

國立交通大學

電信工程學系

碩士論文

6GHz 縮小化頻率調變連續波雷達系統

6GHz Compact Size

Frequency Modulation Continuous Wave

Radar System

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摘要

本篇論文是一套 6GHz 縮小化 FMCW 雷達。從天線到射頻模組以及 FMCW 演算法的改進。天線部份其一是超寬頻天線架構。有別於傳統超寬頻天線大多是用一大片金屬來當輻射體或是多個不同頻段之天線來達到寬頻的要求，此天線架構是利用一段靠近地的間隙來使天線的輸入阻抗在極大的頻寬內沒有很大的變化。此天線架構類似常見的倒 F 型天線(Inverted-F antenna)，但縮小天線與地的間距，即可得到一相當寬頻的天線。另一個是天線陣列，使用槽孔天線當天線元件做成的 2x1 的天線陣列。來滿足所需之天線指向性。

FMCW 雷達演算法改進是基於學長之前所做的 24GHz FMCW 雷達系統再加以改良。本來是用一連串的鋸齒波，並對回波訊號做 2D 的 FFT 來達到偵測目標物距離與相對速度的功能。但舊有的演算法須要較大的運算量以及較高的硬體要求，所以我用了不同的調變方法。有別於一連串的鋸齒波調變，我使用一個較慢的三角調變波，可避免相度速度的影響，且大幅減少運算量以及硬體的的要求。此外，為了在有限頻寬內提高距離解析度，所以加入了補零的動作，並根據舊有的訊號特性改進了原來的中頻放大器。在距離解析度上至少提高了一倍的準確度，改進後的中頻放大器也讓雷達系統的靈敏度提高 10dB 以上。

6GHz FMCW 縮小化射頻模組，跟 24GHz FMCW 雷達不一樣。為了縮小化所以使用同一根天線當接收與發射使用。且系統中只使用了一個 6GHz 壓控震盪器以及一個平衡混頻器。使用單天線會受到天線特性而對系統靈敏度有很大的影響，不過基於 24GHz FMCW 雷達的經驗，能壓抑天線特性的影響進而完成模組的整合。

6GHz FMCW Radar System

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Abstract

A 6GHz compact size radar system is proposed in this article. There are several parts; antenna, Rf module and DSP improvement. This article proposed two different kinds of antenna. One is a novel wideband antenna. A small gap between radiator and ground smoothes the input impedance variation. The antenna structure proposed quite like a Inverted-F antenna. Just lower the gap size, this common antenna type comes a wideband antenna. Another proposed antenna is a 2x1 aperture couple antenna array. Aperture couple antenna has good directivity naturally. So a array with two antenna element can satisfied the requirement.

Digital signal processing is base on the previous approach and adds some improvement. 2D FFT is used in previous approach. Using different control wave can save system resource and 1D Chirp Transform is enough. Zero padding technology is also used to improve distance and relative velocity resolution. And a modified IF amplifier is also proposed. This amplifier upgrades system sensitivity to 10dB better.

At the last is a compact size 6GHz FMCW radar module. In order to have smaller dimension this RF module has a VCO, a hybrid mixer and a filter

only. Not like 24GHz radar system, this radar system uses the same antenna for Tx/Rx. Using single antenna can save half antenna area but the characteristic of antenna affects a lot. Base on the experience in 24GHz radar system there are some approaches to suppress the effect of antenna and implement this compact size radar system successfully.



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Chapter 1

Introduction of Radar system

1.1 Background

Interest in ITS comes from the problems caused by traffic congestion worldwide and a synergy of new information technologies for simulation, real-time control and communications networks. Recent governmental activity in the area of ITS, specifically in the USA, is further motivated by the perceived need for Homeland Security.

Advanced Vehicle Control and Safety System is part of intelligent transport system. The advanced technology is used on the car and road facilities in helping drivers control the car so as to minimize accident and enhance traffic safety. This system includes main functions of anti-collision alarm and control, maneuvering backup, automatic horizontal/longitudinal control, as well as remote automatic driving and automatic highway system in the future.

1.2 Radar System Basic Principle and Radar System Introduction

The electronic principle on which radar operates is very similar to the principle of sound-wave reflection. When shouting in the direction of a sound-reflecting object, there comes an echo. According to the speed of sound in air, one can estimate the distance and general direction of the object. The time required for an echo to return can be roughly converted to distance if the speed of sound is known. Radar uses electromagnetic energy in much the same way. The radio-frequency (RF) energy is transmitted to and reflected from the reflecting object. A small portion of the reflected energy returns to the radar set. This returned energy is called an echo, just as it is in sound terminology. Radar sets use the echo to determine the distance of the reflecting object.

$$R_{\max} = \left[\frac{P_t G^2 \sigma \lambda^2}{(4\pi)^3 P_{\min}} \right]^{\frac{1}{4}} \quad (1.1)$$

Radar system will obey the radar equation in Eq 1.1[1]. It represents the physical dependences and one can access the performance of the radar with the radar equation. First, we assume that electromagnetic waves propagate under ideal conditions. If RF energy is emitted by an isotropic radiator, then the energy propagate uni-formally in all directions. Areas with the same power density therefore form spheres ($A= 4\pi R$) around the radiator. Then in Fig. 1-1 it shows that target can be treat as another antenna. RF energy it reflected also propagate uni-formally. And how much it reflect can be replace by a coefficient “ σ ”, Radar Cross Section (RCS). The used antenna play the role of transmitting and receiving. So antenna gain (G) should be square. And then, when transmitted larger power, the reflection power comes higher. Finally, the system sensitivity will decide the detection of rangeradar system.

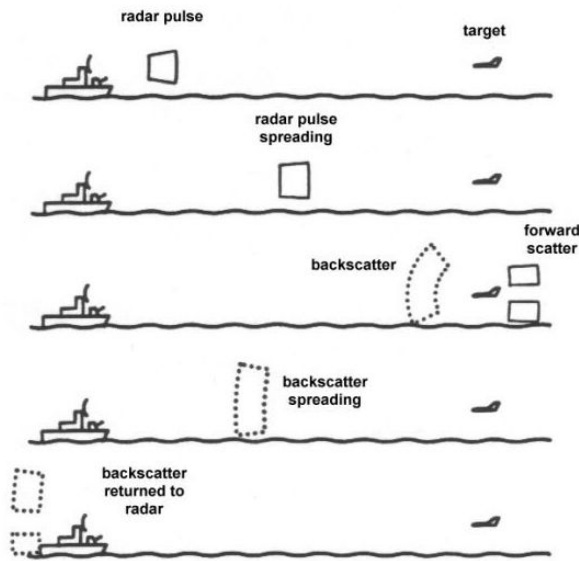


Figure 1-1: Diagram of Radar System

After the introduction of radar system basic principle, we will introduce some different kinds of radar system. There are many different technologies for Anti-collision Safety System such as Ultra-sonic, Infrared, Laser, Video and Microwave radar. Microwave radar performs well in every items. So we choose it to implement our anti-collision system. In microwave radar system, there are also several different kinds. Such as pulse radar, FMCW radar and Doppler radar[2]. Pulse radar is popular in war time and has been well developed. Fig. 1-2(a) is a simple diagram of how pulse radar works. Generate several RF pulse signals, and find out in which time slot the recieved signal is. The distance resolution depends on how narrow in time domain the RF pulse is. Relative velocity can be found in the Doppler effect on RF carrier. The algorithm of pulse radar is quite simple, but implementation of the circuit is much more difficult then FMCW radar.

Fig. 1-2(b) is the diagram of FMCW radar. FMCW is the abbreviation of Frequency Modulation Continuous Wave. We add a linear frequency modulation on the center frequency. Fig. 1-3, Fig. 1-4 is voltage control oscillator (VCO) control voltage versus

to time. The time delay between transmitted signal (Tx) and received signal (Rx) will result in a inter-medium frequency (IF) signal. By detecting the IF signal frequency, we can calculate the target distance. Fig. 1-3 is the situation without relative velocity and Fig. 1-4 is with relative velocity. The IF signal is the result of distance and relative velocity. Relative velocity causes the Doppler effect and will shit the IF frequency higher or lower. Doppler effect will cause another problem in detection.

Doppler radar is similar to FMCW radar. Since relative velocity will cause some frequency shift. Transmit continuous wave (CW) and detect the frequency difference between transmitted and recieved signal can get the relative velocity.

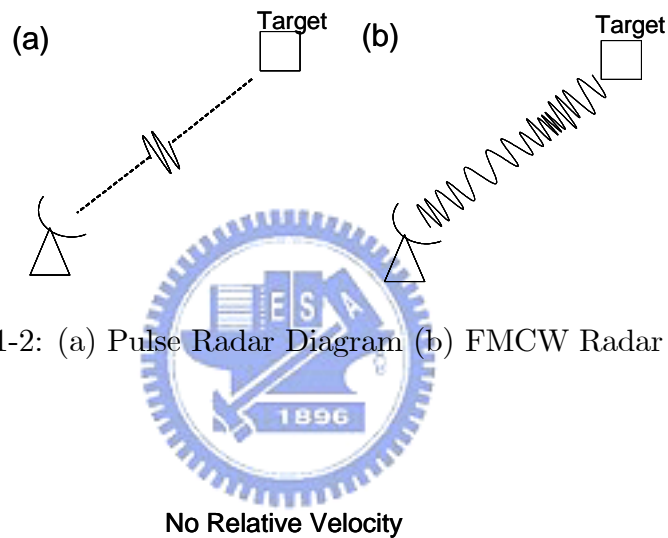


Figure 1-2: (a) Pulse Radar Diagram (b) FMCW Radar diagram

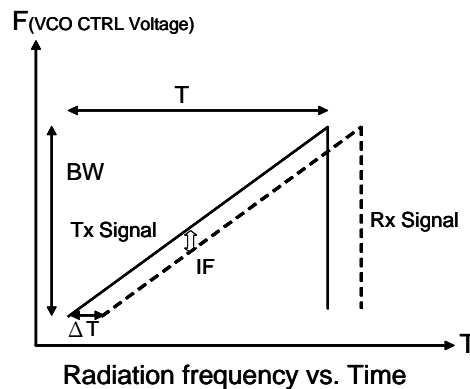


Figure 1-3: Frequency Modulation Wave and Receiving Signal without Relative Velocity

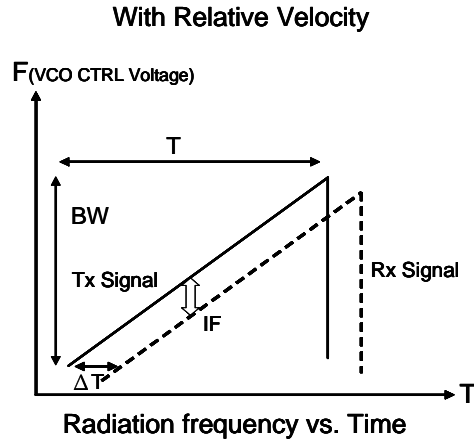


Figure 1-4: Frequency Modulation Wave and Receiving Signal without Relative Velocity

1.3 FMCW Radar Distance and Velocity Detection

In FMCW radar, the IF frequency is proportional to the target distance if there is no relative velocity. So, distance resolution is decided by IF frequency resolution. In Fig. 1-3(a) is the condition without relative velocity. T is the period of control voltage. BW is the bandwidth of frequency modulation. It has 150 points in one cycle, so sample rate is $\frac{150}{T}$. VCO frequency slope “ α ” is $\frac{BW}{T}$ and if the slope larger the IF frequency comes higher. From Eq 1.2 to Eq. 1.5. we can see that distance resolution is proportional to the used bandwidth and the ratio of over-sampling.

$$IF \text{ frequency} = \alpha * \Delta T \propto \alpha * \Delta d \quad (1.2)$$

$$\text{Minimum Frequency Resolution} = \frac{150}{T} * \frac{1}{128} \quad (1.3)$$

so

$$\alpha * \Delta d = \frac{BW}{T} * \Delta d \propto \frac{150}{T} * \frac{1}{128} \quad (1.4)$$

$$\text{Distance Resolution} \propto BW \quad (1.5)$$

Velocity detection is according to Doppler effect. Since Doppler effect is $f_{Doppler} = \frac{2vf}{C}$ only dependent on the operation frequency and relative velocity. Because IF frequency is the combination of distance and velocity, the control voltage slope rate should be higher enough. Doppler effect in FMCW radar system will be discussed later.



