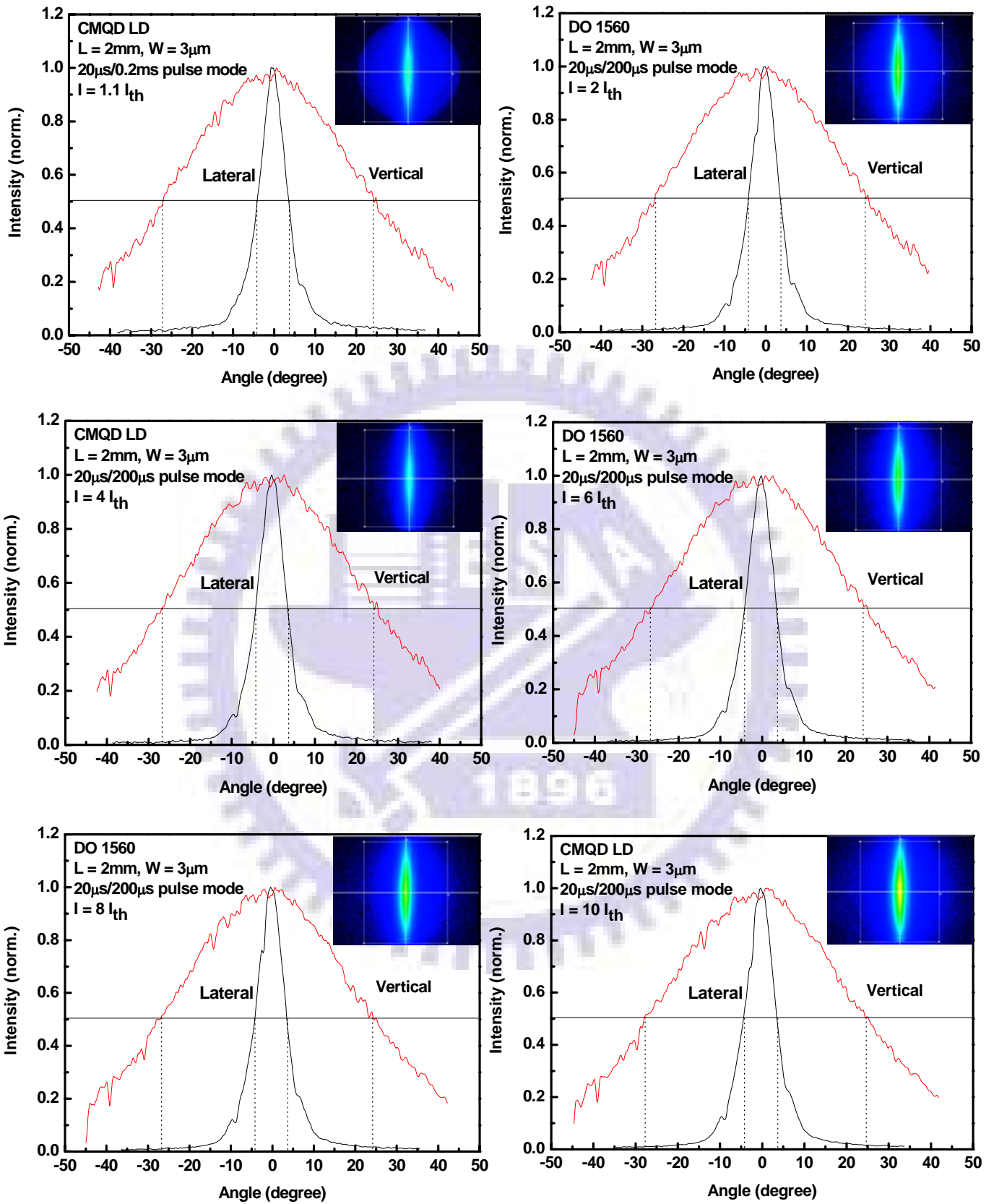| FFP \ I	1.1 I_{th}	2 I_{th}	4 I_{th}	6 I_{th}	8 I_{th}	10 I_{th}
Lateral Angle (degree)	7.8	7.8	7.6	7.6	7.6	7.8
Vertical Angle (degree)	52.0	52.0	52.2	51.8	53	53.2
Aspect Ratio	6.7	6.7	6.9	6.8	7.0	6.8

Fig. 4.8 The measured far-field patterns for the 3μm-wide ridge and 2mm-long CMQD LD with increasing current density.

4.3.4 Temperature Characteristics

Due to the non-radiative recombination rate is a function of temperature, more current is required both for threshold and the increment above threshold as the temperature increased. Fig. 4.9 shows the temperature-dependent L-I characteristics. The device under test was 3 μm in ridge width and 2 mm in cavity length. The temperature changes from 283K to 353K with an interval of 10K. The relation of the characteristic temperature and the threshold current is expressed as $I_{th} = I_0 \exp[T/T_0]$, where T_0 is called characteristic temperature. It represents how many excited electrons and holes by lattice heating contributed to the radiative recombination. Fig. 4.10 shows the threshold current versus temperature and the fitting curve. The extracted T_0 is as low as 82.4K (283K~353K). For broad-spectrum QD laser, many characteristics differ from conventional narrow-spectrum laser. To broaden the spectral width, a deliberate increase in the dot size
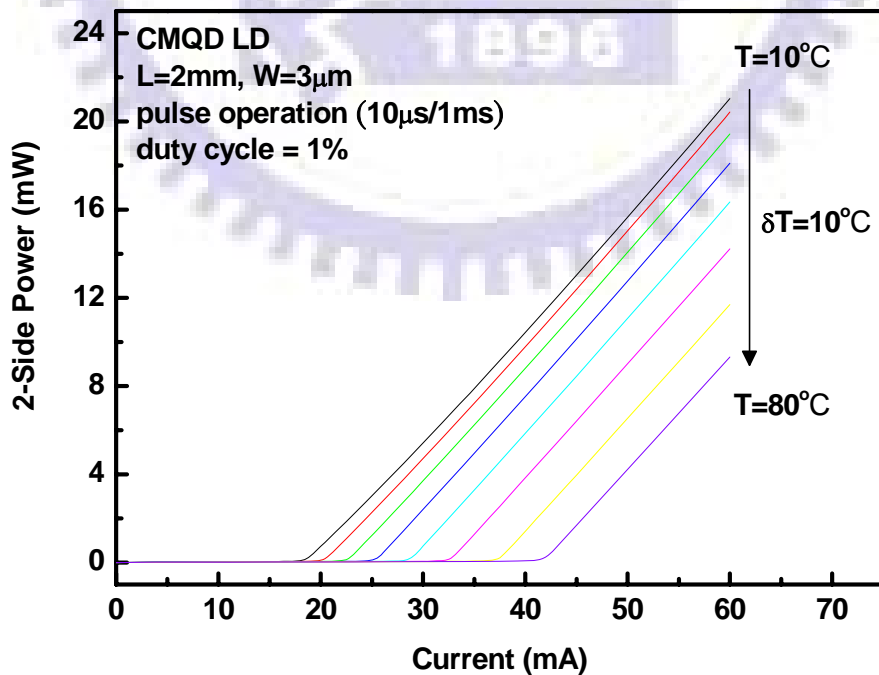

Fig. 4.9 The temperature-dependent L-I characteristics of CMQD LD with 3μm ridge width and 2mm cavity length.
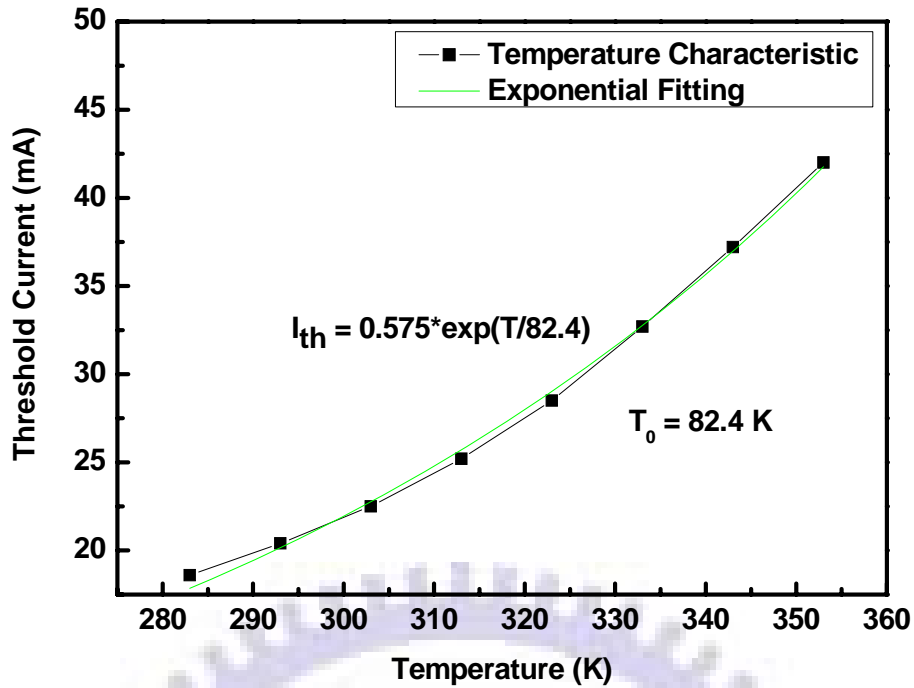
Fig. 4.10 The threshold current versus temperature and the fitting curve.

distribution is necessary. However, due to the Gaussian-like DOS (not delta-function any more), there are trade-offs in threshold current density and characteristic temperature. In other words, the relatively low T_0 obtained in our CMQD structure is not a surprising result. H. S. Djie reported a low T_0 of 40.3K in the range of 278K ~ 323K for the broadband InGaAs/GaAs QD LD with cavity length of 800 μm [40].

4.3.5 Spectral Characteristics

The main issue in this thesis focuses on whether our CMQD LD could exhibit broad spectral width and centered near 1.3 μm to meet the demand of low-coherence applications. The RT lasing spectrum with varying injection levels and cavity lengths for CMQD LD with 3 μm ridge width are shown in Fig. 4.11.

It is obvious that the spectral ripple is severe for short-cavity device in low injection current. This phenomenon can be attributed to the longitudinal mode existed in a Fabry-Perot cavity. The longitudinal mode
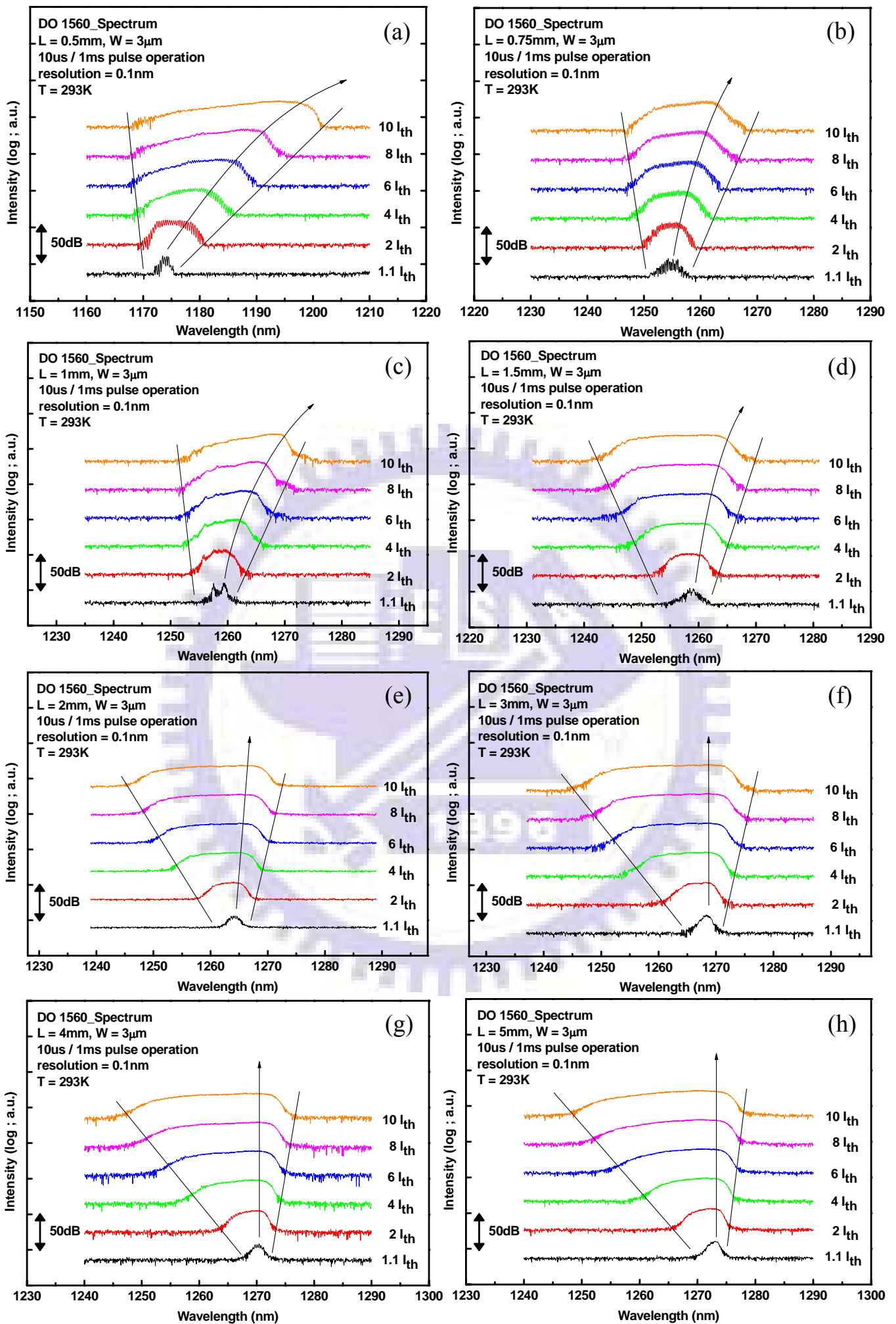
Fig. 4.11(a)~(h) The RT lasing spectrum operating from lasing threshold to well-above threshold current for CMQD LD with 3μm ridge width and different cavity lengths.

separation measured in the output spectrum can be expressed by $\Delta\lambda \approx \lambda^2/2nL$, where n and L are the group effective index of active region and the cavity length, respectively. The longer the cavity length is, the closer the longitudinal mode separation will be. In other words, the longitudinal mode spacing cannot be specifically defined for devices with longer cavity length. In our case, the longitudinal mode spacing can only be defined as 0.37 nm, 0.28 nm and 0.21 nm for devices with L of 0.5 μm, 0.75 μm and 1 μm, respectively. The corresponding group effective index of 3.73 is obtained. It is believed to be a rational value in our InAs/InGaAs active region. In fact, whether the longitudinal mode is clear or not strongly depends on the resolution, an adjustable parameter when measuring power spectrum with OSA. However, due to the Fourier-transformation relation between power spectrum and interferogram, it is the narrow peak and random-like behavior of longitudinal mode in spectrum that severely affects the profile of interferogram. That is why the resolution must be mentioned when the spectral width of a broadband laser is quantitatively determined.

Table 4.2 lists the corresponding peak wavelength and FWHM as increasing the injection level for these devices. Fig. 4.11 shows the plot of peak wavelength versus current injection level for each device. The broadest spectrum equals to 14.2 nm occurs in the 3-mm LD at $10*I_{th}$. As stated before, the lasing wavelength is expected to be coming from the GS of QD_L for all devices except for the one with cavity length of 0.5 mm. Around the threshold current, a slight blue-shift occurs when cavity length decreases. It could be attributed to the moving of maximum gain spectrum curve towards higher photon energies as the injection current increases below the lasing threshold current, which is proposed by Maximov *et al* [45]. Due to the mirror loss is inversely proportional to the cavity length, the threshold current density of short-cavity device is

Table 4.2 The list of corresponding peak wavelength and FWHM as increasing injection levels for all devices.

L \ I/I_{th}		1.1	2	4	6	8	10
0.5mm	λ_p (nm)	1173.4	1173.9	1179.2	1183.9	1187.7	1193.8
	$\Delta\lambda$ (nm)	1.4	6.4	6.2	9.1	5.9	8.7
0.75 mm	λ_p (nm)	1254.3	1255.7	1256.1	1257.9	1259.7	1261
	$\Delta\lambda$ (nm)	2.2	3.7	4.3	5.1	5.3	5.3
1mm	λ_p (nm)	1259.3	1259.5	1261.3	1262.3	1265.3	1268.3
	$\Delta\lambda$ (nm)	2.2	2.9	4.9	4.3	4.0	4.3
1.5mm	λ_p (nm)	1259.1	1257.8	1257.1	1260.6	1260.6	1260.7
	$\Delta\lambda$ (nm)	1.2	4.7	8.1	9.8	11.6	12.4
2mm	λ_p (nm)	1264.3	1264	1264.8	1265.1	1264.9	1265.2
	$\Delta\lambda$ (nm)	1.5	3.9	8.4	10.2	12.5	12.8
3mm	λ_p (nm)	1268.3	1267.9	1268.2	1268.4	1268.3	1268.5
	$\Delta\lambda$ (nm)	1.1	4.7	8.8	12.6	13.7	14.2
4mm	λ_p (nm)	1270.4	1270.4	1269.3	1270.2	1270.1	1267.9
	$\Delta\lambda$ (nm)	1.2	3.9	6.5	9.3	12.3	14.0
5mm	λ_p (nm)	1273	1272.1	1271.7	1270.2	1270.6	1270.1
	$\Delta\lambda$ (nm)	1.4	3.8	6.8	9.0	10.5	11.5

higher than that of long-cavity one. As a result, the degree of blue-shift for short-cavity diode laser will be much more apparent. This is consistent with our data.