Chapter 2

24GHz FMCW Radar System

2.1 24GHz FMCW Radar System Architecture

Fig. 2-1 is the 24GHz FMCW radar system architecture. It can be separate into two parts. One is the RF circuit module and another is the IF amplifier, frequency modulation control circuit and DSP core. First in RF circuit , there is a 6GHz VCO source and the tuning range should larger then the operation bandwidth. After VCO is a 6GHz to 12GHz frequency doubler and 12GHz amplifier. In order to lower the effect of antenna, two antenna type is chosen. One for transmitting signal and another for receiving the echo. After 12GHz amplifier is a power divider which transmits the signal to Tx and Rx. In Tx path, there is a 12GHz to 24GHz frequency doubler, a band-pass filter and a patch antenna for easy integration with other circuit. In Rx path, there is another 12GHz amplifier to generate a flat LO signal. Next to the 12GHz amplifier is a sub-harmonic mixer, band-pass filter and patch antenna. LNA is the following work.

The base band circuits are IF amplifier, frequency modulation control circuit and DSP core. IF amplifier provides voltage gain and is an active band-pass filter also. Frequency modulator is combined with DSP core in the micro-processor unit (MCU) we used. Combination of these two part can suppress timing error.

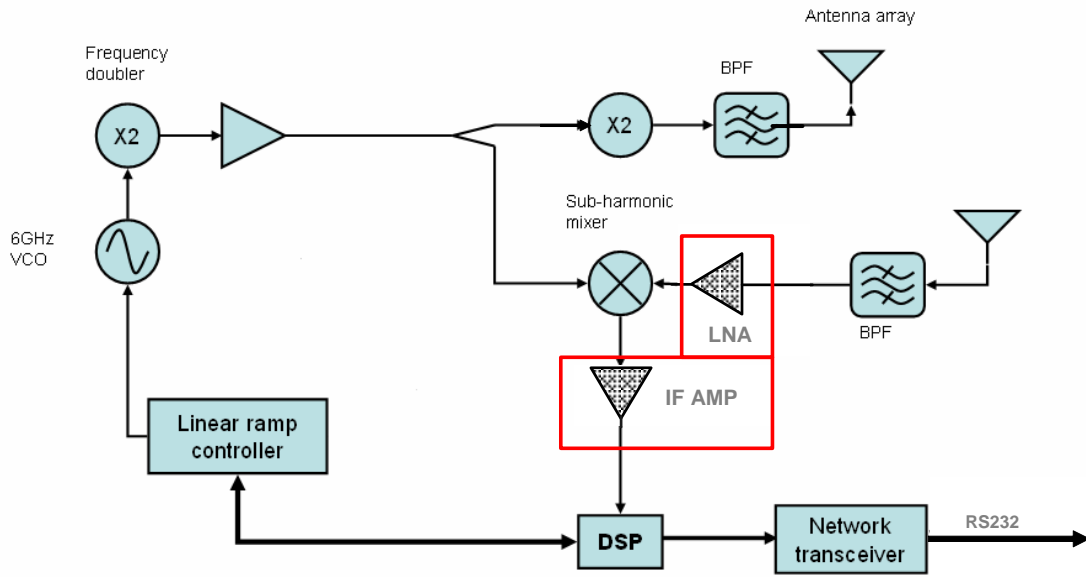


Figure 2-1: 24GHz FMCW Radar System Architecture

2.2 24GHZ FMCW Radar System Algorithm

2.2.1 Signal Processing Flow Chart

Fig. 2-2 is the signal processing flow chart of 24GHz FMCW radar system. It implements in ARM7 base microprocessor with 64KB RAM. Peripherals initial at the beginning. Set system clock to 40MHz to drive this chip in the highest performance. Then initiate peripherals such as:

- 1.AD/DA : For frequency modulation and sampling IF signal
- 2.Timer : Interrupt timer is to control AD/DA in the correct timing.
- 3.UART : Use it to transport data and change system parameter.
- 4.GPIO : Transport other control data such as LED alarm.

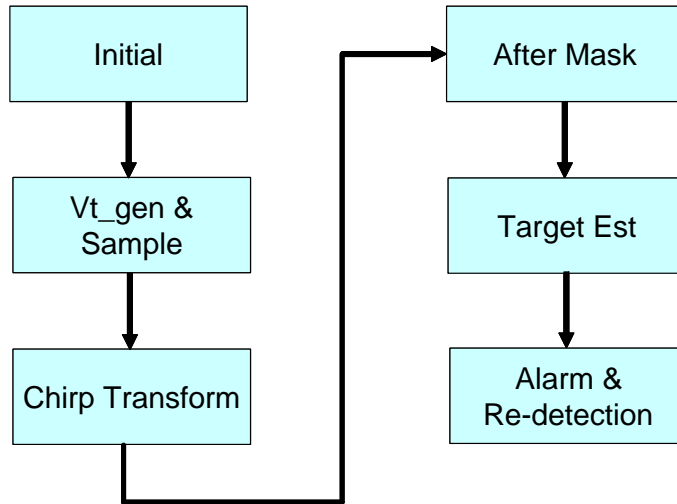


Figure 2-2: FMCW Radar Digital Signal Flow Chart

The timer counts down and interrupts system into interrupt subroutine after initialization. Fig. 2-3 is the C code of interrupt subroutine. One key point should notice. The timing of resetting timer counter is important. Since the subroutine doesn't spend the same operation time, the timer should be reset at the beginning ($T1CLR1 = 0$). Other C code is to generate frequency modulation wave by changing register DAC0DAT and reading register ADCDAT to get IF signal.

Interrupt Subroutine

```

T1CLR1 = 0;
DAC0DAT = (_Vtune[FIQ_times]<<16);
ADCCON = 0x7E3;
while (!ADCSTA){}
  _Sample_data[FIQ_times]=ADCDAT>>16;
  FIQ_times++;
  
```

Figure 2-3: C Code of the Interrupt Subroutine

Put those data into Chirp Transform and ignore the head and tail sample data to avoid transient distortion.. In the next section, there is some introduction of Chirp Transform and how to implement in C code. After Chirp Transform is a block call “After Mask”. As we all know, every system has its own noise. The way to design whether this result is a target or not is to compare the IF signal and background noise in frequency domain. In FMCW radar algorithm, a target makes an echo and results in a tone in frequency domain. We calibrate back ground noise and generate a threshold called “ Mask “. The detection result in frequency domain will compare with this threshold. The comparison result transports to the block “ Target Estimation”

Target Estimation is consisted of several determinations. The lower threshold is used the farer this system can detect. What happens if the threshold comes lower? There comes more un-wanted noise peak higher then the threshold. The determinations can filter out some un-wanted noise and lower the threshold.

The result of target estimation is a final target table. The alarm condition has been decided at the beginnig and the micro-processor will generate alarm or start another detection according to those condition. In Fig. 2-1 some debug data will transport using UART. Once the radar is set at the testing car, it is hard to get the data in memory. So there is a simple communication protocol to communicate with radar system using UART.

2.2.2 Chirp Transform

Chirp Transform (Fig. 2-4) is the extension of the DFT[3]. It is not optimal in minimizing any calculation, but is more flexible than the FFT. Unlike the FFT, the DFT is that multiply every data with the mapping coefficient. Then the sum of all those multiply result is the value in frequency domain. Chirp Transform is quite the same as DFT. By modifying the coefficients only part of points in unit circle are computed. Eq. 2.1 to Eq. 2.8 are the equations of Chirp Transform.

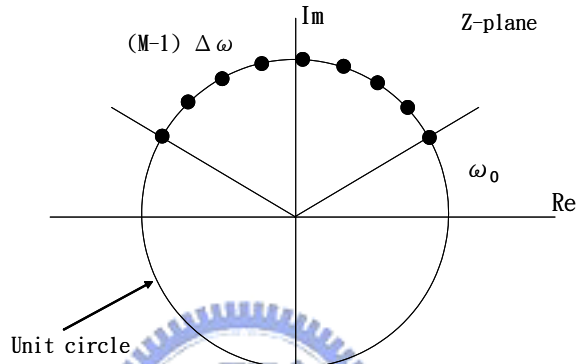


Figure 2-4: Diagram of Chirp Transform

$$\omega_k = \omega_0 + k\Delta\omega, \quad k = 0, 1, \dots, M-1 \quad (2.1)$$

$$X(e^{j\omega_k}) = \sum_{n=0}^{N-1} x[n]e^{-j\omega_k n}, \quad k = 0, 1, \dots, M-1 \quad (2.2)$$

with W defined as

$$W = e^{-j\Delta\omega} \quad (2.3)$$

$$X(e^{j\omega_k}) = \sum_{n=0}^{N-1} x[n]e^{-j\omega_0 n} W^{nk} \quad (2.4)$$

To express $X(e^{j\omega_k})$ as a convolution, we use the identity

$$nk = \frac{1}{2} [n^2 + k^2 - (k - n)^2] \quad (2.5)$$

$$X(e^{j\omega_k}) = \sum_{n=0}^{N-1} x[n] e^{-j\omega_0 n} W^{\frac{n^2}{2}} W^{\frac{k^2}{2}} W^{-\frac{(k-n)^2}{2}} \quad (2.6)$$

Letting

$$g[n] = x[n] e^{-j\omega_0 n} W^{\frac{n^2}{2}} \quad (2.7)$$

We can then write

$$X(e^{j\omega_k}) = W^{\frac{k^2}{2}} \left(\sum_{n=0}^{N-1} g[n] W^{-\frac{(k-n)^2}{2}} \right), \quad k = 0, 1, \dots, M-1 \quad (2.8)$$

The received signal frequency is start from DC so ω_0 is zero and simplifies the C code. Calculate the coefficient (nk) first and find the mapping cosine and sine wave index. There is a natural back ground noise in low frequency. In order not to affect higher frequency by the skirt of back ground noise, sample data should apply window on it. We choose Blackman Window since it has the lowest skirt level. Then multiply those after window data with W and add the results together. There is a shift n-bit operation in this C code. Because the micro-processor only calculates integer and in order not to be over-float, pre-shift operation is necessary. Fig. 2-5 is part of Chirp Transform in C code.

```

for (n=0 ; n<128 ; n++)
{
    nk=n*k;
    index_temp=(nk>>8);
    After_window=
    (*psample_data*Blackman_window[n-64])>>10;
    real+=After_window*(sin[index]);
    image+=After_window*(cos[index]);
    psample_data++;
}
.
.
real=(real>>12);
image=(image>>12);
_Chirp_result[k]=(real*real+image*image)>>1;

```

Figure 2-5: C Code of Chirp Transform

2.2.3 UART Protocol

There is a UART communication in the program for debugging this system. There are two things should notice. One is to make sure the communication link can built and the data in package should read correctly. Second is that this debug program should not affect the main processing. If the terminator (PC with Labview) doesn't plug on, this UART program should be bypassed. Under these two consideration, we design the following UART protocol as in Fig. 2-1. It is simple and can make sure the link is built. Also, it can bypass the UART program if the terminator doesn't plug on.