As shown in Fig. 4.12, ES of QD_L emitted by device with 0.5-mm-length was red-shifted severely after the threshold current due to thermal effect which is caused by high injection current density. However, this red-shift is compensated by the blue-shift caused by smaller dots in
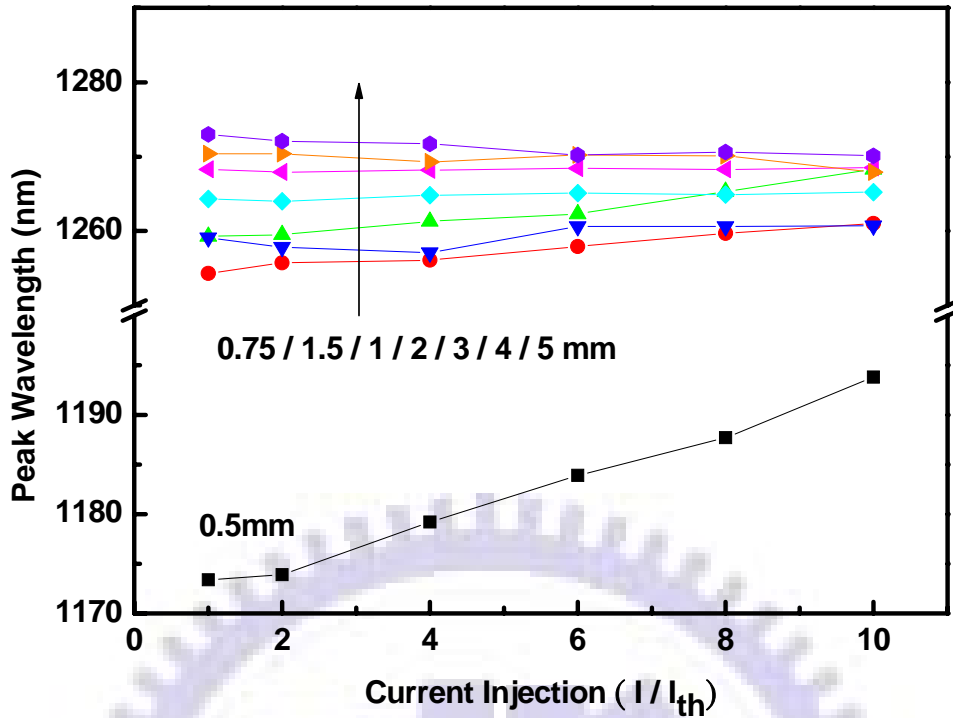
Fig. 4.12 The plot of peak wavelength versus current injection level for each device.

the devices with cavity length of 0.75 mm, 1 mm and 1.5 mm, and furthermore the blue-shift becomes dominant for longer devices. For our unpackaged and uncoated devices, the temperature-controllable heat sink plays an important role to prevent severe thermal effect. With larger contact area with the heat sink, thermal effect of long-cavity devices can be effectively suppressed.

A progressive broad bandwidth in the lasing spectrum is noticed with increased injection current because of the inhomogeneous broadening. Larger dots with lower energy would be filled at first as increasing current injection. A blue-shift in gain spectrum caused by filled smaller dots with higher energy occurred at high pumping. However, the spectral width is not as broad as expected due to non-uniform enhancement of gain spectrum as increasing pumping. Furthermore, the effect of $4*QD_M$ and $3*QD_S$ in the structure of CMQD are not apparent from our measurement at injection level up to ten times of threshold

current. It means that the carrier population cannot be well-distributed and results in a non-equal contribution of threshold modal gain. On the other hand, Fig. 4.13 shows the measured emission spectrum at much higher injection level under pulse operation from a 3-mm-long device of CMQD LD. Table 4.3 lists the spectral dependence on current injection. The spectral FWHM decreased at current level from 1.5 A to 2.3 A is due to the dip at 1270 nm. Simultaneous lasing from GS of QD_L and a higher state occurred wherein incomplete gain clamping and retarded carrier relaxation process are the main attribution [35]. It is believed that this higher state was contributed by both the ES of QD_L and GS of QD_M. Besides, an extremely broad spectrum of 29 nm centered at 1270 nm was observed. It is worth noting that these measurements are all under a fine resolution of 0.1 nm. However, the energy spacing between GS and ES is too large (> 60 meV for S-K type QDs generally [46]) to joint these two spectra to be a really broad one. To overcome these problems, it is advised to optimize the structure of active region in CMQD, such as capping thickness, number of stacking layers and growth condition for
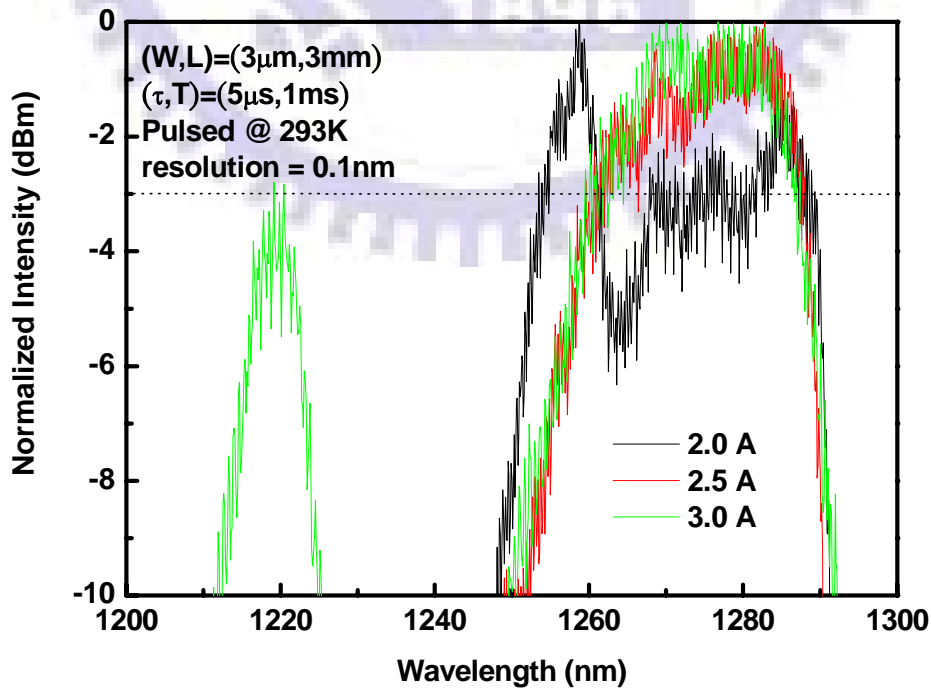
Fig. 4.13 The evolution of spectrum at high injection level for CMQD.

Table 4.3 The spectral dependence on current injection.

I (A)	0.3	0.5	0.8	1	1.3	1.5	1.8	2	2.3	2.5	2.8	3
FWHM (nm)	12.0	16.6	18.7	19.6	20.8	29.0	6.0	24.7	17.8	27.7	28.0	28.3

InAs QDs. By the way, simultaneous two GS lasing for CMQD with different structure at active region can be observed [47], which implies the potential for CMQD to be a suitable broadband light source.

4.3.6 Coherence

To obtain the information about the coherence of CMQD LD, we measured the interferograms for all devices as increasing current by the fiber-based, delay-tunable Mach-Zehnder interferometer. In order to couple the light into the fiber-based MZI, operating the lasers at cw mode is necessary. However, only devices with lengths longer than 1.5 mm could be operated at cw mode. Besides, pulse mode operation was adopted at higher current injection to prevent severe thermal effect. Fig. 4.14(a) ~ 4.14(e) shows the results with the linear-scale spectrum operating at $10*I_{th}$ for each device.
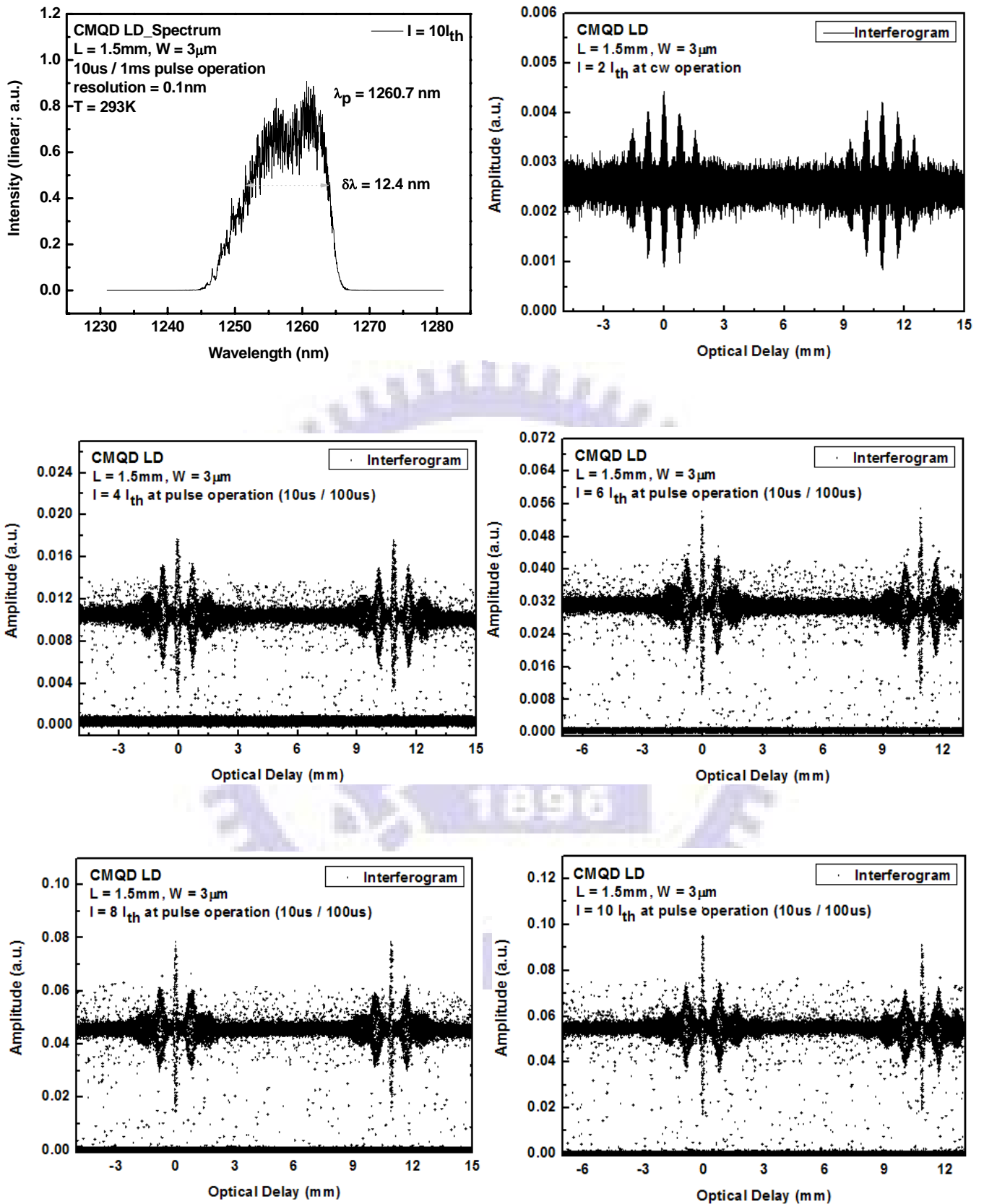
Fig. 4.14(a) The interferograms for CMQD LD with L =1.5 mm as increasing current injection and the linear-scale spectrum operating at $10 * I_{th}$.
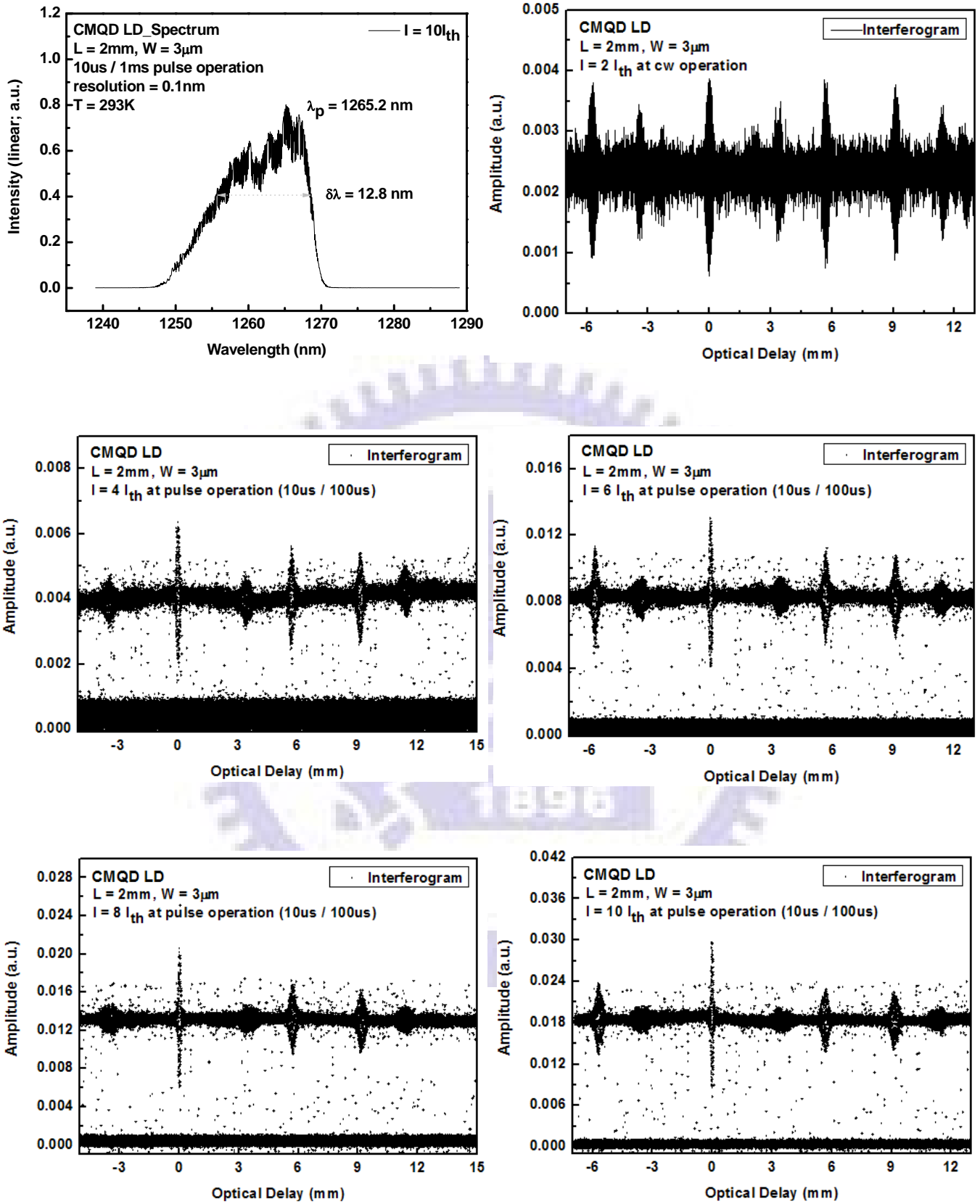
Fig. 4.14(b) The interferograms for CMQD LD with L=2mm as increasing

current injection and the linear-scale spectrum operating at 10* I_{th} .

Fig. 4.14(c) The interferograms for CMQD LD with L=3mm as increasing current injection and the linear-scale spectrum operating at $10 \ast I_{th}$.
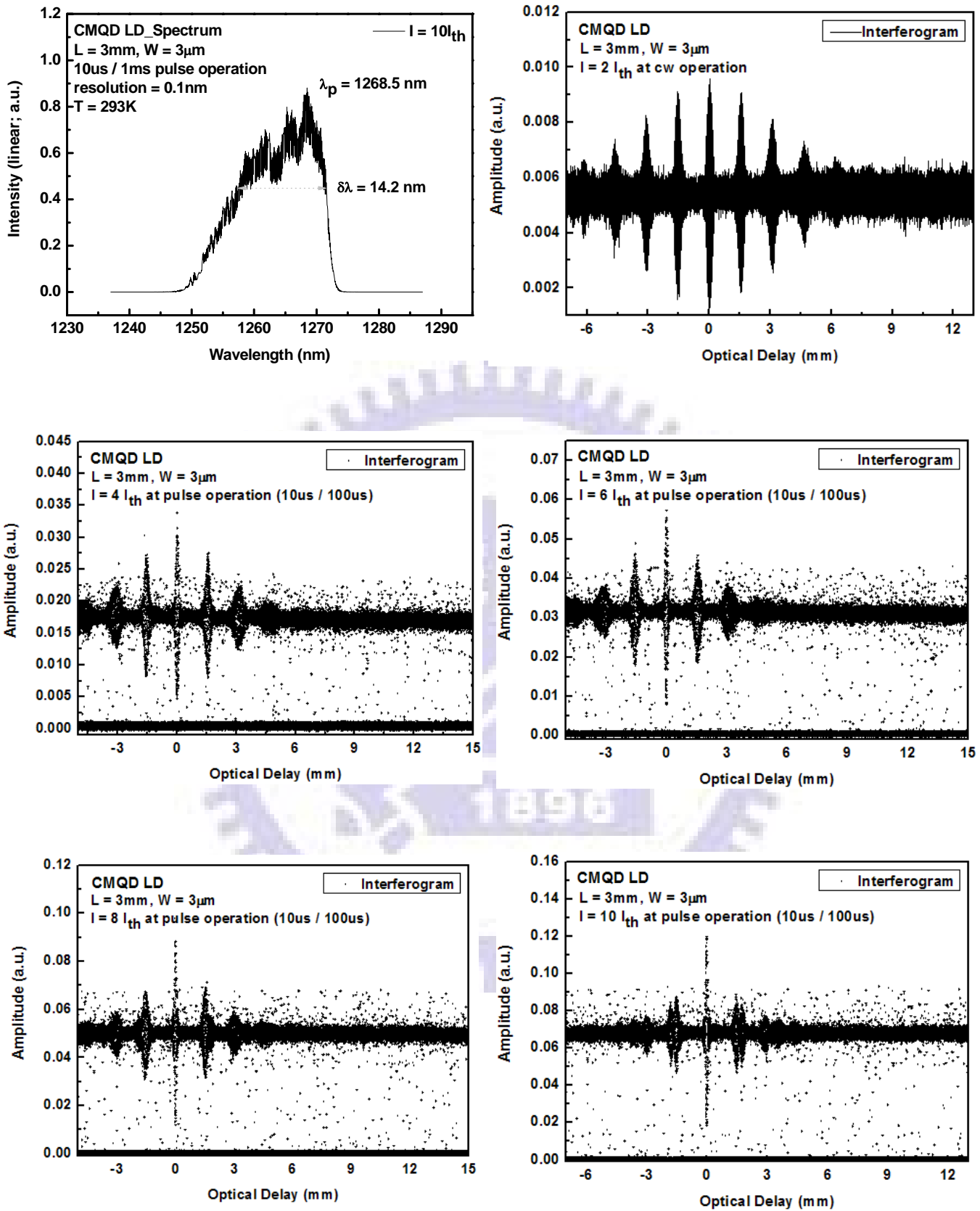
Fig. 4.14(d) The interferograms for CMQD LD with L=4mm as increasing

current injection and the linear-scale spectrum operating at $10*I_{th}$.