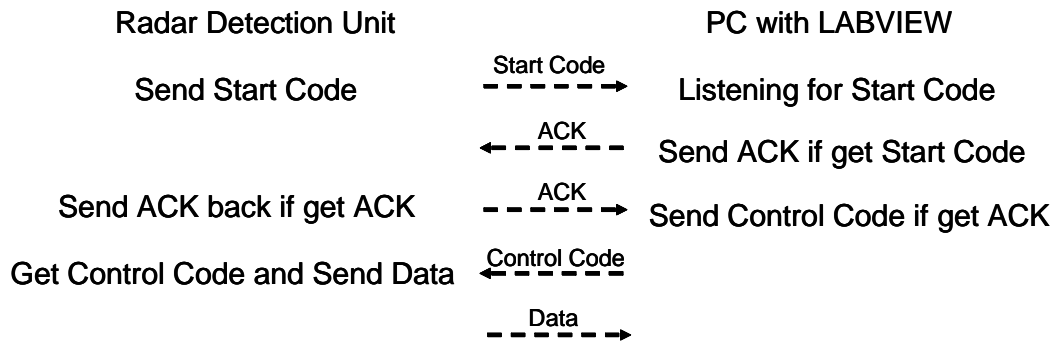


Figure 2-6: Protocol of UART

Fig. 2-6 is the diagram of UART protocol. The terminator is in listening mode at the beginning. When start up the debug program, micro-processor send a start code and wait for a short time. If there comes back an ACK, it send an ACK back. Then terminator transmits the control code. Control code can choose which data to read, such as sample data and Chirp Transform result. Control code can also change some parameters in radar system, such as frequency modulation range.



Chapter 3

Improvement of Radar system

3.1 Previous Approach in Algorithm (2D-FFT)

The previous approach is to generate 70 continuous triangular control waves. Since there is some transience and distorts the receiving data, we ignore the beginning ramps. Each triangular control wave has 150 sample points to avoid the transience at the head and tail of control wave. Choose 128 points each control wave and put into FFT with Hanning window. So we can get 64 FFT results just as showed in Fig. 3-1. Then take 64 FFT results into FFT again (Fig. 3-2). In first FFT, we acquire the information of distance. In second FFT, Doppler effect can be separated out.

The trick of this approach is that after operating the first FFT, the results have amplitude and phase information. Since Doppler effect presents on phase, the phase of the received signal can acquire the Doppler frequency. Common mode noise results in DC tern in 2D-FFT and a moving target can easily detected.

There are some defects of this approach. First it needs a lot of computation. In this setting, it requires 128 points FFT x 64 times and 64 points FFT x 128 times to get hole 2D spectrum result. Second is the common mode noise will blank the static target. Third is that in order to avoid Doppler effect which distorts the distance information, control wave frequency should higher enough. Doppler effect makes receiving signal shift

in frequency domain and the shift level is proportional to relative velocity and operation frequency. In order to bear higher relative velocity, the control voltage slope comes larger. In the setting, frequency resolution is $\frac{150}{128} \frac{1}{T}$ and Doppler effect should less than a frequency resolution. Since this radar system implements in an imbedded system, smaller T not only needs a faster AD/DA but also increases the cost of this system.

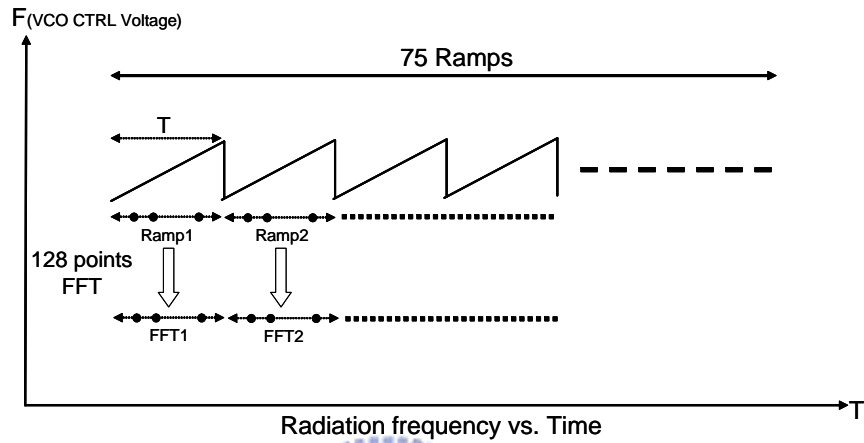


Figure 3-1: First FFT Operation

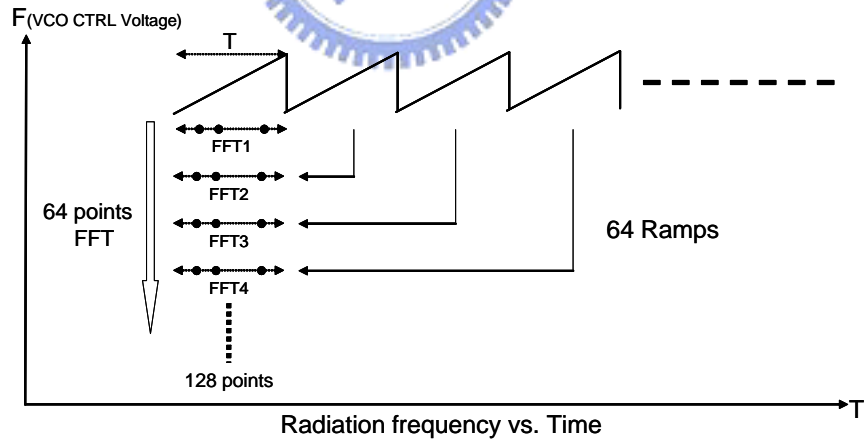


Figure 3-2: Second FFT Operation

3.2 New Approach in Algorithm

3.2.1 Triangular Control Wave

In previous approach, there should have a fast AD/DA, large RAM size and a DSP core to calculate so many FFT points. Looking at the frequency modulation wave in previous approach, it just uses the rising edge. What if we use a triangle modulation wave? In Fig. 3-3 is the new control wave and triangle shape has two side information. If the target is approaching to radar, Doppler effect shift the receiving signal upward. If we call F1 as the frequency of rising part IF signal and F2 as the frequency of falling part IF signal, F1, F2 are different about two times Doppler frequency.

$$F1 = \text{Distance frequency} - \text{Doppler frequency} \quad (3.1)$$

$$F2 = \text{Distance frequency} + \text{Doppler frequency} \quad (3.2)$$

Plus F1 and F2 together can cancel Doppler effect and F2 minus F1 can get two times of Doppler frequency. This simple change makes us to use Doppler effect rather than to against it. There are some conclusions of this new approach. (1)It can easily cancel Doppler effect. (2)Comparing F1, F2 can get the relative velocity and whether the target is approaching or not. (3)This approach can slow down AD/DA update rate. Because it doesn't need to avoid Doppler effect distortion but using it. (4)It can apply several decision condition to avoid noise. For example, rising part and falling part should detect the target at the same time. The frequency difference between rising part and falling part should be limited in a range. It can ignore many random noise and lower the false alarm rate. (5)New approach only need twice 128 points FFT which saves a lot of memory and a slower micro-processor is enough.

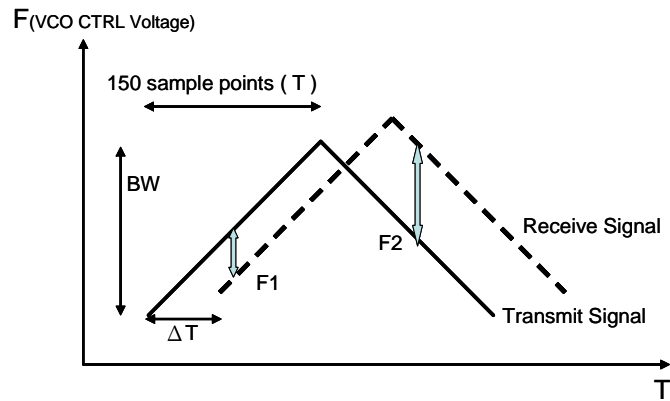


Figure 3-3: Triangular Control Wave

3.2.2 Triangular Control Wave Test Result

Fig. 3-43-5 are the test result of this triangular control wave. There is a moving car at the speed 10km/hr and the direction is away from the radar. In Fig. 3-43-5 there are two peak in the test result. That is because a car may have more than one reflection center and will result in multi-peaks in frequency domain. The test car is in the direction away from radar system and the test result of rising part of control wave will higher than falling part. Fig. 3-4 is the rising part and Fig. 3-5 is the falling part. It is easy to find that the result of rising part has one index more than the falling part. One index difference means the relative velocity is about 10km/hr and is quite match the test condition.

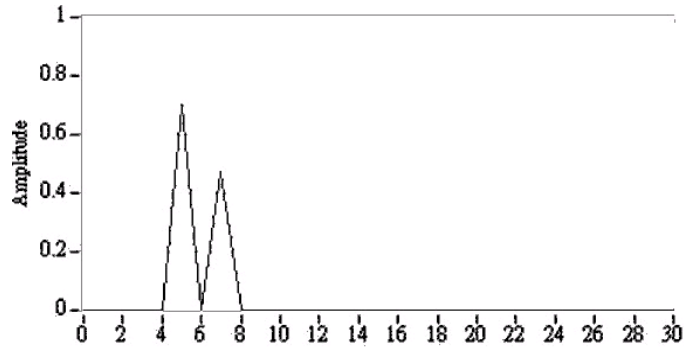


Figure 3-4: Test Result of Rising Part



Figure 3-5: Test Result of Falling Part

3.2.3 Zero Padding

We know that distance resolution depends on the bandwidth. But according to FCC mask, only 200MHz bandwidth can be used. Ideally, 75cm is the natural limitation in distance resolution. What if we want the target position more precisely? In digital signal processing there is one way called “Zero Padding”. Under the same sampling rate and the same sample point, frequency resolution is already decided as $\frac{\text{sampling rate}}{\text{sample points}}$. But we can fill up the result between each frequency index by zero padding[4].

Zero padding is that add several zeros at the head and tail of the signal. In Fig. 3-6(a) is the diagram of zero padding. First generate a 5.7KHz 128 points sine wave signal (Fig. 3-7(a)). Apply Blackman window on this test signal and then adds 128

zeros (Fig. 3-7(b)). After FFT operation, the maximum value appears at 6KHz without zero padding. Using zero padding, the maximum value is at 5.5KHz. So the frequency resolution becomes two times better than normal FFT and distance resolution becomes two times better also. Fig. 3-8 is the simulation result.

Next step is to implement this approach in C code after the simulation of zero padding. Fig. 3-6(b) is the diagram of Chirp Transform calculation with zero padding. Add zeros at the head and tail of data as a new data. Then operate Chirp Transform on the new data set. Since Chirp Transform is more flexible than FFT, we can use some programming skill to lower the computation quantity. In Fig. 3-6(a), every data should multiply with a coefficient and add together. Zeros also multiply and add together but they waste the computation resource. So, just change the first for loop of the C code in Fig. 2-5. Shift the start index from 0 to zero numbers then zero padding is easily implemented.

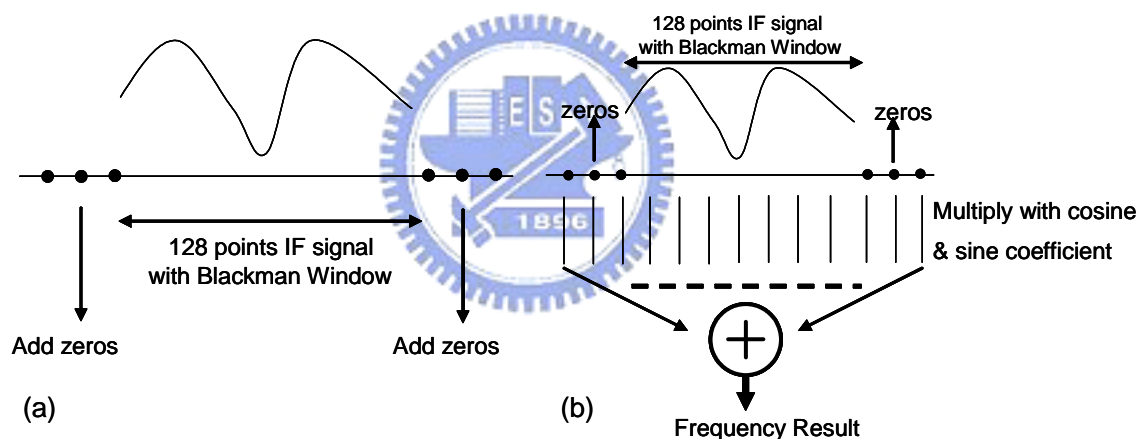


Figure 3-6: (a) Diagram of Zero Padding (b) Diagram of Chirp Transform Calculation with Zero Padding

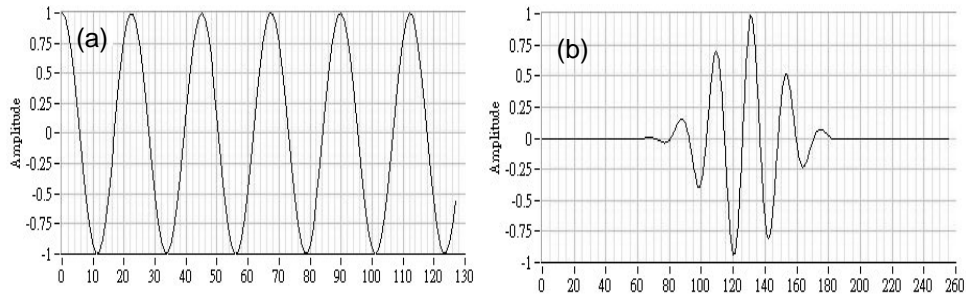


Figure 3-7: (a) 128 points 5.7KHz sine waveform (b) Test Signal with Blackman Window and Zero Padding

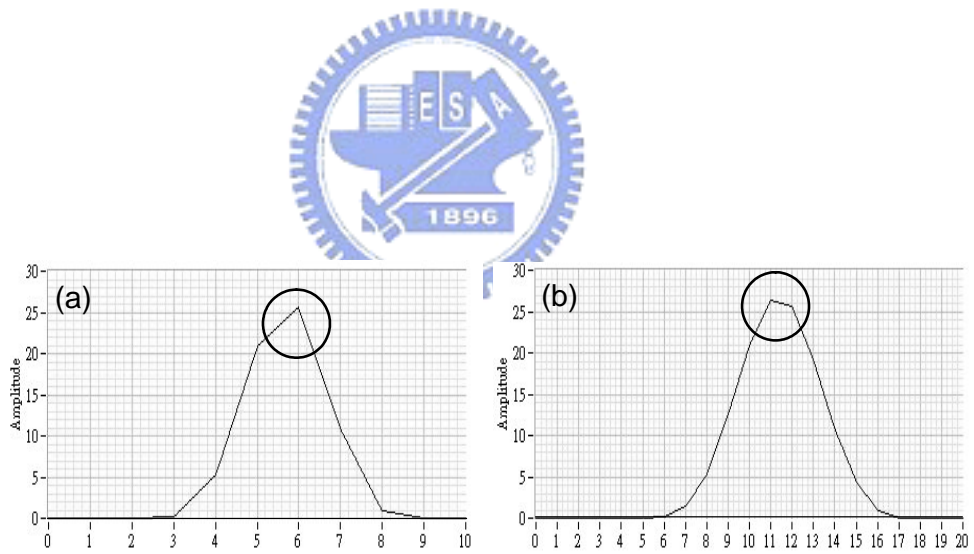


Figure 3-8: (a) Without Zero Padding Frequency Result (b) With Zero Padding Frequency Result

3.3 Improvement in IF Amplifier

There is a back ground noise in FMCW radar system naturally. Output power flatness will cause an AM modulation and result in a low frequency back ground noise. Self-mixing in mixer, antenna leakage and leakage wave in RF module will also result in a back ground noise. Fig. 3-9 is the IF signal under previous IF amplifier and Fig. 3-10 is the FFT result. It is easy to find that back ground noise is in lower frequency.

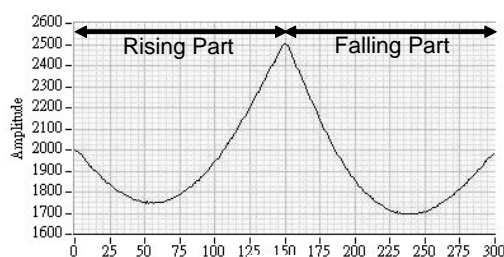


Figure 3-9: IF Signal in Previous IF Amplifier

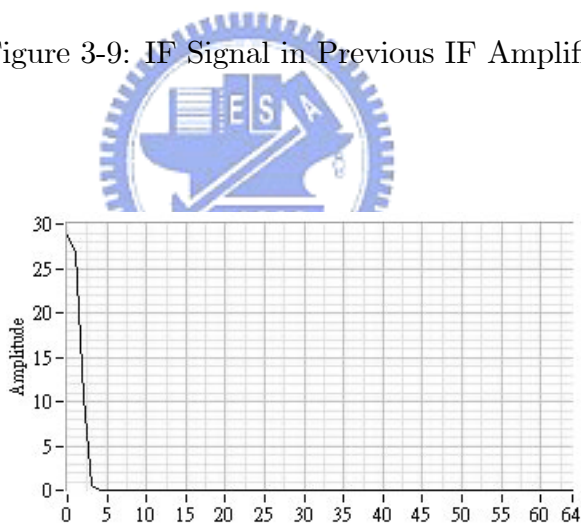


Figure 3-10: FFT Result of IF Signal

Since the wanted frequency is also start from DC, this overlap between back ground noise and wanted signal results in two problem. One is that back ground noise is too large and blinds the region near to radar. Second is that back ground noise limits IF amplifier gain and makes system sensitivity poorer. Fig. 3-11 is the diagram of limitation in frequency domain. In region 1, back ground noise dominate the noise floor. In region 2 and region 3 the skirt of back ground noise and quantization error consist the noise floor. Region 2 is the previous detection region. Quantization error dominates the noise floor in region 3 because the skirt of back ground noise is quite lower then in region 2. How can we suppress the quantization error noise?

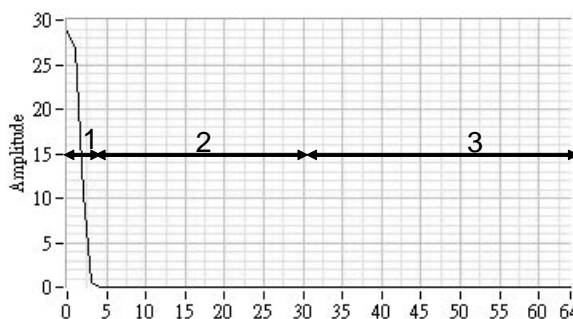


Figure 3-11: Diagram of the Limitation in Frequency Domain

Back ground noise is the limitation of gain in previous IF amplifier. But what if we move pole 1 to higher frequency. Fig. 3-12 is the frequency response of previous IF amplifier and the new one. Using IF amplifier as an active filter. Higher pole1 can suppress back ground noise and lower pole2 can filter out aliasing and noise in higher frequency. Once the back ground noise has been suppressed, higher IF amplifier gain is admitted. Signal in region 3 amplifies to higher voltage and improves the signal to noise ratio. Fig. 3-13 are the test result and a diameter in 15cm iron tube is the target. Fig. 3-13(a) is the result using previous IF amplifier frequency response and Fig. 3-13(b)

is the result of new one. The farthest detection distance moves up to 17m and system sensitivity improves about 10dB. This new IF amplifier provides higher gain and noise floor in region 3 dominates by RF module.

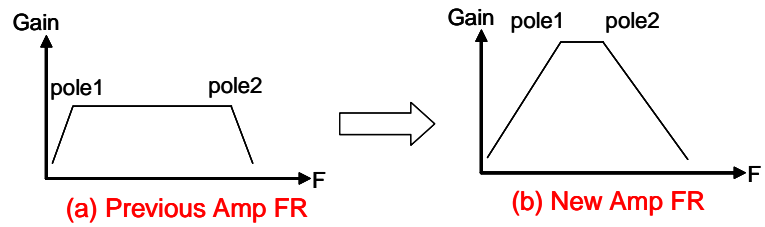


Figure 3-12: (a) Frequency Response of Previous IF Amplifier (b) Frequency Response of New IF Amplifier

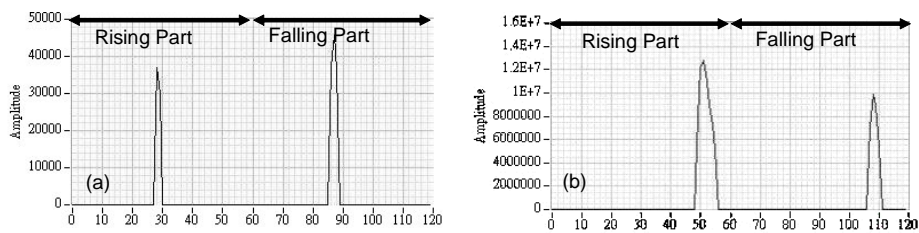


Figure 3-13: (a) Test Result with Previous IF Amplifier (b) Test Result with New IF Amplifier

Chapter 4

6GHz Compact Size FMCW Radar System

We try to built a compact size 6GHz FMCW radar system base on the experience in 24GHz FMCW radar. In 24GHz FMCW radar, there are two antennas to lower the interaction between Tx path and Rx path. And since it is built by discrete component, it's hard to generate a 24GHz source directly. So there comes two frequency doubler and more RF circuit make the module size larger.

In 6GHz FMCW radar system, we try to use as less components as possible. There is only a 6GHz VCO, a 90° hybrid mixer and uses one antenna for both Tx and Rx. Fig. 4-1 is the block diagram of compact size 6GHz FMCW radar system RF module. In the following article, we will have some discussion on antenna, mixer, filter and VCO. First is two different antenna types. One is a compact size novel wideband antenna and another is a 2 x 1 antenna array using aperture couple antenna.

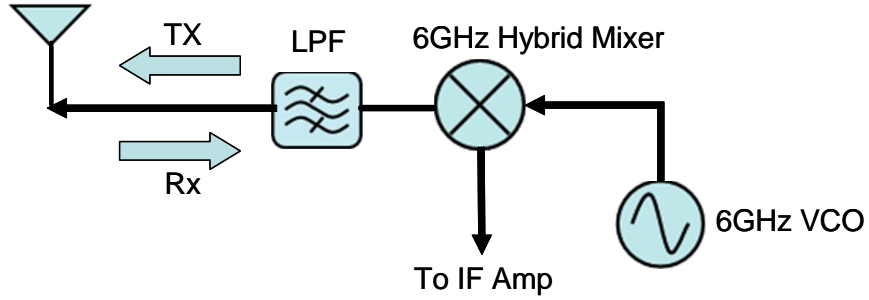


Figure 4-1: 6GHz Compact Size FMCW Radar Block Diagram

4.1 Novel Wideband Antenna Configuration

Recently there is tremendous demand for the development of wireless communication systems or mobile phone system. In order to have compact size device, several antenna structures with small dimension are proposed. Inverted-F antenna is a common structure. One shorted end makes it only quarter wavelength. This structure can provide E-plane and H-plane current path make its radiation pattern more omni-direction.