Fig. 4.14(e) The interferograms for CMQD LD with L=5mm as increasing

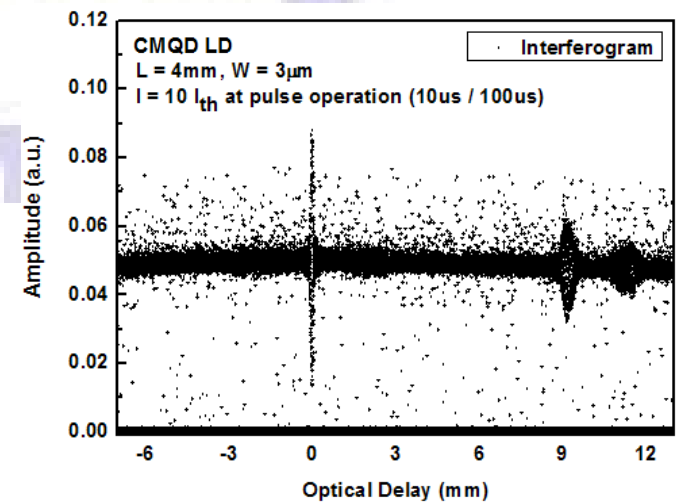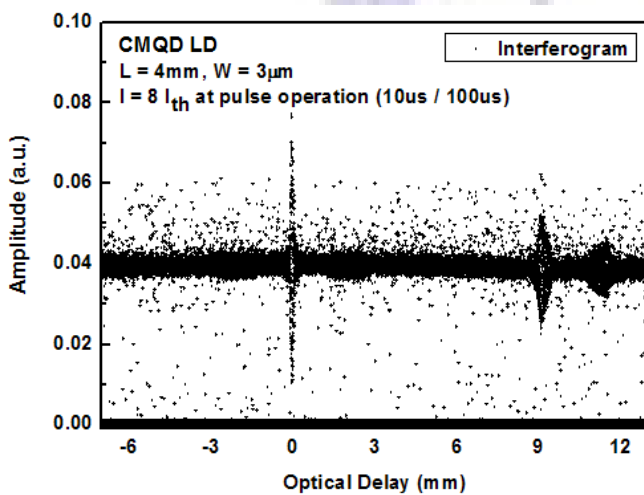current injection and the linear-scale spectrum operating at $10*I_{th}$.