In order to integrate with other circuit, printed inverted-F structure is proposed (Fig. 4-2)[5]. In Fig. 4-2 there is a big gap G in traditional printed inverted-F antenna. What if we reduce the gap size? Lower the gap size and move the antenna quite close to the ground plane can highly improve antenna bandwidth. So in the article, we propose a wideband antenna structure with small gap proximity to ground plane and will discuss several parameters and their effect.

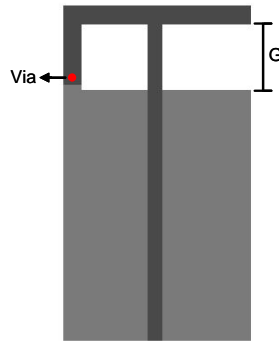


Figure 4-2: Configuration of Inverted-F Antenna

4.1.1 Antenna structure and Parameter discussion

When designing an antenna, we should consider not only how much area antenna has but also the ground plane size. In this antenna we decide to use on a dungo size device. So the ground plane we choose is 20mm x27mm. Fig. 4-3 illustrates the geometry of this investigated antenna. It is printed on 0.8mm FR4 with micro-strip line feed. The area of the antenna is 19mm x 11.5mm $((L1+L2) \times H)$, ground plane is 20mm x 27mm with the gap (G) 0.8mm and there is a via short to ground plane. Next we will discuss the effect of several parameters and all those comparisons are simulated in HFSS 8.0.

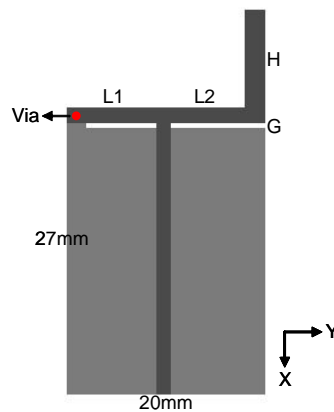


Figure 4-3: Geometry of Novel Wideband Antenna

First separate this wideband antenna structure into two part. One is the main radiator at the right side. Another is a short end at the left. The main radiator in Fig 4-4 is just like a monopole antenna serial with one transmission line. But the transmission line doesn't lie right on the ground plane. So it has high impedance an will generate some radiation. Comparing these two antenna structures we can find out that add this radiant transmission line can highly improve return loss bandwidth (Fig. 4-5).

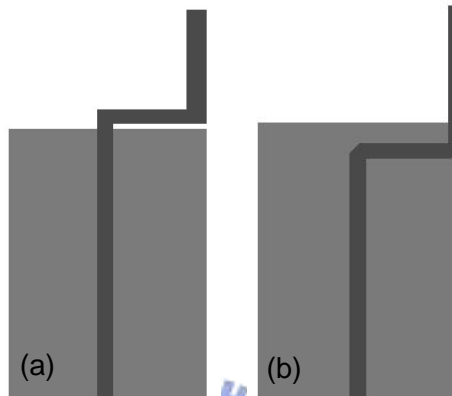


Figure 4-4: (a) Right Part of Wideband Antenna with Radiant Transmission Line (b) Right Part of Wideband Antenna without Radiant Transmission Line

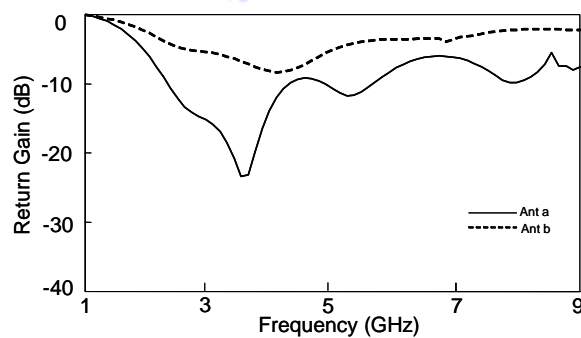


Figure 4-5: Simulation Result of With and Without Radiant Transmission Line.

Fig. 4-6 demonstrates the simulated result in different gap distance (G). This the new wideband antenna is similar to traditional inverted-F but the gap proximity to ground plane is different. In order not to change the lowest frequency, we keep total length ($L1+L2+H+G$) as constant. We choose several gap values from 4 mm to 0 mm. When G becomes smaller, the effect become stronger. By changing G the bandwidth become wider and there comes a new deep in higher frequency. In here $G=0.5\text{mm}$ has the widest bandwidth.

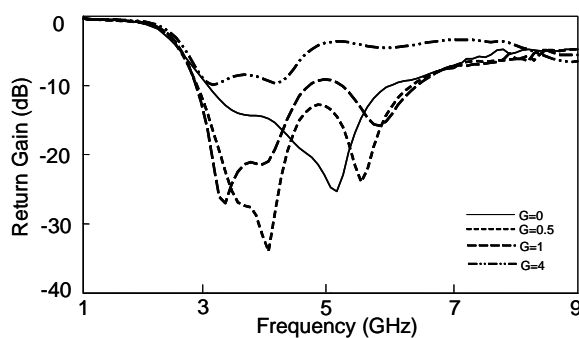


Figure 4-6: Simulated Result of G from 0mm to 4mm



In Fig. 4-7 we change H and find out that the deep locations change. Since this antenna can be treat as a monopole with two matching transmission line. The length H just like a monopole antenna load. When H becomes larger, frequency becomes lower. Since $L1$, $L2$ and G keep un-changed, the matching circuit is the same.

Fig. 4-8 shows the relationship between $L1$ and return lose. We choose several $L1$ values from 4.5mm to 9mm and the band-width doesn't change much but shift to lower frequency when $L1$ is shorter. At the beginning, we seperate this antenna into two part. The wideband mechanism is a monopole with a radiate transmission line and $L1$ is a matching circuit which makes the bandwidth wider.

Fig. 4-9 is the result of different $L2$. Variation of $L2$ has great effect at the deep

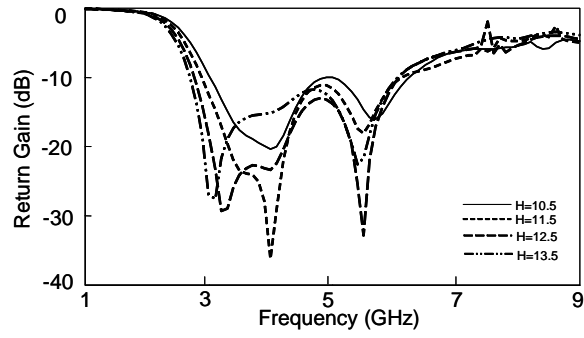


Figure 4-7: Simulated Result of H from 10.5mm to 13.5mm

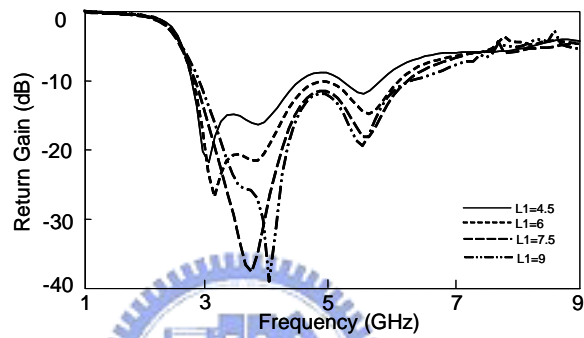


Figure 4-8: Simulated Result of L1 from 4.5mm to 9mm

locations and bandwidth. In the next several Smith Chart (Fig. 4-10 Fig. 4-11), we put different L2 simulation results into Smith Chart to find out how L2 effect. When L2 become smaller, it pulls the S-parameter closer to center. At the same G size, L2 is a critical part of wideband matching.

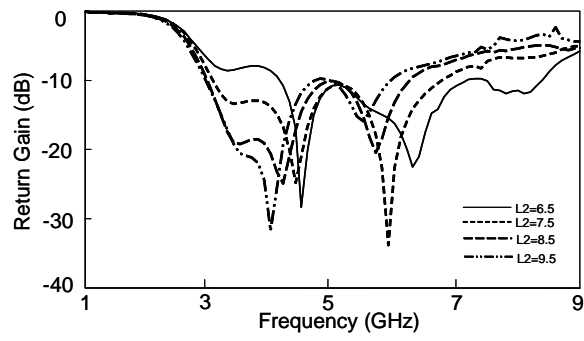


Figure 4-9: Simulated Result of L1 from 6.5mm to 9.5mm

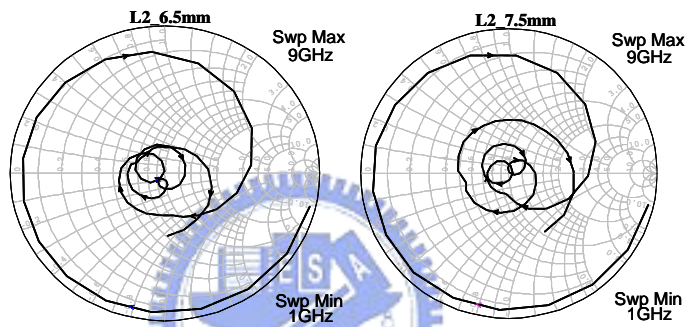


Figure 4-10: L2=6.5mm & L2=7.5mm

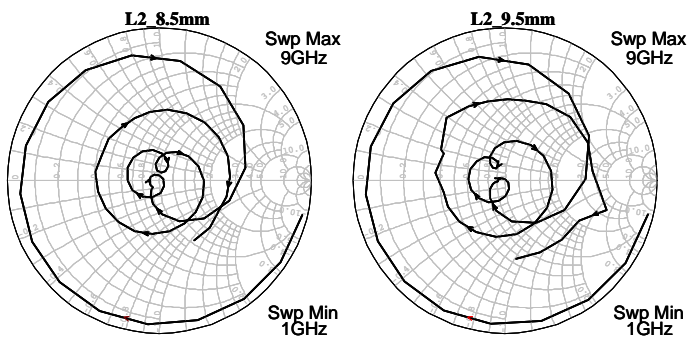


Figure 4-11: L2= 8.5mm & L2= 9.5mm

From the comparison before, we know that monopole with radiant transmission line is naturally a wideband structure. Now we just simulate the right part of novel wideband antenna and only change the gap size. In Fig. 4-12 when gap is precisely chosen, the bandwidth can be quite large to about 2GHz. There is a deep in higher frequency and is caused by the discontinuity of antenna.

Base on this wideband structure, we propose a wideband antenna with its bandwidth from 3.1GHz to more the 9GHz. Antenna size is 14.6mm x 10mm ((L1+L2) x H). The main radiator is like a triangle. It can provide longer and different current path for lower frequency. Then use radiant transmission line for wideband purpose. Use the short end to smaller the size to quarter wavelength and be the final matching too. By tuning those parameters we have this wideband antenna in such a small size. Fig. 4-13 is the structure of this wideband antenna and Fig. 4-14 is the measurement return gain of it.

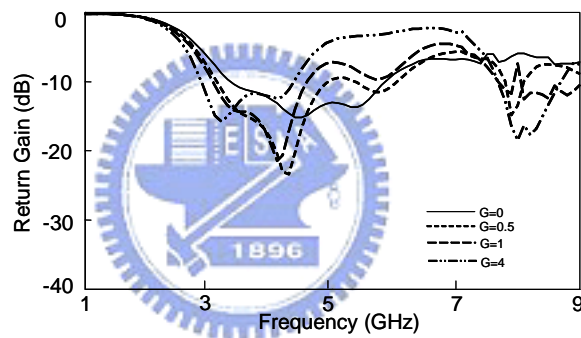


Figure 4-12: Right Part Only and Change G from 0mm to 4mm

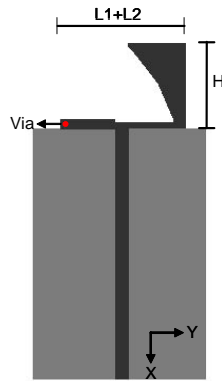


Figure 4-13: Novel Wideband Antenna Structure

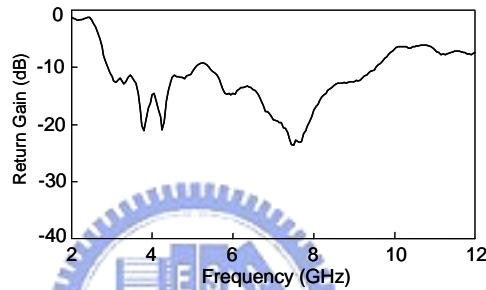


Figure 4-14: Return Gain of Wideband Antenna

4.1.2 Antenna Pattern

There are the radiation patterns in 3.5GHz and 7.5GHz. Main radiator has a radiation pattern similar to a monopole and the transmission line ($L1+L2$) which proximity to the ground compensates some null in radiation pattern. With this radial transmission line, the total field becomes more omni direction. When the frequency becomes higher that transmission line generates more radiation. In 7.5GHz the antenna gain is smaller then zero. This may causes by the loss of fr4.

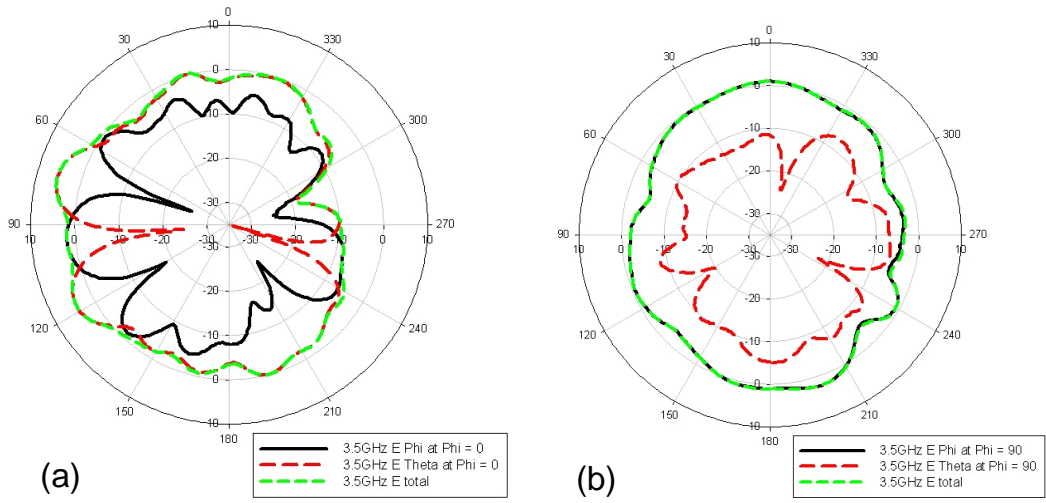


Figure 4-15: (a) XZ plane in 3.5GHz (b) YZ plane in 3.5GHz

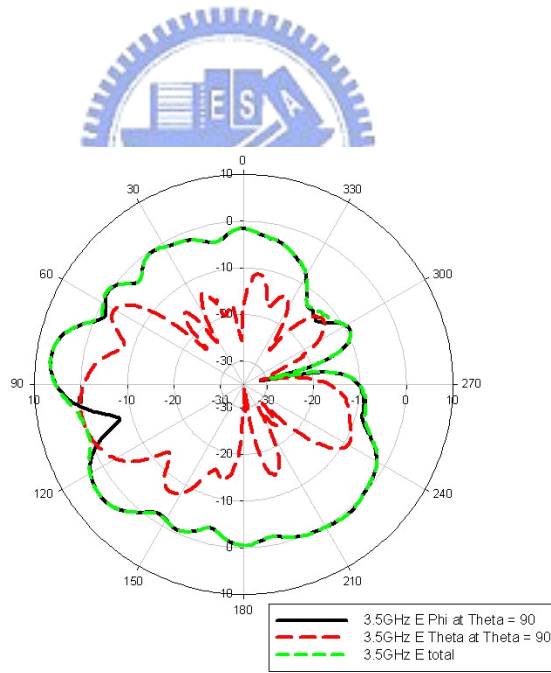


Figure 4-16: XY plane in 3.5GHz

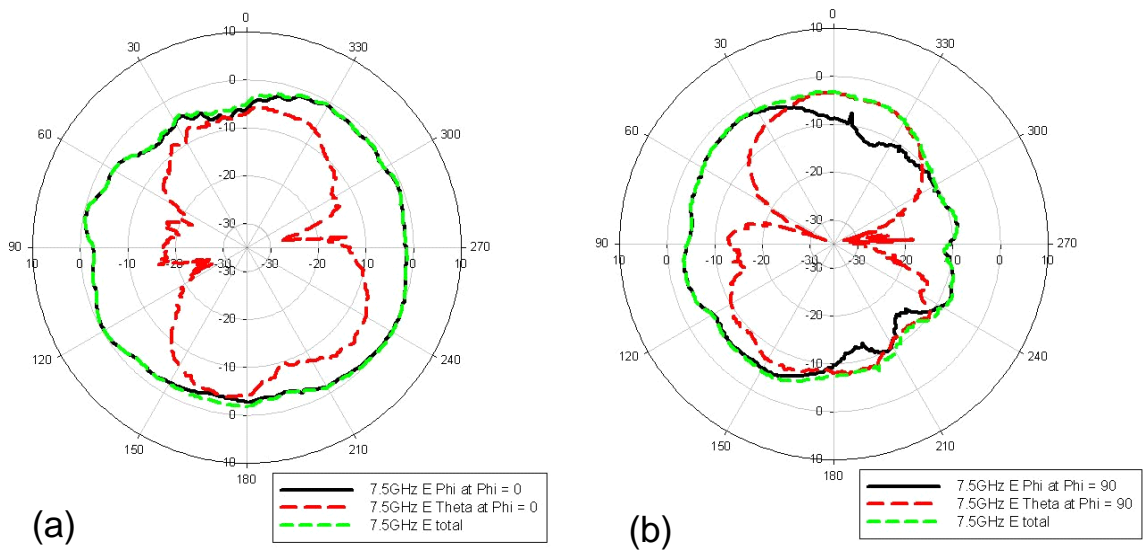


Figure 4-17: (a) XZ plane in 7.5GHz (b) YZ plane in 7.5GHz

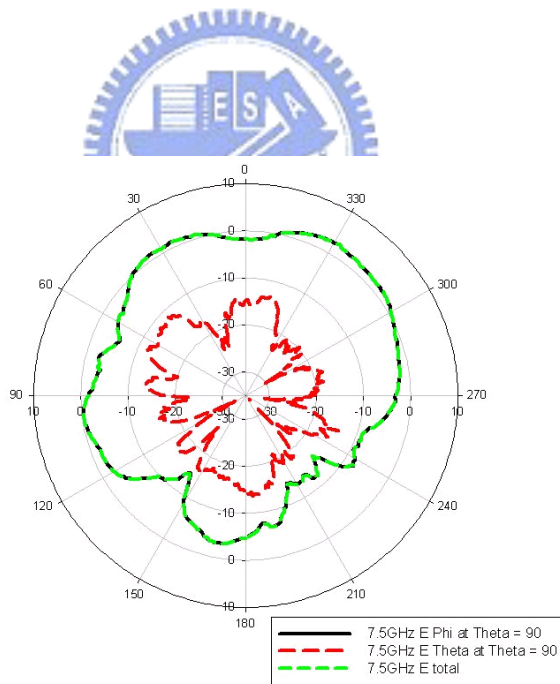


Figure 4-18: XY plane in 7.5GHz

4.2 Aperture Couple Antenna Array

In chapter 4.1 is a wideband antenna structure. It has an omni-direction radiation pattern but in some application the radiation pattern should be more directivity. In this section, we propose a aperture couple antenna array. This can avoid some reflection from the un-wanted region such as ground plane.

4.2.1 Aperture Couple Antenna Array Configuration

Fig. 4-19 is the structure of this antenna array[6]. Fig. 4-19(a) is the slot and the feed line. Fig. 4-19(b) is the main radiator. Fig. 4-20 is the sight draft of this antenna array. Total size is 46mm x 70mm x 5mm (W x L x H) and uses 0.4mm fr4. The feed line excites the the radiator through the aperture. Once the operation frequency is decided, the size of the main radiator also decided. The over length of the feed line is used to tune the matching and the length and width of slot also effect the matching. The main radiator is about $\lambda/4$ of the operation frequency and the distance between two radiator is $\lambda/2$. Aperture couple antenna has narrower beam width then normal patch antenna, so two antenna elements is enough.

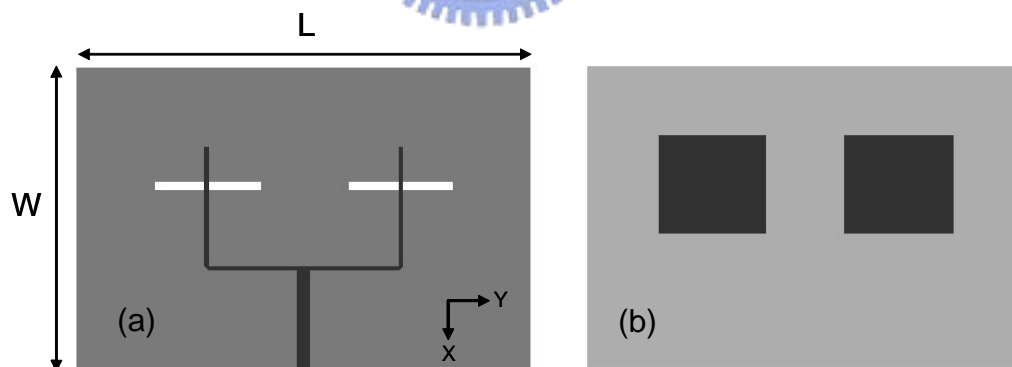


Figure 4-19: (a) The Lower Part of Array (including feed line and slot) (b) The Upper Part of Array



Figure 4-20: Sight Draft of Antenna Array

4.2.2 Return Gain and Antenna Pattern

This aperture couple antenna array has 400MHz bandwidth from 5.8GHz to 6.2GHz. Half power beam width in XZ plane is 42° and peak gain is 10.8dBi.