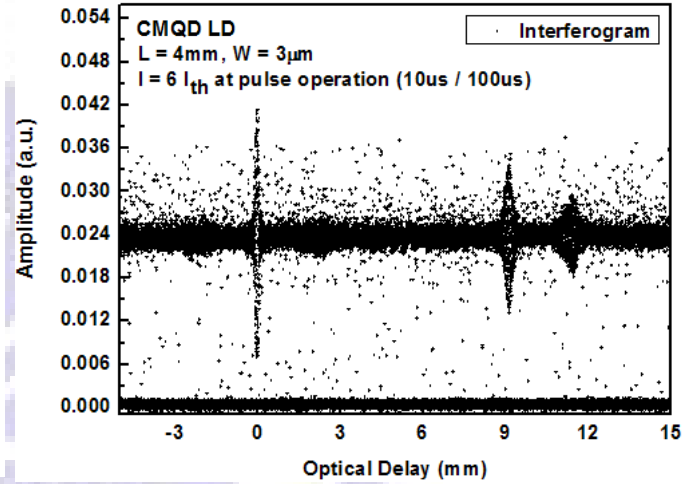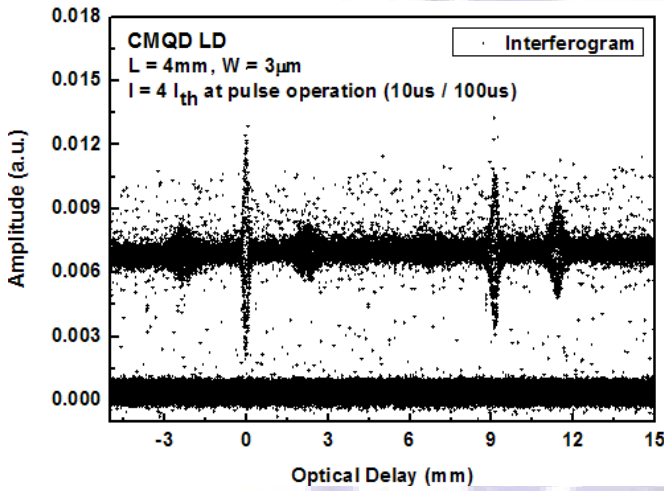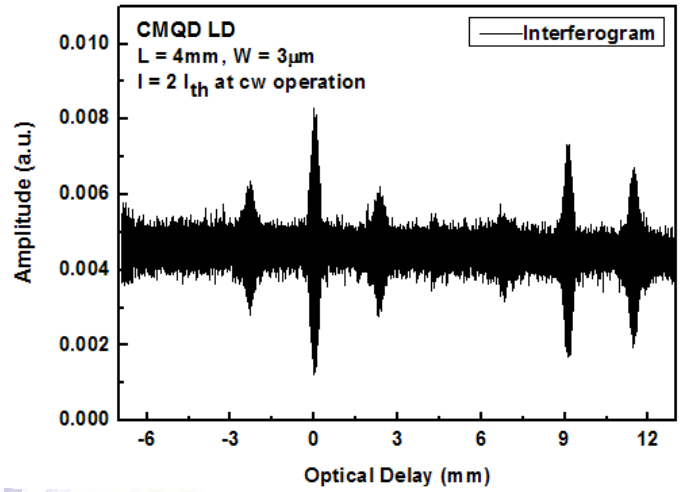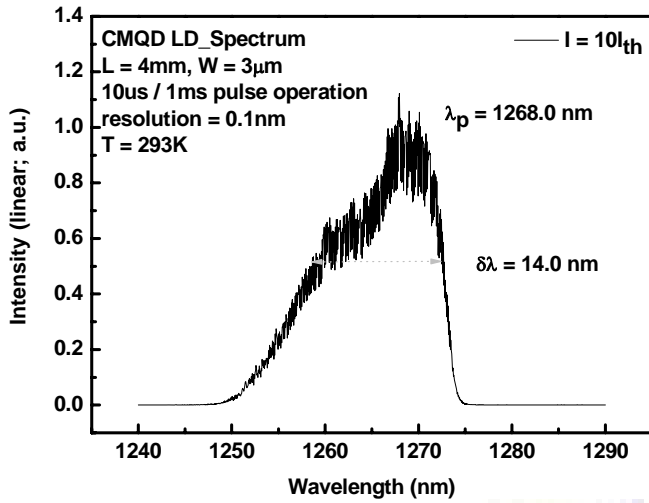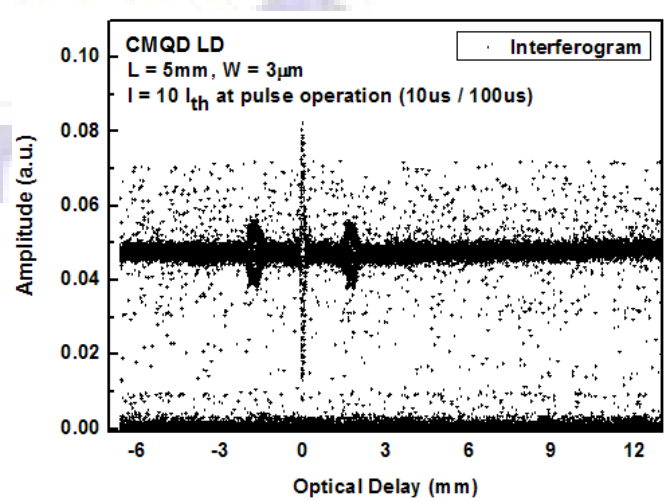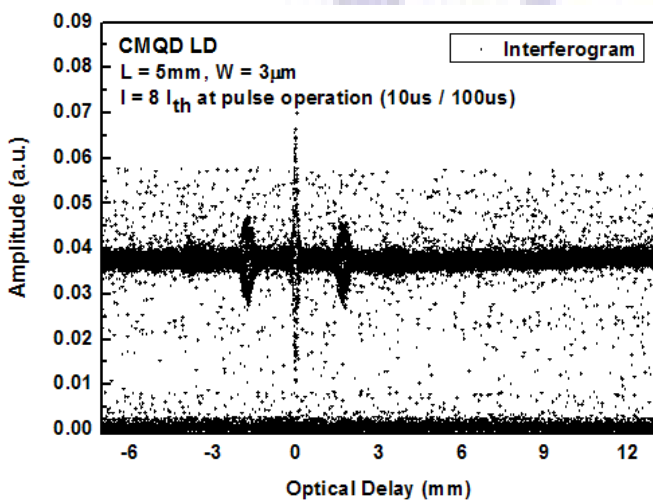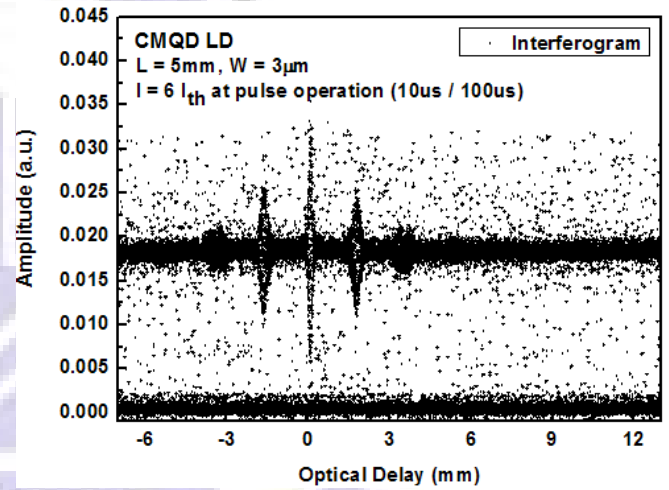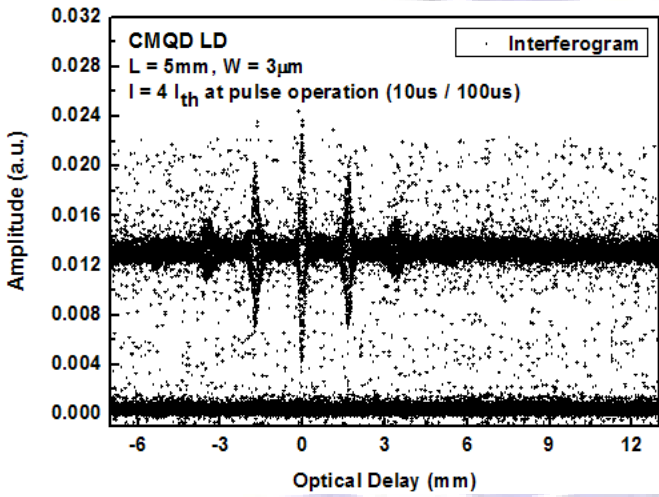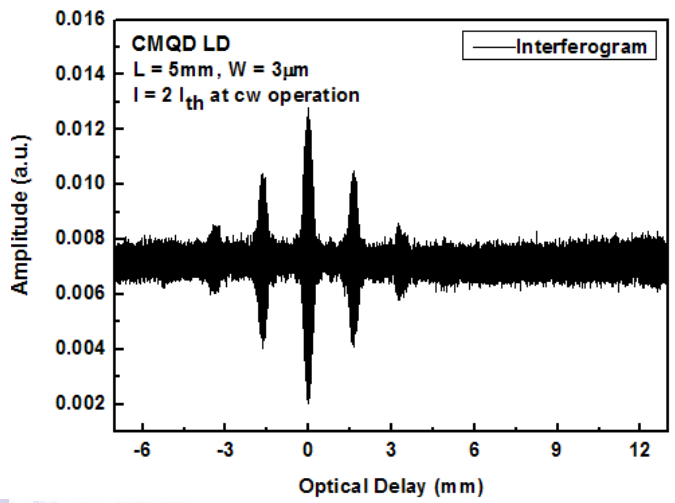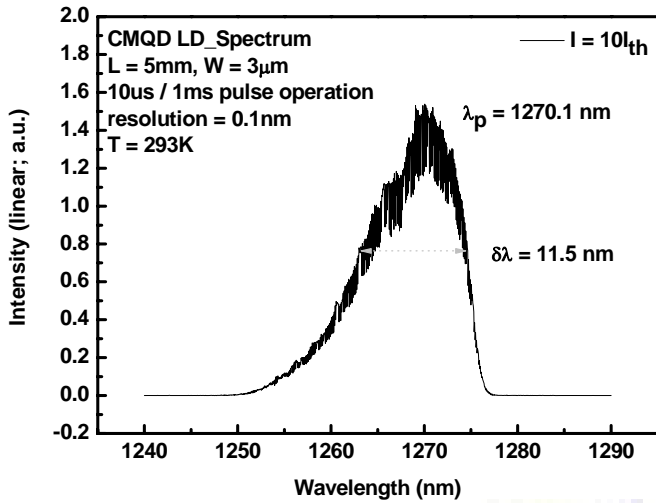Compared with the interferogram measured under cw operation, some noise data was observed in interferograms under pulse operation. Power fluctuation and digitization during the current rising and falling time are the main attribution. Though there exists these noise data under pulse operation, the profile of autocorrelation can still be clearly defined.

It is obvious that the interferogram doesn't seem to be a function of cavity length. There is no simply rule that could explain what the interferogram will look like with varying cavity length. Based on Wiener-Khinchin theorem, we know that the power spectrum density and the interferogram of a light source form a Fourier-transform pair. To understand why these interferograms do look like what they are, we start with discussing the relationship between spectra in linear scale of devices with different length. First of all, these spectra also show little dependence on cavity length, except for the longitudinal mode spacing. We tried to acquire more ideas from simulation and demonstrated the inverse Fourier transform of two adjacent Gaussian-like spectra with the same amplitude and FWHM, as depicted in Fig. 4.15. The result showed that the peak separation in the interferogram would depend on the distance between centers of the two Gaussian functions. Specifically, the interferogram would appear like the "beat" with a Gaussian envelope. In such a simplified case, the position of side peaks in interferograms could be easily predicted. However, it is difficult to make a connection between interferogram and its power spectrum in real case. Second, these spectra we measured may not the "real" spectra owing to the specific value of resolution we adopt when measuring. Therefore, it is difficult and, in fact, unnecessary to prove the validity of interferograms for such a complex spectrum of a broadband laser by Fourier transformation. In other words, instead of judging by spectrum, measuring interferogram is a more direct and more practical way to decide if a broadband "laser" is suitable or not

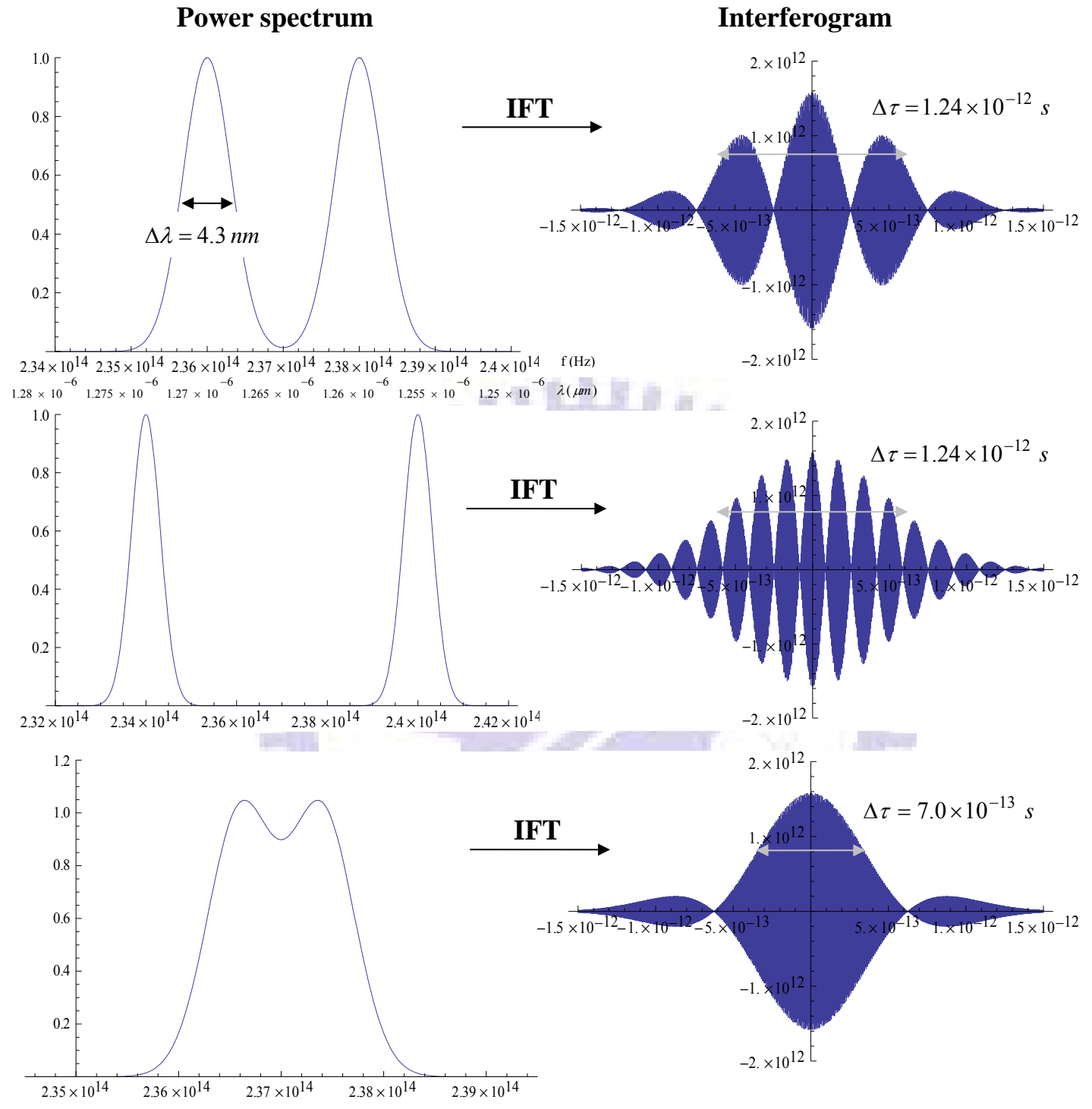**Power spectrum**　　　　　　　　　　　　**Interferogram**