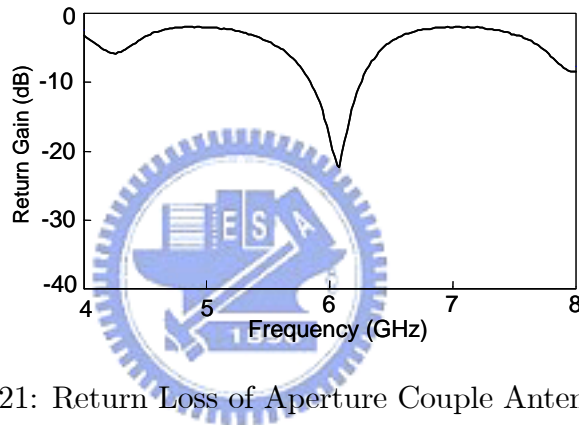


Figure 4-21: Return Loss of Aperture Couple Antenna Array

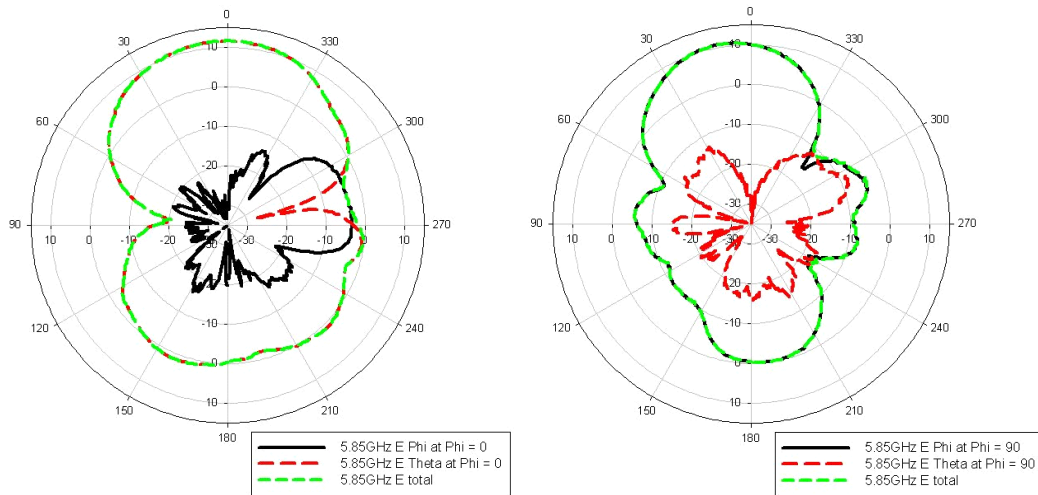


Figure 4-22: Aperture Couple Antenna Array Radiation Pattern in XZ and YZ plane

4.3 Compact Size Low-pass Filter

In Fig. 4-1, there is a low-pass filter after the hybrid mixer to filter out all harmonic frequencies generated by the circuit. In this radar structure there only needs a low-pass filter not a band-pass filter to filters out VCO fundamental frequency. So a low-pass filter with zeros at 12GHz and 18GHz is enough and that makes the circuit in small size. Fig. 4-23(a) is the layout of this filter and Fig. 4-23(b) is the equivalent circuit. Total size is 4.6mm x 3.2mm (L x W) on 20mil RO4003. There comes two zeros. One is the parallel inductor with couple capacitor. Another is the serial inductor with capacitor to ground. The equivalent circuit is a common type of low-pass filter[7]. Fig. 4-24 is the measurement result. There is one pole near 12GHz to filter out second harmonic frequency and another pole is at 17GHz. Although we want to put the first pole at 12GHz and the next pole at 18GHz these two poles have interaction and is hard to modify them indepently.

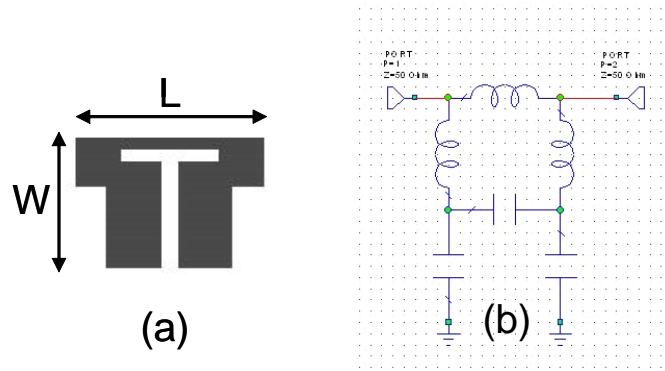


Figure 4-23: (a) Lowpass Filter Layout (b) Filter Equivalent Circuit

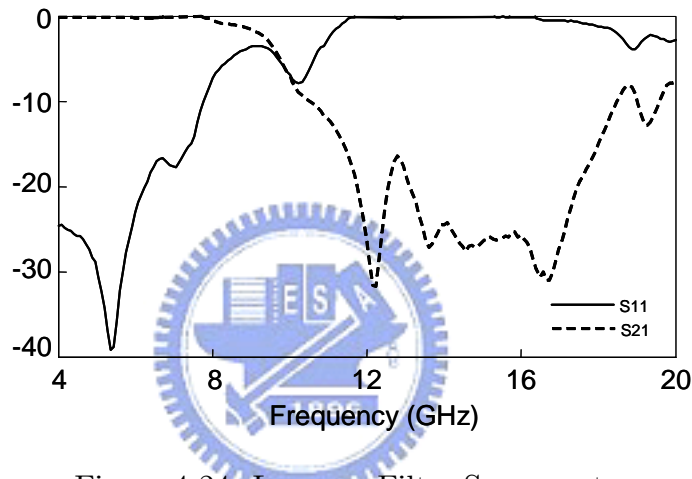


Figure 4-24: Lowpass Filter S parameter

4.4 Hybrid Mixer

Fig. 4-25(a) is the schematic of hybrid mixer[8]. It consists of a quadrature hybrid and two low barrier schottky diodes. The symmetrical structure can compensate the common mode noise. With high LO power and low barrier diode, there needs no extra bias network to improve the conversion loss. Because the Lo signal is far away from IF signal, it only needs a simple quarter open stub and a LC network to perform as a LPF.

90 hybrid splits the LO signal with equal amplitude and 90 phase difference to mixing

diodes. These signals are reflected and combine at the antenna port. The insertion loss of this hybrid mixer is the summation of reflection loss from diode and hybrid loss. The received signal also splits by this 90 hybrid. The IF signal comes 180 phase difference and a operational amplifier is used as a balun and active filter.

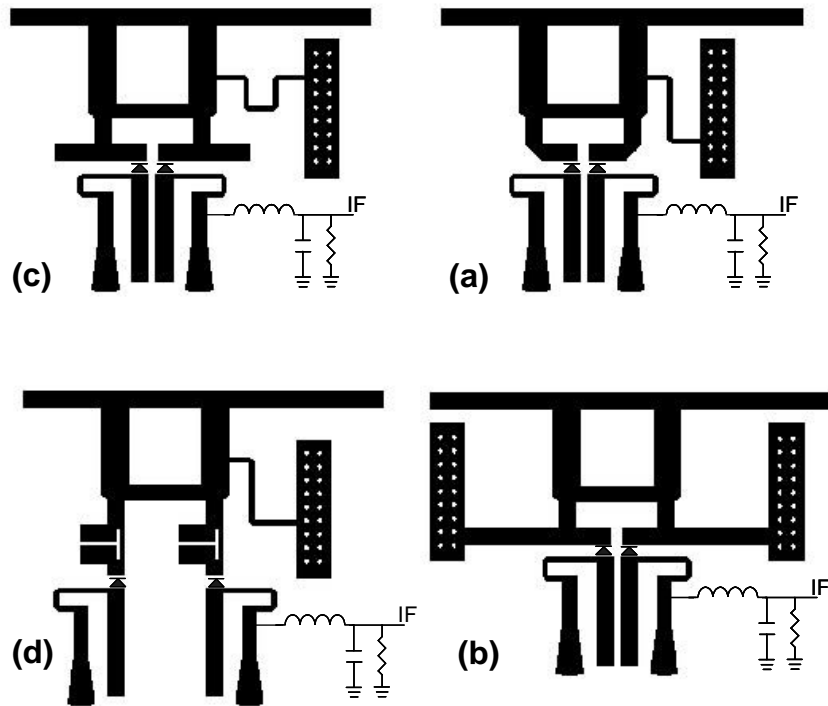
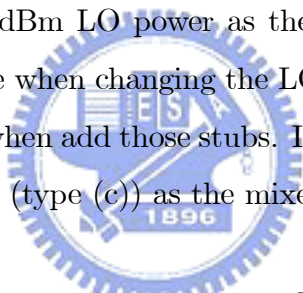


Figure 4-25: (a) Normal Hybrid Mixer (b) Hybrid Mixer with Short Stub (c) Hybrid Mixer with Open Stub (d) Hybrid Mixer with Filter

4.4.1 Hybrid Mixer Improvement and Test Result

In basic hybrid mixer structure it has 1.7 dB insertion loss and 12 dB conversion loss. Is there any approach to improve the performance without increasing too much area? There are some papers[9][10] discussing the improvement of conversion loss. We can have a conclusion that at each port (LO port, RF port and IF port) if the wanted frequency can pass and the un-wanted frequency is reflected, this will be an optimum conversion loss mixer.

IF port has a LPF and quarter wave stub in hybrid mixer so LO signal and RF signal can't through. RF port and LO port are the same and should reflect the un-wanted signal. To achieve this purpose, we try to add some stub or filter at RF port. Fig. 4-25 is the schematic of hybrid mixer. There are some different types; open stub, sort stub and compact size LPF. All those external circuits are used to reflect the second harmonic frequency back to the mixing diode. Fig. 4-26 is the comparison result and the comparison is base on 6dBm LO power as the condition this module is. And the test results are quite the same when changing the LO from 4dBm to 8dBm. There comes about 1~2dB improvement when add those stubs. In order to save more space, we choose the structure with open stub (type (c)) as the mixer in this radar module.



Mixer type	Insertion Loss	Conversion Loss
Type (a)	1.7dB	12dB
Type (b)	1.7dB	11.5dB
Type (c)	1.5dB	10dB
Type (d)	1.3dB	11.3dB

Figure 4-26: Mixer Comparison Result with 6dBm LO Power

4.5 Voltage Control Oscillator

For a BJT negative resistance oscillator the most effective network is the common base configuration[11]. An serial inductor from base to ground can easily generate negative resistance but it is for low output power use. In this radar module, we choose common emitter network to generate high output power. There is a open stub at the collector to obtain negative resistance. A micro-strip line and a varactor connects to the base as LC tank and derive the signal at the emitter. For better performance discrete components only use as bias and bypass. Fig. 4-27 is the schematic of this oscillator. Fig. 4-28 is the layout of this oscillator. Fig. 4-29 is the phase noise measurement result. It is -101 dBc/Hz @ 100KHz, -124dBc/Hz @ 1MHz and the output power is 12dBm.