Fig. 4.15 Simulation on interferogram of two adjacent Gaussian-like spectra with the same amplitude and FWHM.

for OCT application.

　　We try to quantitatively determine the coherence length for our CMQD LD. For a LD with specific cavity length, the difference between

interferograms of different pumping level can be well-explained. As the spectrum broader and broader (as increasing current), a narrower main peak (at zero optical delay) and a larger contrast between main peak and side mode (at elsewhere) can be observed in all interferograms we measured. This tendency consists well with our simulation of Fourier transformation for complex and multi-Gaussian profile. However, a problem occurs when it comes to determine the coherence length quantitatively. Due to the complexity of lasing spectrum, it is difficult to clearly define the whole envelope of interferogram within the limited delay range (~2 cm) in our MZI [47]. Moreover, the penetration depth of OCT at wavelength around 1.3 μm is about 2 mm. Consequently, we "roughly" defined the FWHM of the main peak in interferograms as the "practical coherence length". The main peak of interferogram for 3-mm-long device was shown in Fig. 4.16. The practical coherence lengths with varying injection levels are depicted in Fig. 4.17. These show that practical coherence length could be as short as 100 μm in our CMQD laser. It is a reasonable value for spectral width of 14 nm which centered at 1260 nm. It means the extremely broad spectral width of 29 nm at high injection current we mentioned before was expected to have coherence length less than 50 μm. Indeed, it is still too long to be applied to OCT. Besides, the progressive shrink in the FWHM of main peak implies that a broader bandwidth could be obtained at higher pumping level. Fig. 4.18 shows the FWHM of spectra plotted as a function of injection current. The result consists with the characteristic of Fourier transform. In conclusion, the FWHM of the main peak in an interferogram could be viewed as an indicator for judging how broad the spectrum of a broadband laser is.
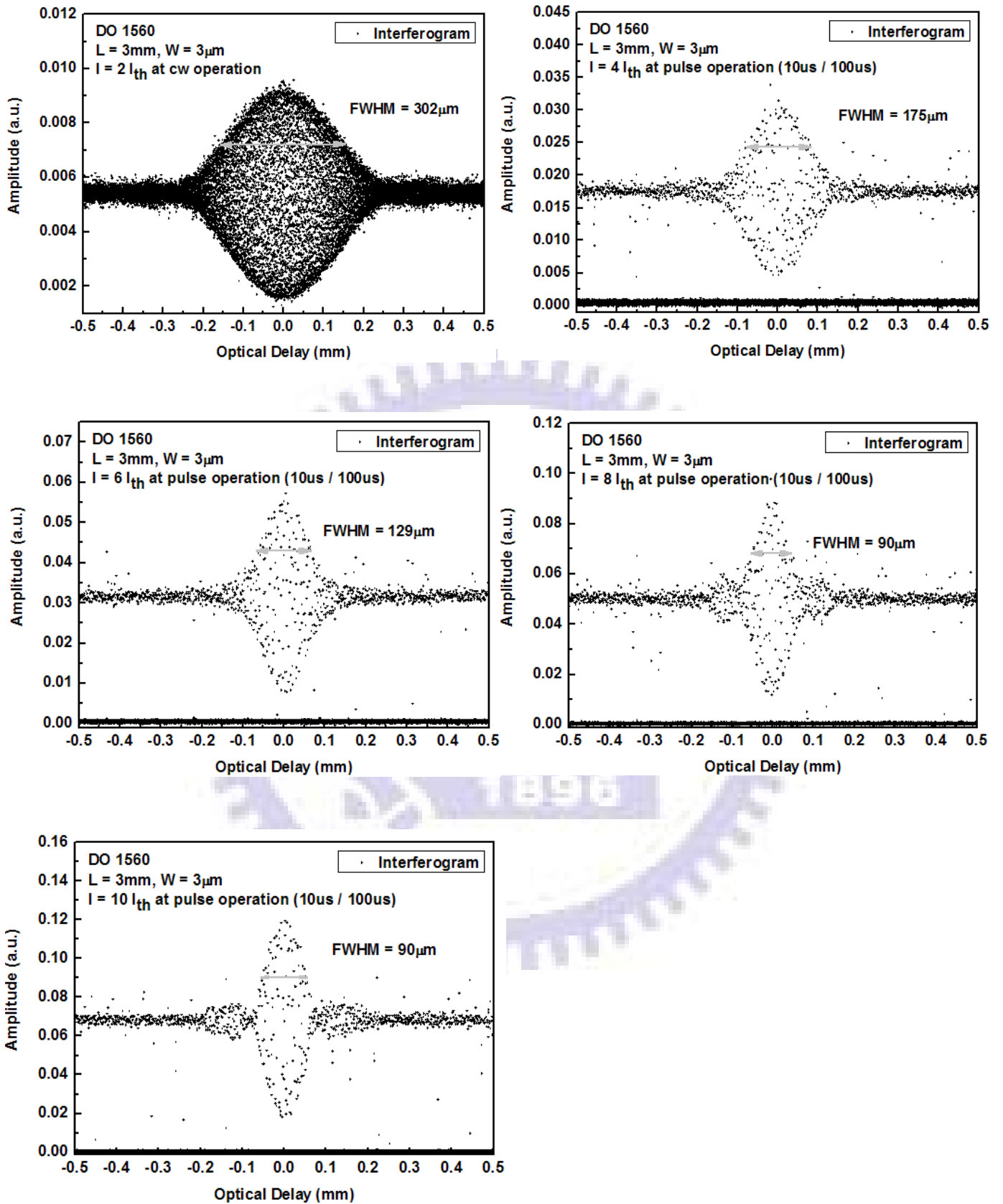
Fig. 4.16 The main peak in interferograms as increasing current injection for 3-mm-long device of CMQD LD.
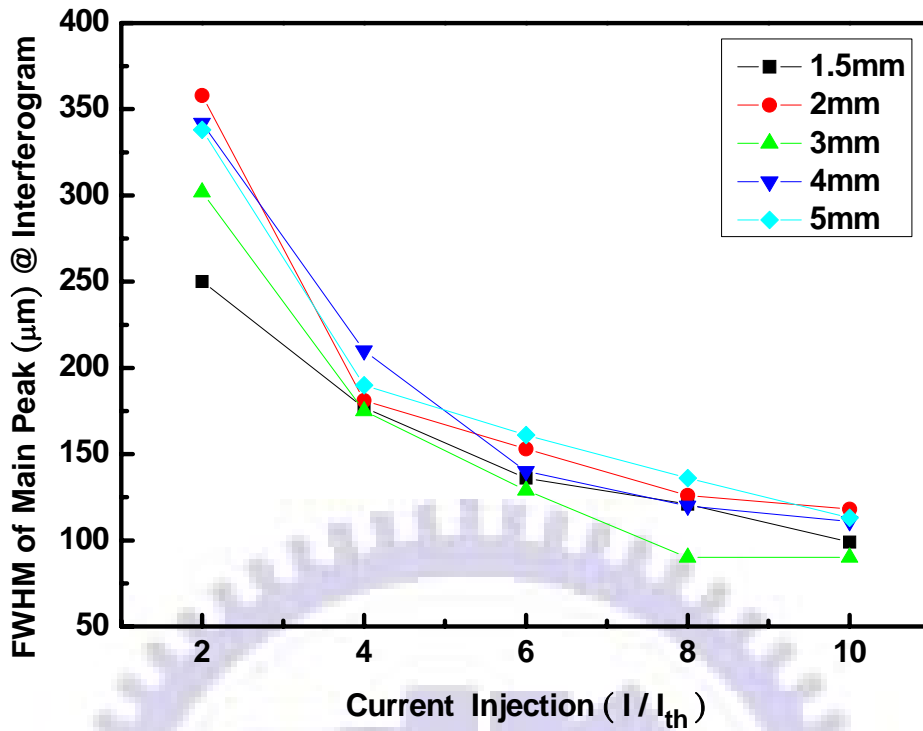
Fig. 4.17 The practical coherence length plotted as a function of current injection for CMQD LD.
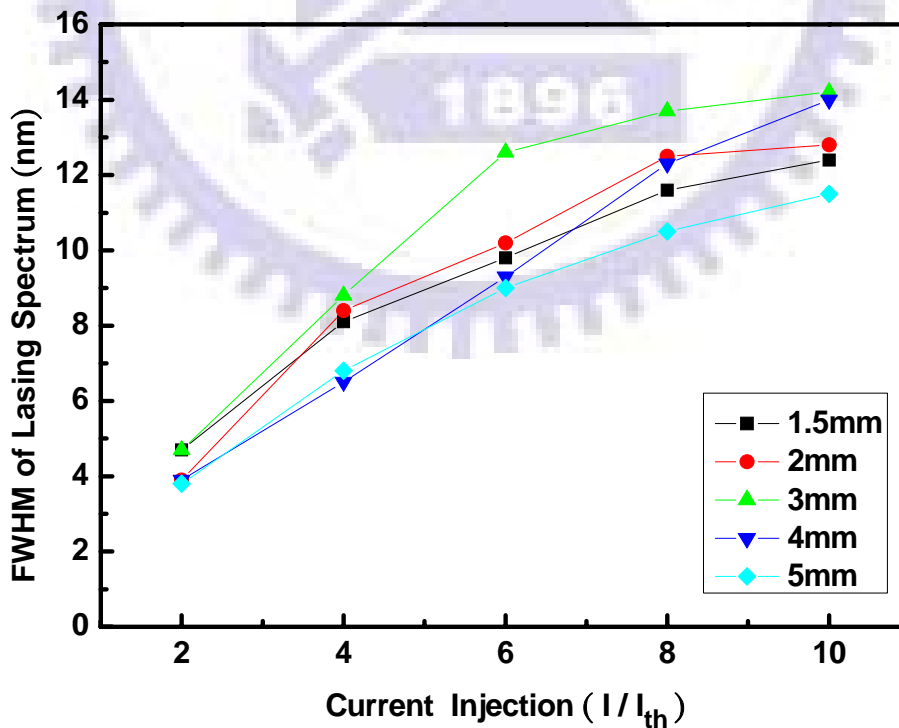

Fig. 4.18 The FWHM of lasing spectra plotted as a function of injection current.

Chapter 5
Conclusions and Future Works

5.1   Conclusions of Present Studies

In summary, we have demonstrated a specially designed chirped-multilayer (N=10) quantum dot (CMQD) broadband laser with 3-, 4- and 3-layer of longer-, medium, and shorter-wavelength QD states, respectively. An extremely broad spectrum of 29 nm without any 3dB dip at very fine resolution of 0.1 nm was achieved. It centered at 1270 nm and was expected to have an applied coherence length less than 50 μm. Laser parameters with η_i of 88.3% and α_i of 3.0 cm^{-1} were extracted from devices with different cavity lengths. Instead of coming from single quantized state, the lasing peak results from the total effect of simultaneous multi-states pumping. The carrier population without well distribution and non-equal contribution to threshold modal gain are the main attribution. A higher GS saturated gain and higher transparency current density of 126.1 A/cm^2 were obtained from gain-current analysis. The structure of CMQD should be optimized to improve the vertical beam divergence for higher coupling efficiency. The characteristic temperature T_0 of 82.4 K in the range of 283 K~353 K has been measured.

Competition between thermal effect and inhomogeneous broadening was observed in spectra of devices with different gain-loss condition. A reasonable group effective index at active region of 3.73 was extracted from longitudinal mode separation. To acquire the coherence information of our CMQD, we have set up a fiber-based, delay-tunable Mach-Zehnder interferometer. The accuracy of measurement has been confirmed by mathematical simulation (Weiner-Khinchin theorem) on commercial

lasers with simple spectral profiles. Due to longitudinal modes in broad-spectrum laser, the interferogram is much more complex than that of SLD. Instead of judging by spectrum, interferogram measurement is a more direct and more practical way to decide if a "broad-spectrum" laser is suitable or not for OCT application. Finally, the FWHM of the main peak in an interferogram could be viewed as an indicator for judging the spectral width of a broadband laser.

5.2   Suggestion for Future Works

For low-coherence application such as OCT, a real broad and nearly flat-top spectrum without ripple is demanded. Owing to the high-power advantage of broadband laser over SLD, the main issue for realizing broadband laser is how to make its spectrum broader. To achieve the goal, simultaneously two-state lasing (ES and GS or two GSs) is one of the approaches. However, only FWHM of spectrum of 29nm, corresponding to coherence length less than 50μm, can be achieved in our CMQD. To improve the performance in the spectral issue, it is advised to optimize the structure of active region in CMQD, such as capping thickness, number of stacking layers and growth condition for InAs QDs.

First of all, simultaneously two-GS lasing can only be achieved in the structure where the carrier population is well-distributed. It means that a change in gain-current characteristic has to be made by readjusting the number of stacking layers of different QD states [48].

Second, the growth condition of active layer, such as InAs thickness and growth temperature, must be optimized carefully. With increasing InAs thickness, the PL peak will shift to the long wavelength side due to an increased dot size and the spectral width becomes small due to the improved dot size uniformity [49]. In other words, a broad spectral width

can be obtained when the InAs is thinner due to size dispersion. On the other hand, at lower growth temperature, the spectral width of the QDs increases and the PL efficiency decreases [49]. This can be attributed to a reduced diffusion length of atoms at lower growth temperature [50]. The size distribution of these dots is very inhomogeneous which may result in the broad emission spectrum.

Third, it is reported that the Beryllium modulation-doping could be used to further increase the PL spectral width in MQWs [51]. The physical mechanism of the broadening is considered to be partly related to the many-body effect by built-in majority holes. A similar mechanism may also play a role in the modulation-doped QD case [52].
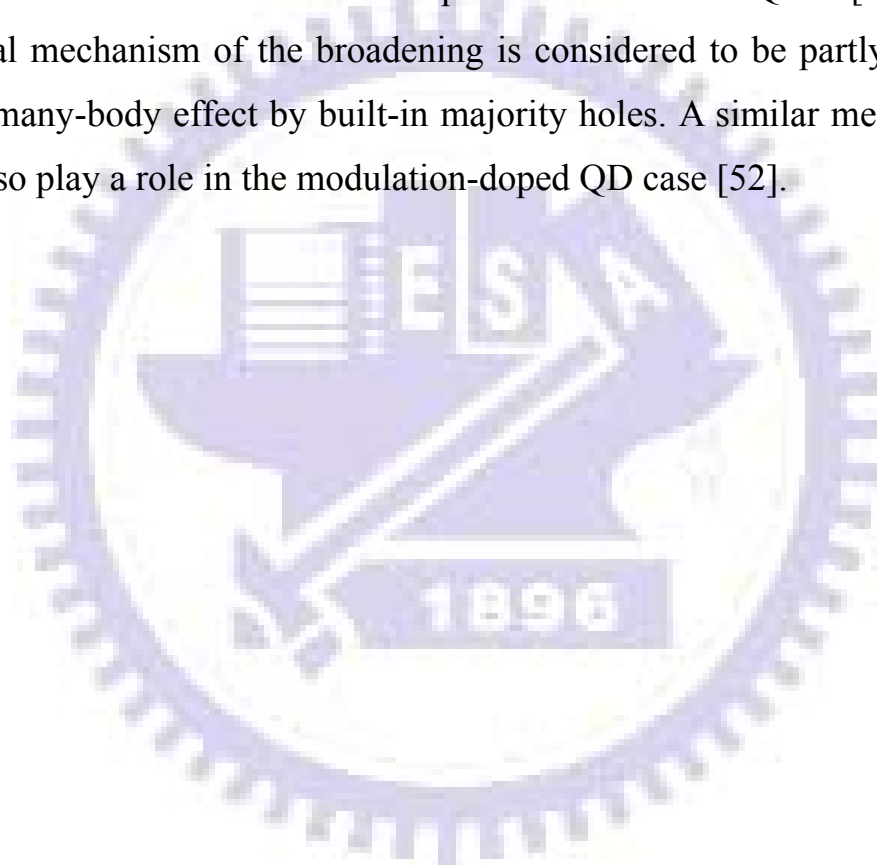
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喁啾式多層堆疊量子點雷射之特性暨其適用於光學同調斷層掃描系統之可行性分析研究

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