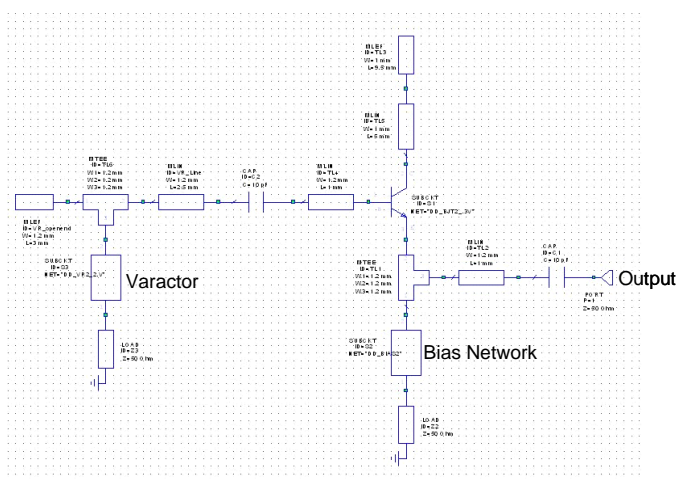


Figure 4-27: VCO Schematic

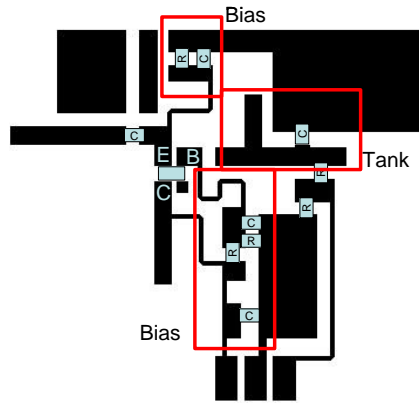


Figure 4-28: VCO layout

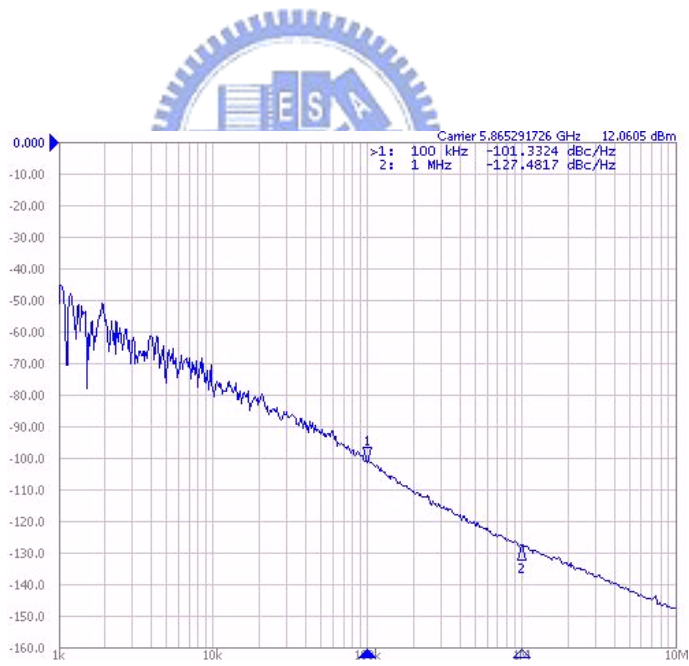


Figure 4-29: Phase Noise of VCO

Chapter 5

6GHz FMCW Radar System Integration and Measurement

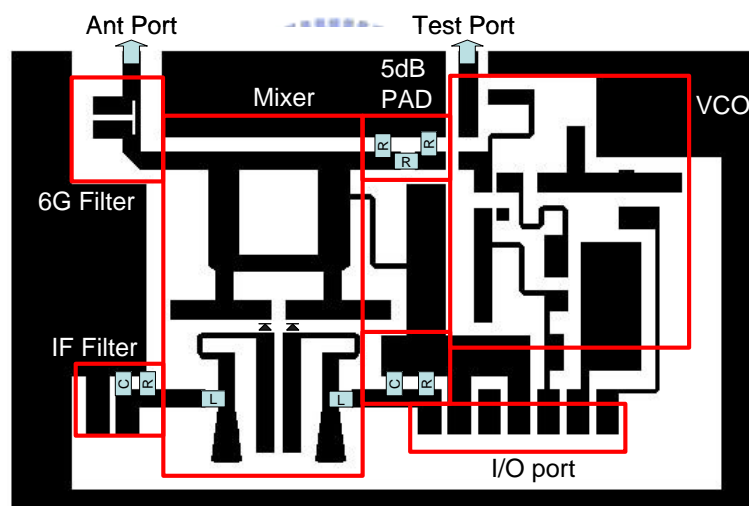


Figure 5-1: RF Module Layout

Fig. 5-1 is the RF module layout of this Radar system. The dimension is 30mm x 50mm and implements on 20mil RO4003. The power consumption is less than 200mW under 5V supply voltage. There is a 5dB PAD after 6GHz VCO. Generally, There is an

amplifier or a frequency multiplier next to oscillator. An amplifier can not only enhance power to push the next stage but also be a buffer to avoid load pulling effect. But to minimize circuit size, we use a 5dB pad to lower the load pulling effect. Even we do so, mixer and VCO still need to be co-designed. After mixer is a low-pass filter to suppress harmonic generated by mixer and VCO.

In Fig. 5-2 is the measurement result of this RF module. There is about 5dBm output power in the operation frequency range. The frequency sensitivity doesn't perform well but we can modify the control voltage shape to make the output frequency linearer. Fig. 5-3 is the harmonic test result. All harmonic frequencies are suppressed more then 40dB. This means that filter performs well.

Vt (V)	Output Frequency (GHz)	Output Power (dBm)	Sensitivity (MHz/V)
0	5.624	5.82	
0.5	5.6608	5.82	73.6
1	5.6975	5.78	73.4
1.5	5.7383	5.63	81.6
2	5.7833	5.45	90
2.5	5.83	5.28	93.4
3	5.88	5.18	100
3.5	5.9375	5.17	115
4	5.9883	5.22	101.6
4.5	6.0308	5.2	85
5	6.0675	5.52	73.4

Figure 5-2: RF Module Measurement Result

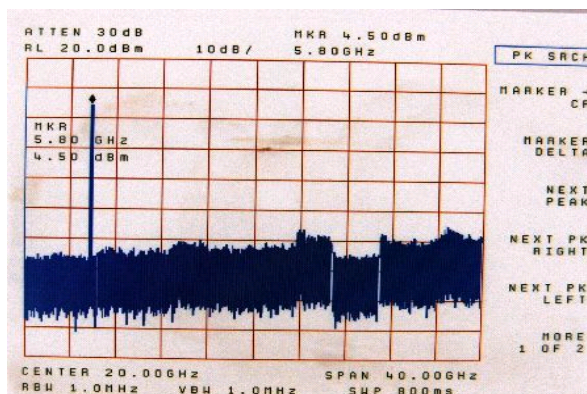


Figure 5-3: RF Module Output Spectrum

Since the hybrid mixer has differential IF output, an operational amplifier is used as balun and active filter. Fig. 5-4 is the schematic of IF amplifier. In the previous section, system sensitivity can be better by changing pole1 and pole2. The ratio of input and feedback resistor decides the amplifier gain and change the capacitors can modify pole position to find an optimum value. Fig. 5-5 is the test result of this 6GHz FMCW radar system. The target is an iron tube is 15cm diameter at 34.5m. NI DAQCard-6062E is used as the control wave generator and the ADC sampler. The frequency modulation bandwidth is 150MHz and the distance resolution is 1.2m ideally. Using zero padding technology the distance resolution upgrades to 0.3m. The detection result is at index 118 and the distance resolution is 0.29m. This is quite close to the expect result. Fig. 5-6 and Fig. 5-7 are the photographs of RF module and total system.

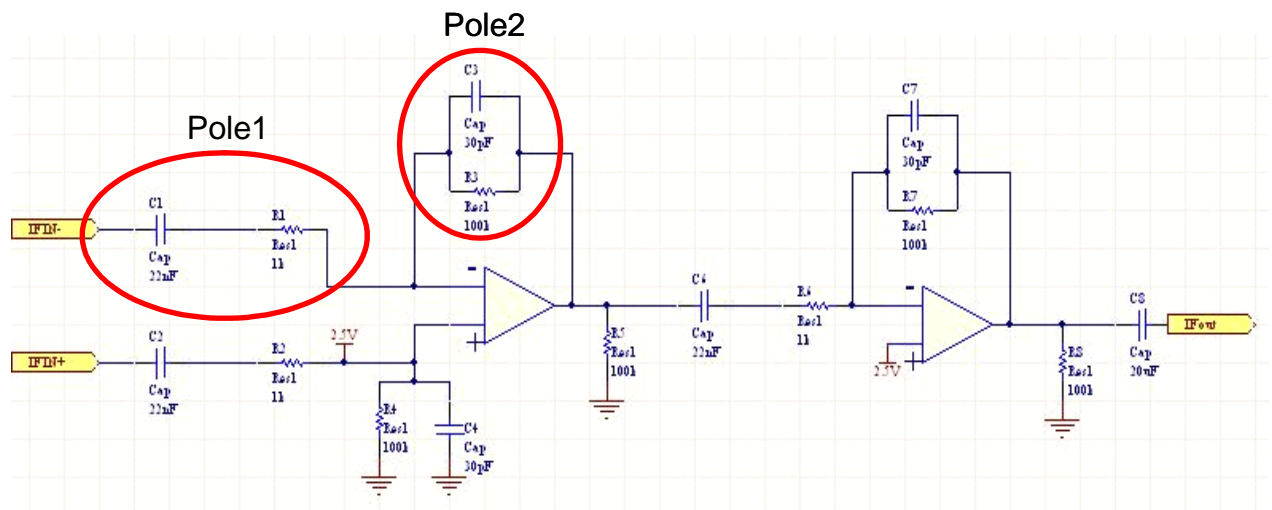


Figure 5-4: IF Amplifier Schematic

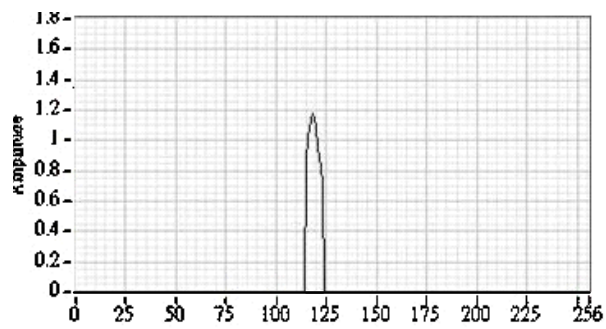


Figure 5-5: 6GHz FMCW Radar Test Result

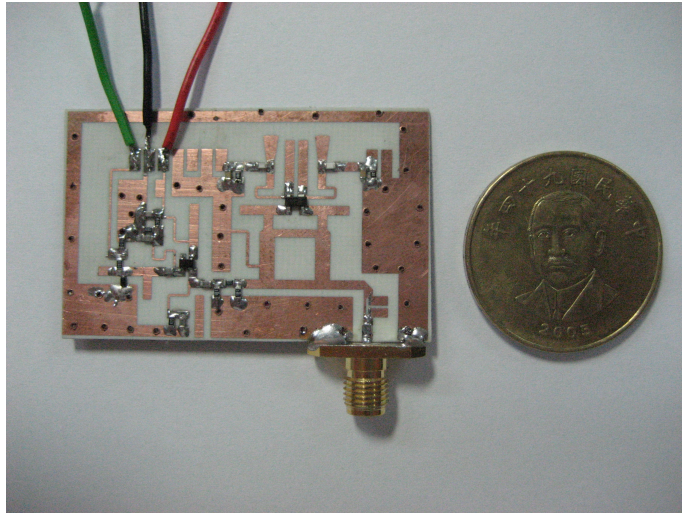


Figure 5-6: 6GHz Radar RF Module Photograph

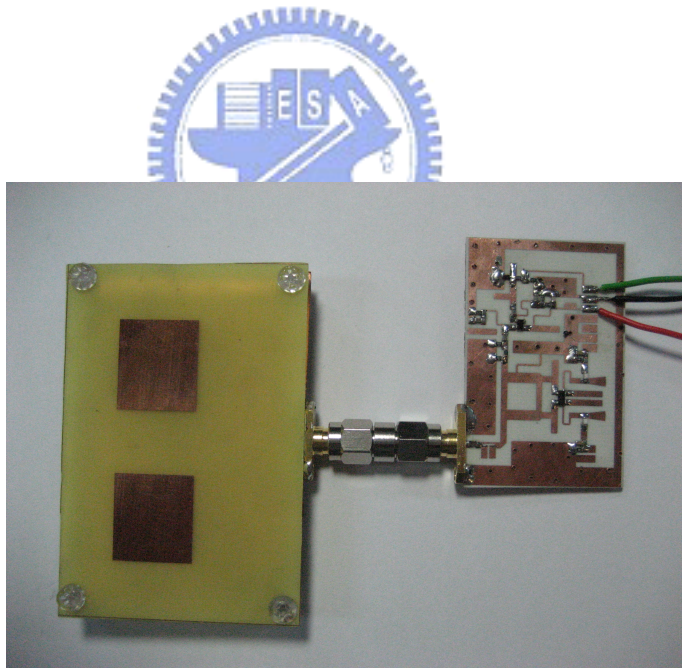


Figure 5-7: Photograph of Antenna Array and RF Module

Chapter 6

Conclusion

This article provides a compact size 6GHz FMCW radar module. From antenna to RF circuit and digital signal processing are all included. Different kinds of antennas can be chosen according to different applications. RF module has low power consumption and low cost either. In digital signal processing there are some improvements base on the experience in 24GHz FMCW radar system.

Triangle modulation wave increases system stability and saves a lot of system resource. Chirp Transform is more flexible then FFT and is easy to implement zero padding technology. The modified IF amplifier can increase system sensitivity about 10dB better and the detection range becomes two times farer then before.

The drawback of this radar system is the antenna size. The circuit performance is better in lower frequency and can accept more manufacturing torelance. But a radar system always needs high directivity and low operation frequency makes antenna larger. A compact size antenna with high directivity will be the future work.

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